

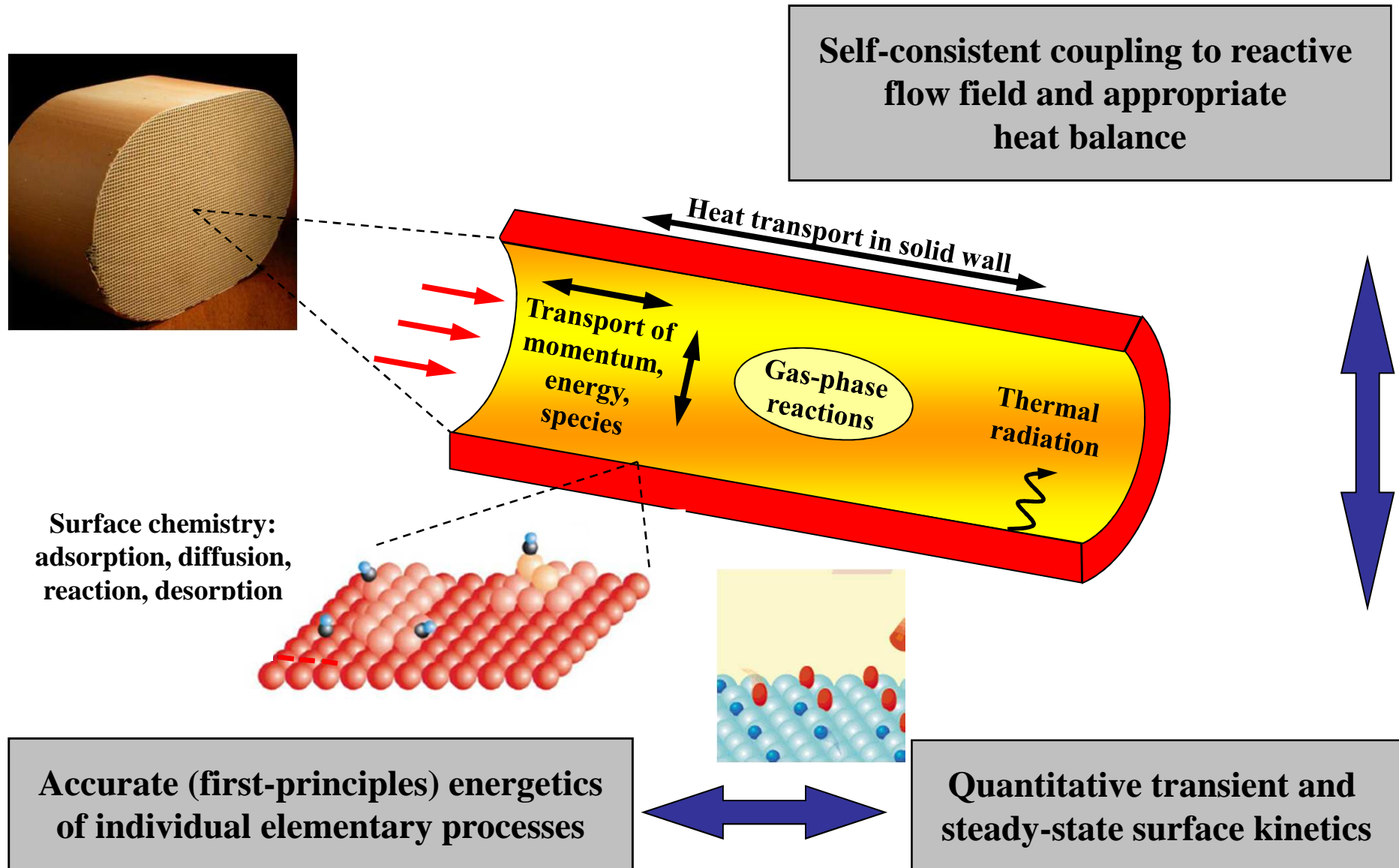


Towards a First-Principles Chemical Engineering

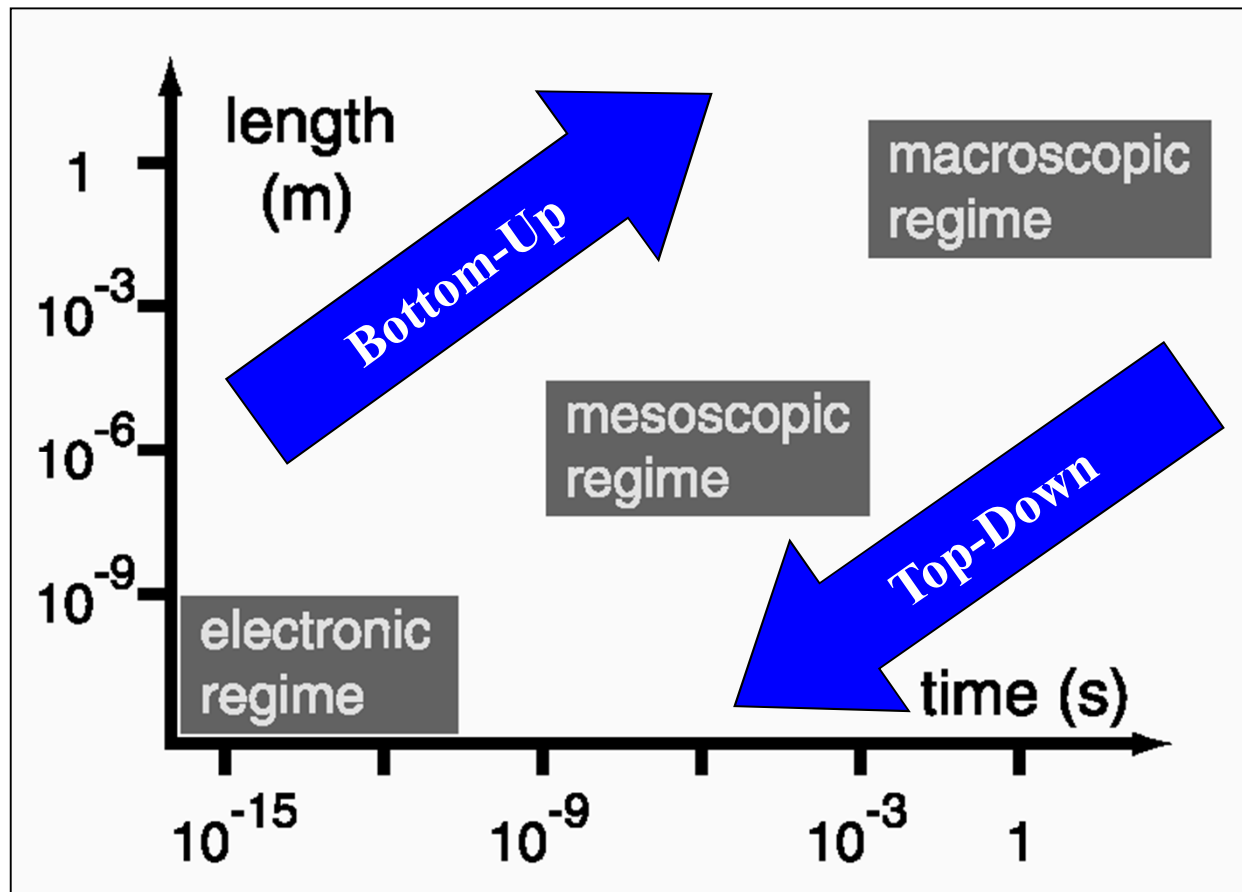
Karsten Reuter

**Chemistry Department and Catalysis Research Center
Technische Universität München**

Challenges across the scales



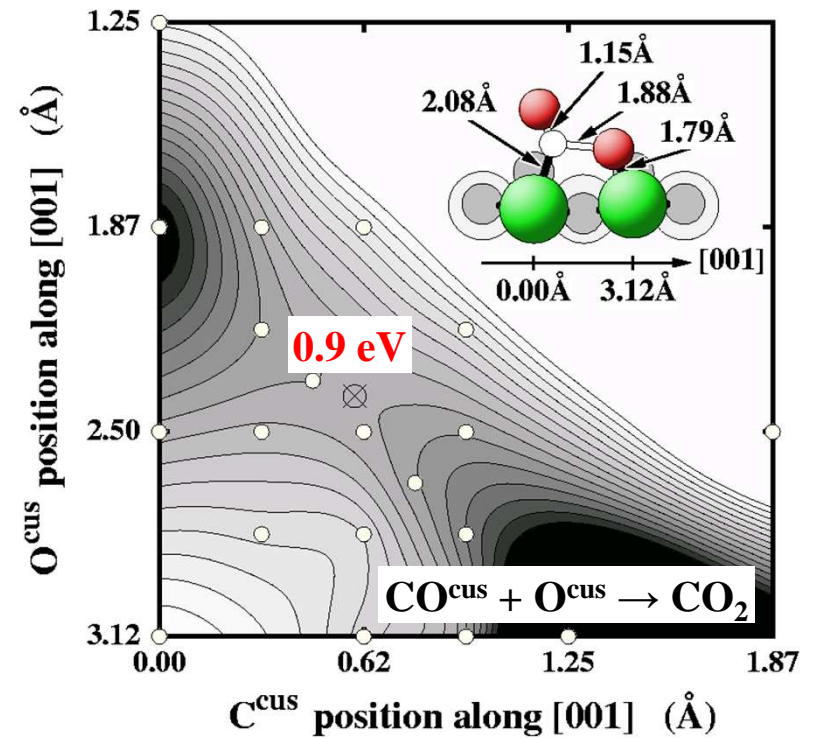
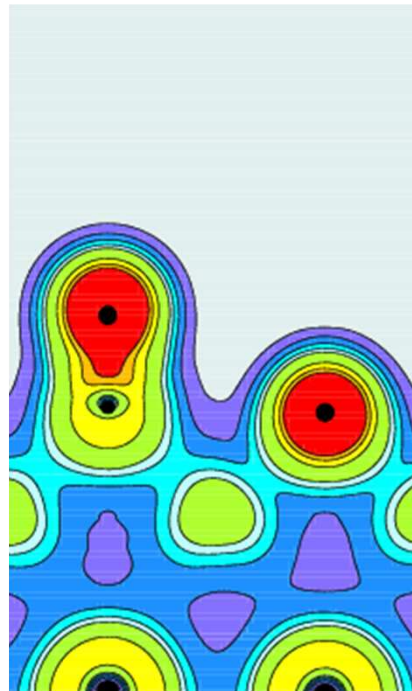
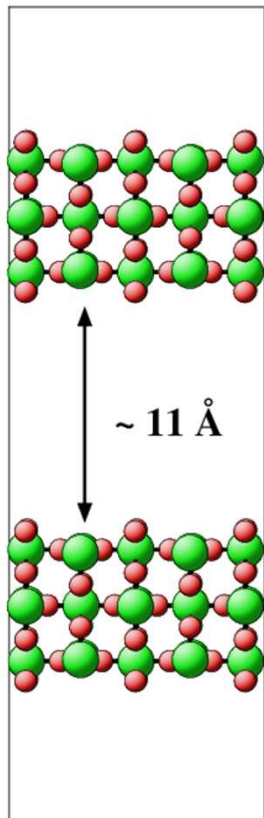
Multiscale modeling



Ab initio atomistic thermodynamics and statistical mechanics of surface properties and functions
K. Reuter, C. Stampfl, and M. Scheffler, in: *Handbook of Materials Modeling Vol. 1*,
(Ed.) S. Yip, Springer (Berlin, 2005). <http://www.fhi-berlin.mpg.de/th/paper.html>

**I. „Bottom up best practice“:
Multiscale modeling approach to
in-situ CO oxidation at RuO₂(110)**

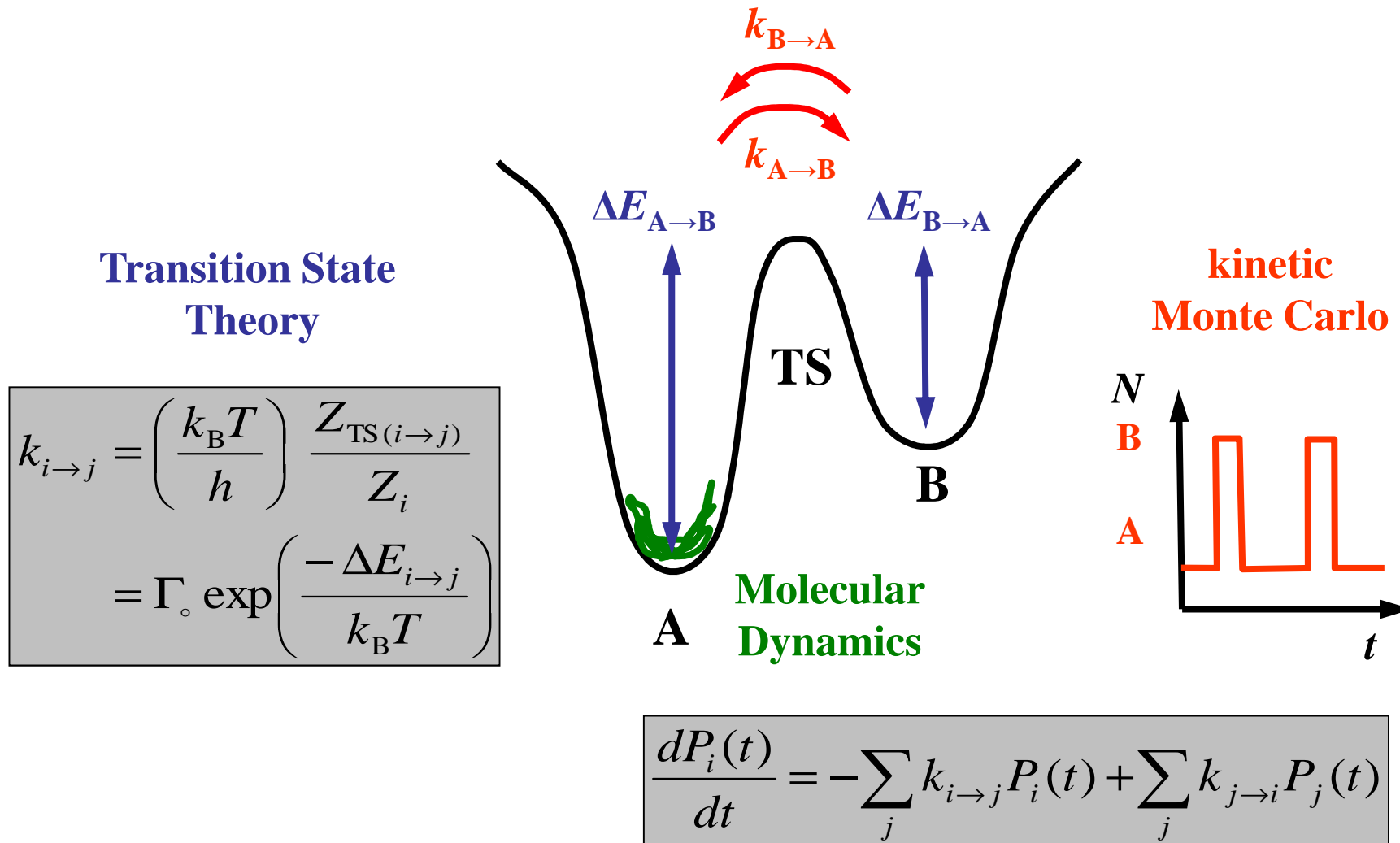
Electronic regime: Energetics of elementary processes



Density-Functional Theory

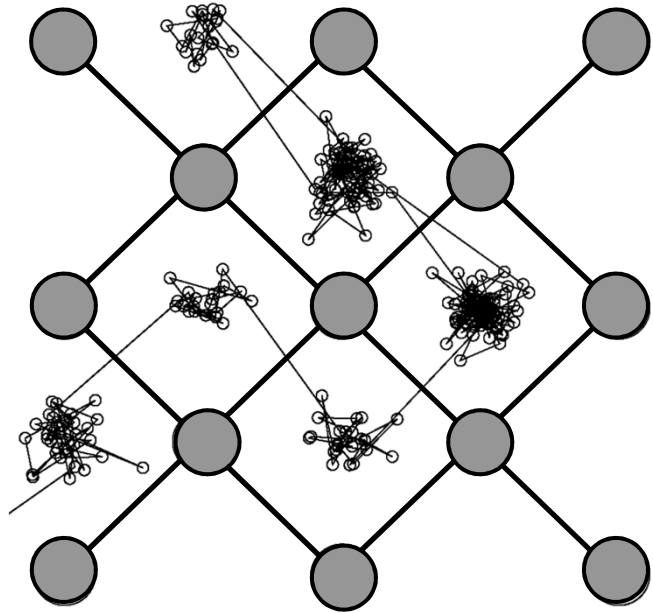
$V_{\text{xc}} = \text{GGA (PBE...)}$

Mesososcopic regime: Tackling rare-event time scales



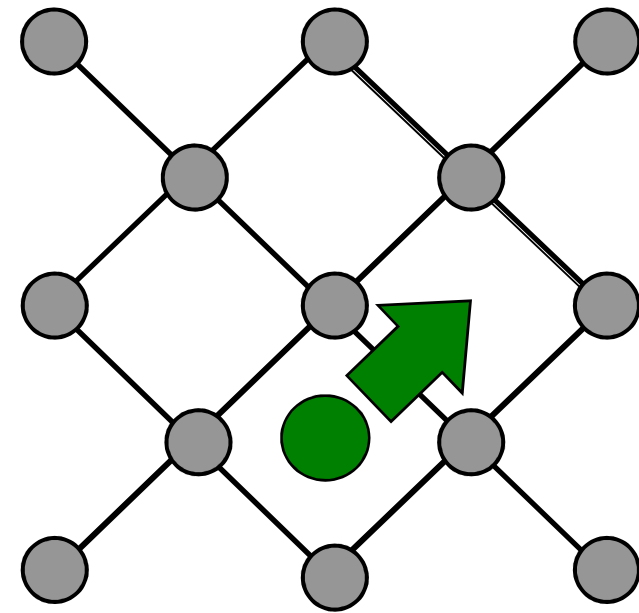
First-principles kinetic Monte Carlo simulations for heterogeneous catalysis: Concepts, status and frontiers
 K. Reuter, in “Modeling Heterogeneous Catalytic Reactions: From the Molecular Process to the Technical System”,
 (Ed.) O. Deutschmann, Wiley-VCH, Weinheim (2011). <http://www.fhi-berlin.mpg.de/th/paper.html>

Kinetic Monte Carlo: essentially „coarse-grained MD“



**Molecular Dynamics:
the whole trajectory**

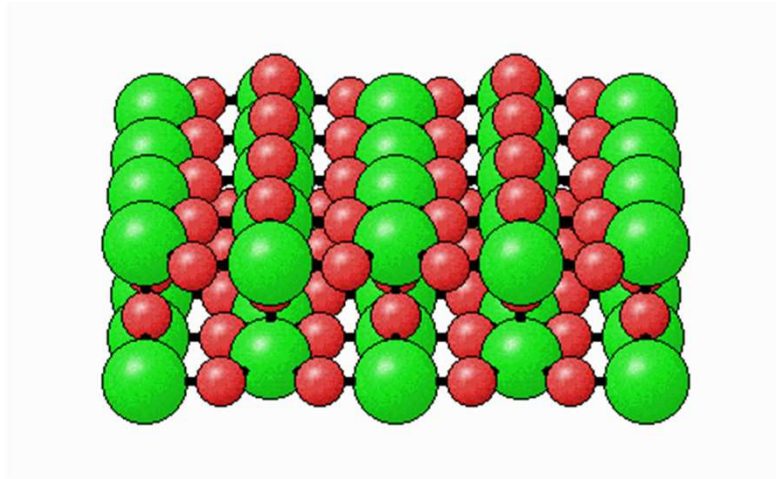
***ab initio* MD:
up to 50 ps**



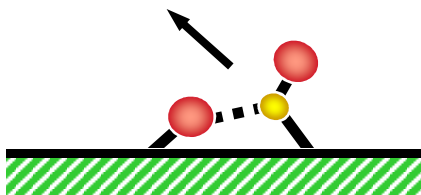
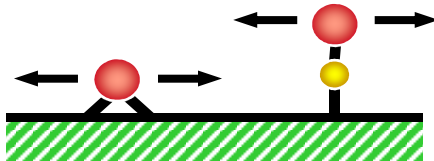
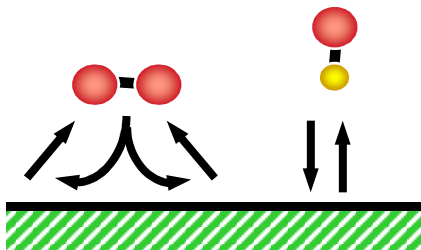
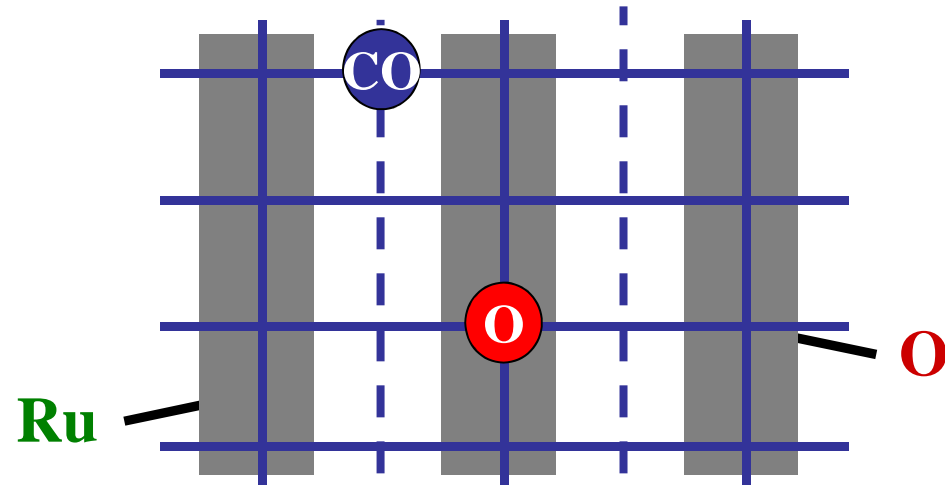
**Kinetic Monte Carlo:
coarse-grained hops**

***ab initio* kMC:
up to minutes**

Building a first-principles kinetic Monte Carlo model



CO oxidation @ RuO₂(110)



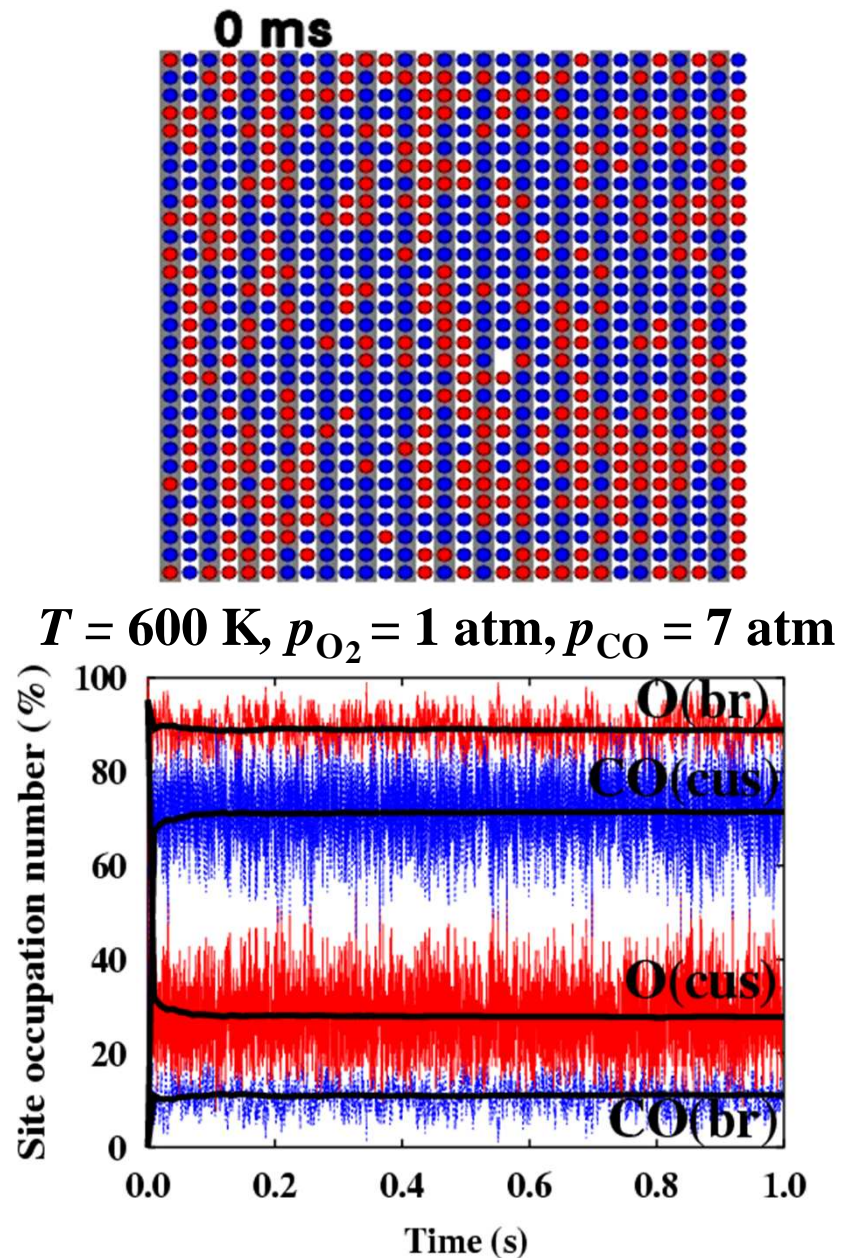
26 elementary processes (site-specific):

- O₂ adsorption/desorption (dissociative/associative)
- CO adsorption/desorption (unimolecular)
- O and CO diffusion
- CO + O reaction

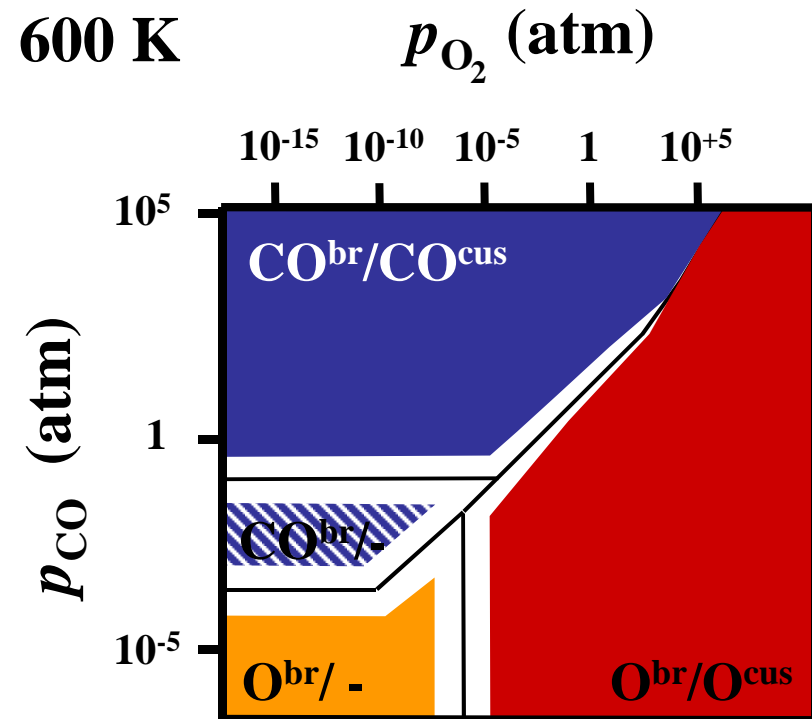
K. Reuter, Oil&Gas Sci. Technol. 61, 471 (2006)

K. Reuter and M. Scheffler, Phys. Rev. B 73, 045433 (2006)

Surface structure and composition in the reactive environment

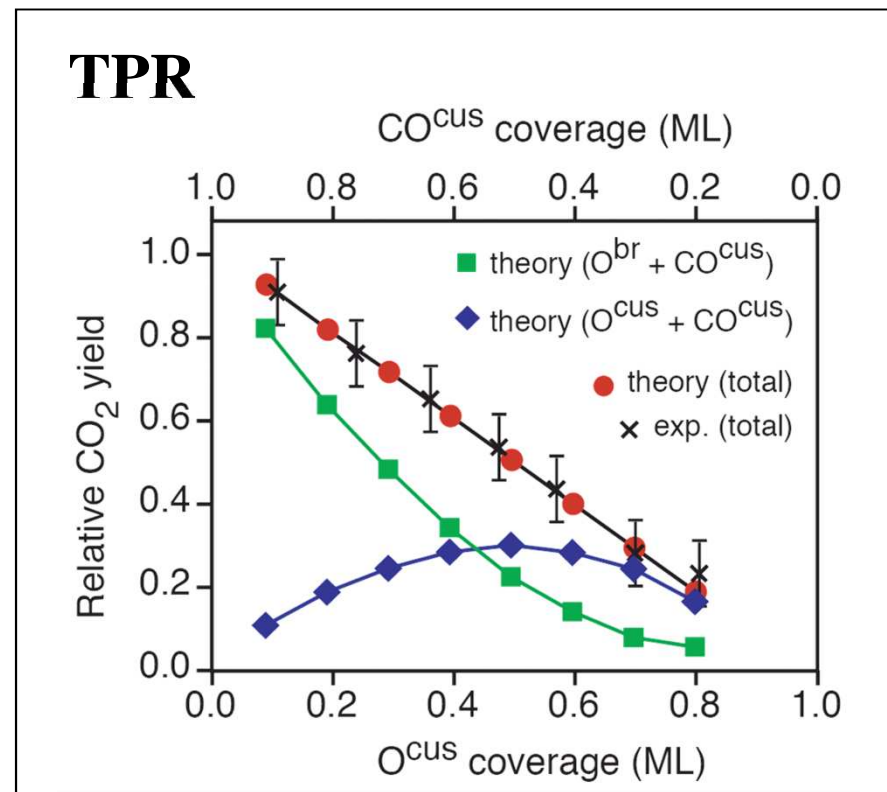
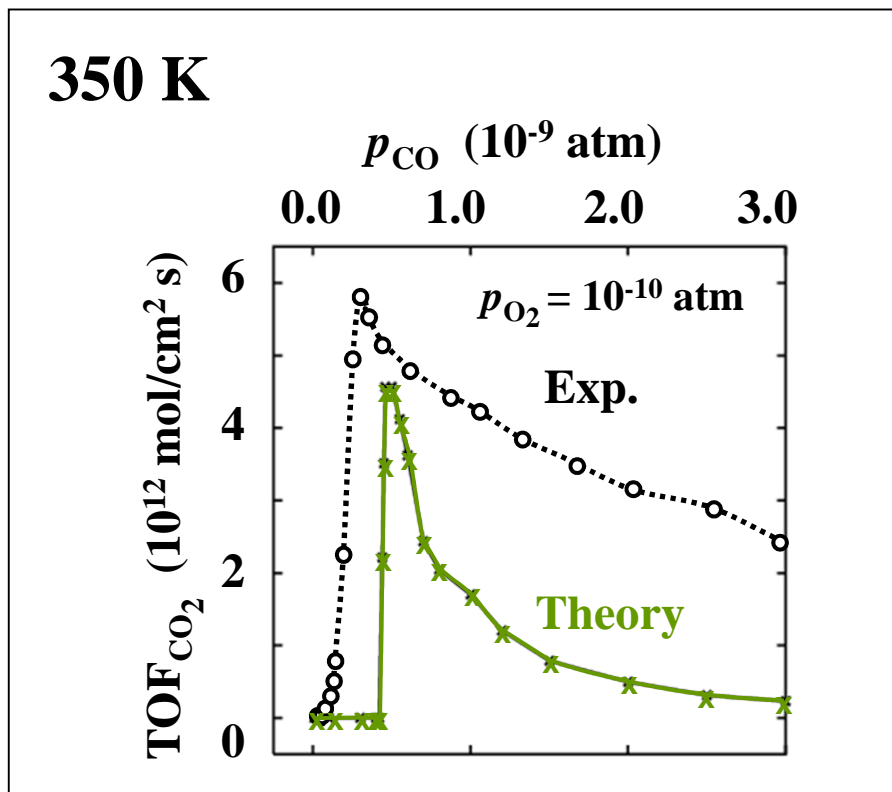


CO oxidation at $\text{RuO}_2(110)$



K. Reuter, D. Frenkel and M. Scheffler,
Phys. Rev. Lett. 93, 116105 (2004)

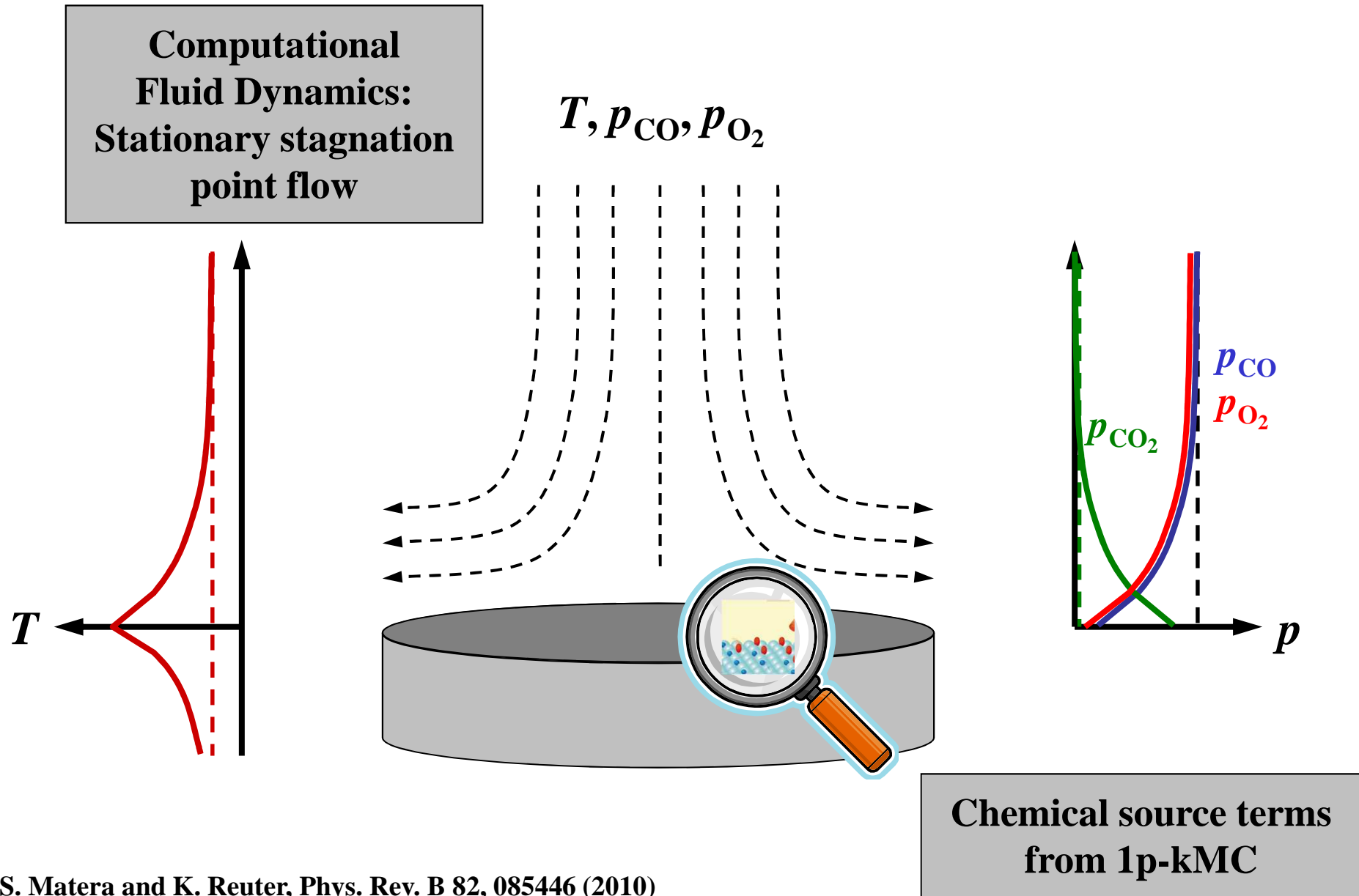
Steady-state and transient parameter-free turnover frequencies



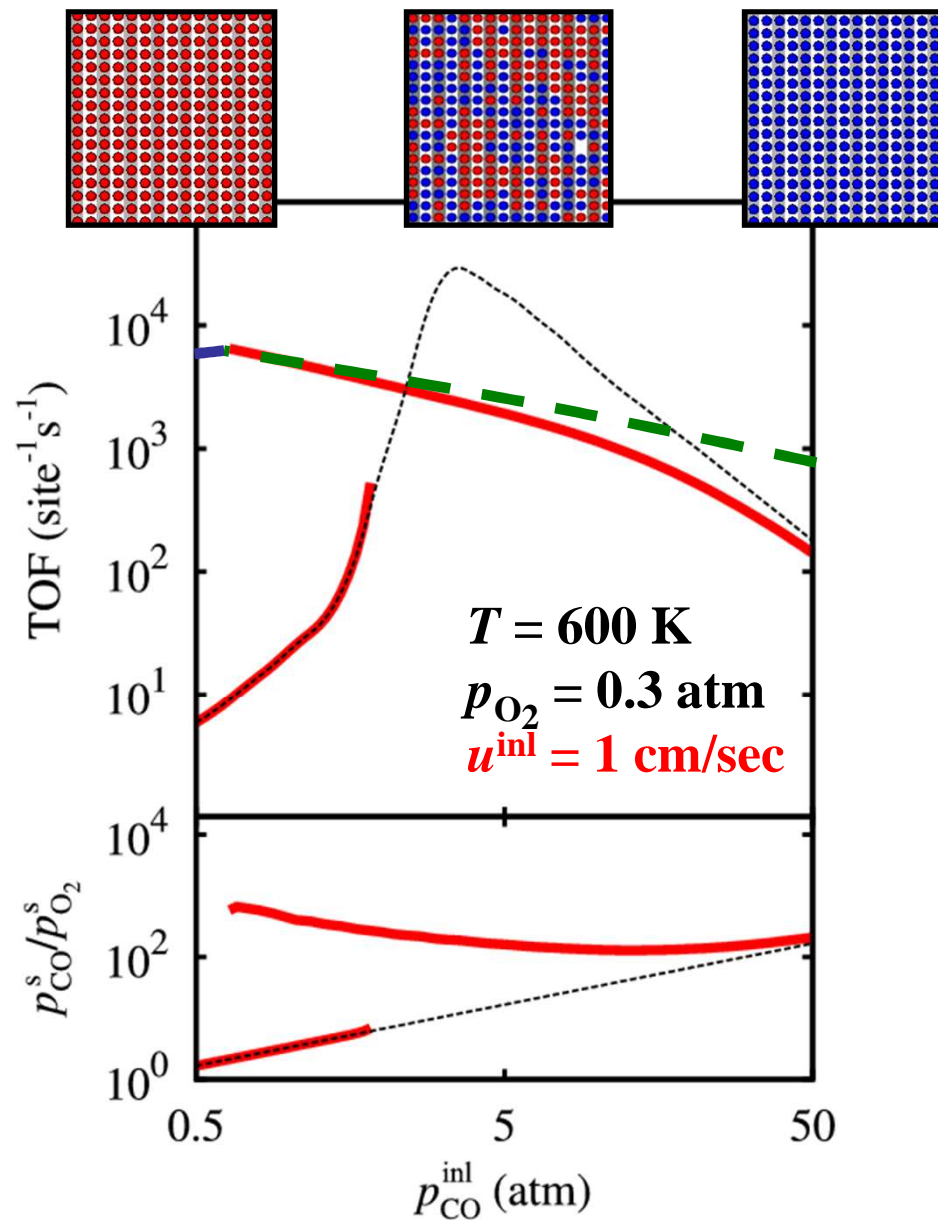
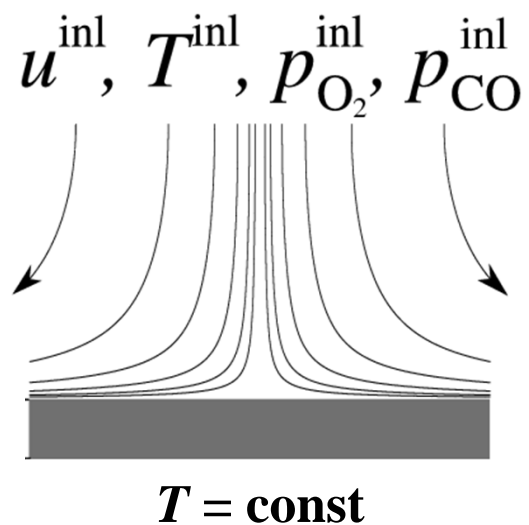
K. Reuter and M. Scheffler,
Phys. Rev. B 73, 045433 (2006)

M. Rieger, J. Rogal, and K. Reuter,
Phys. Rev. Lett. 100, 016105 (2008)

Macroscopic regime: Heat and mass transfer



Isothermal limit: Mass transfer limitations



II. Towards error-controlled first-principles microkinetic models

Key ingredients to „predictive-quality“ microkinetic modeling

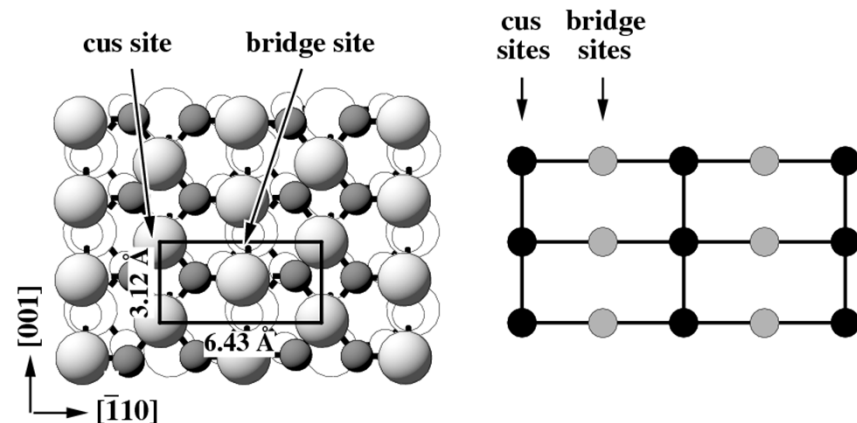
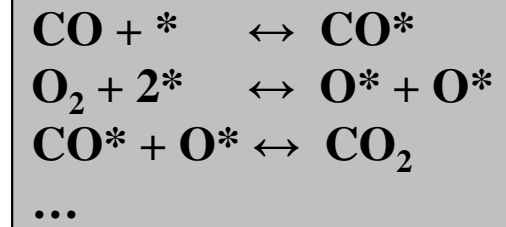
Accurate rate constants:

$$k_{i \rightarrow j} = \Gamma_0 \exp\left(\frac{-\Delta E_{i \rightarrow j}}{k_B T}\right)$$

Transition state theory and beyond
DFT functionals: „self-interaction“
van der Waals interactions

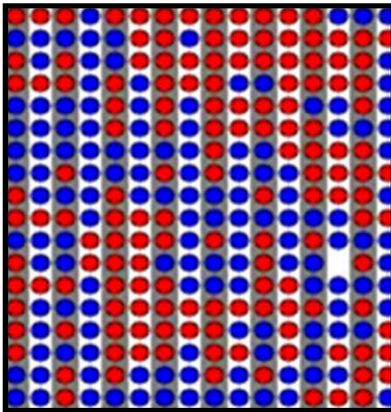
Reaction mechanism:

Process identification
Lattice mapping / spatial distributions
„Hot chemistry“ beyond Markov



Mean-field approximation: Phenomenological rate equations

$$\frac{dP_i(t)}{dt} = - \sum_j k_{i \rightarrow j} P_i(t) + \sum_j k_{j \rightarrow i} P_j(t)$$



$$\begin{aligned} &\theta(\text{O}^{\text{cus}}) \\ &\theta(\text{O}^{\text{br}}) \\ &\theta(\text{CO}^{\text{cus}}) \\ &\theta(\text{CO}^{\text{br}}) \end{aligned}$$

$$P(\text{O}^{\text{br}}, \text{CO}^{\text{cus}}, t)$$

↓

$$\theta(\text{O}^{\text{br}}, t) \cdot \theta(\text{CO}^{\text{cus}}, t)$$

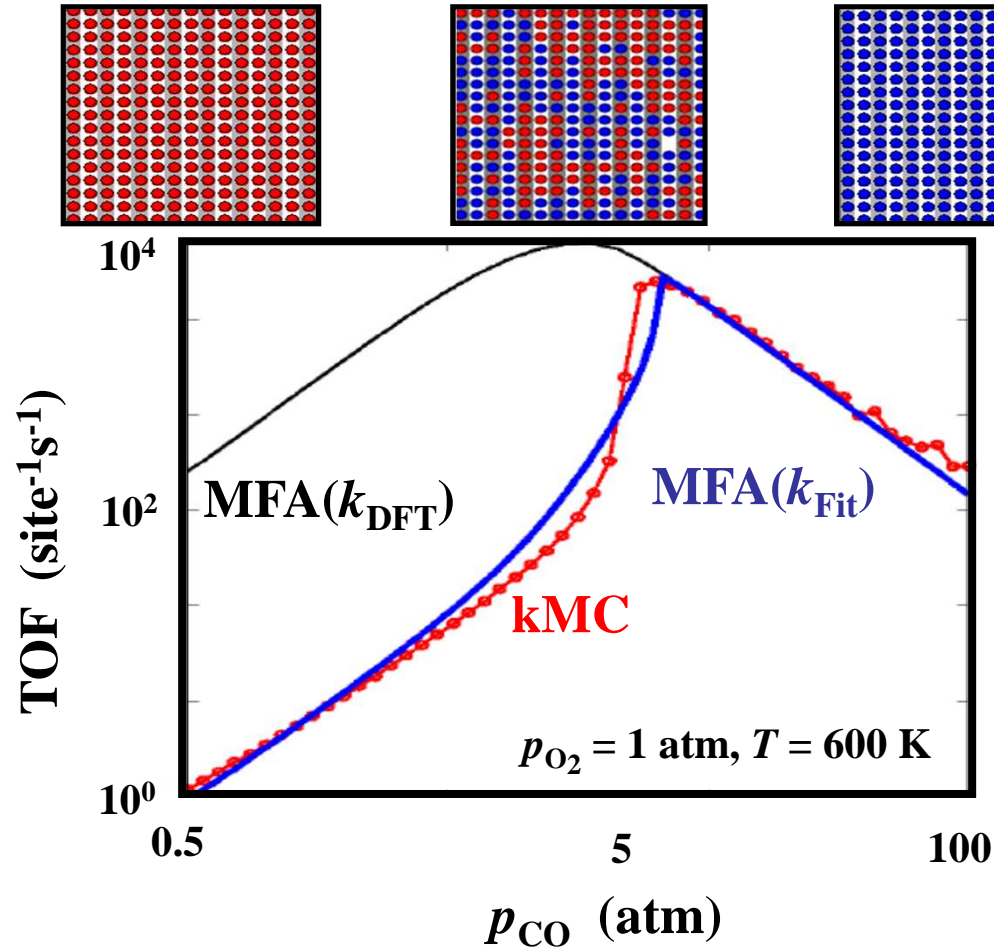
$$\frac{d\theta(\text{O}^{\text{cus}}, t)}{dt} = f_1 \left\{ k_{i \rightarrow j}, \theta(\text{O}^{\text{cus}}, t), \theta(\text{O}^{\text{br}}, t), \theta(\text{CO}^{\text{cus}}, t), \theta(\text{CO}^{\text{br}}, t) \right\}$$

$$\frac{d\theta(\text{O}^{\text{br}}, t)}{dt} = f_2 \left\{ k_{i \rightarrow j}, \theta(\text{O}^{\text{cus}}, t), \theta(\text{O}^{\text{br}}, t), \theta(\text{CO}^{\text{cus}}, t), \theta(\text{CO}^{\text{br}}, t) \right\}$$

...

The „power“ of fitting

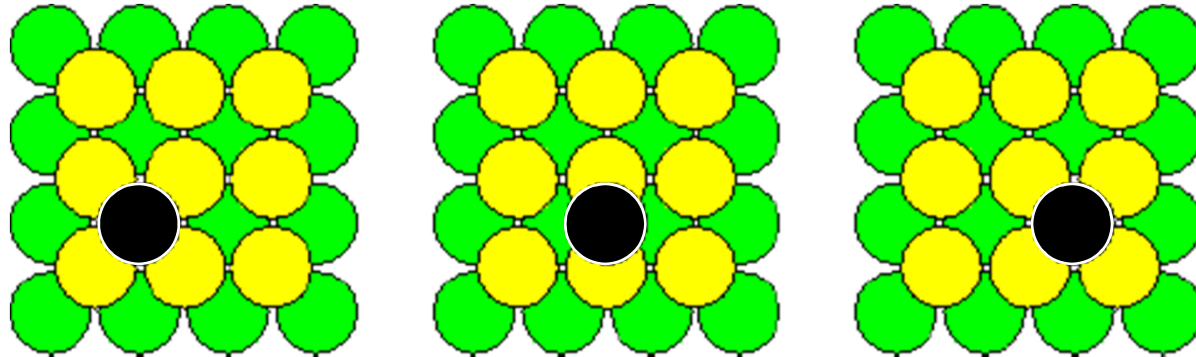
CO oxidation
at RuO₂(110)



Fitted rate constants deviate from “real” rate constants
by up to two orders in magnitude for dominant processes

Effective parameters without microscopic meaning

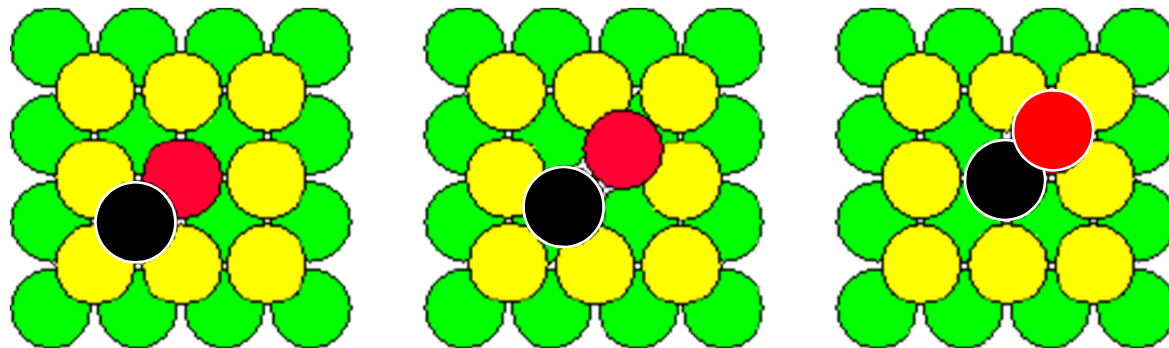
Diffusion at metal surfaces: surprises...



Hopping mechanism

Ag(100) $\Delta E = 0.45$ eV

Au(100) $\Delta E = 0.83$ eV



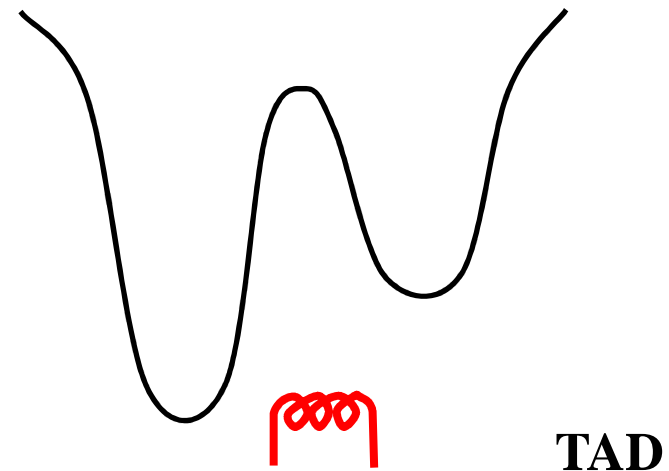
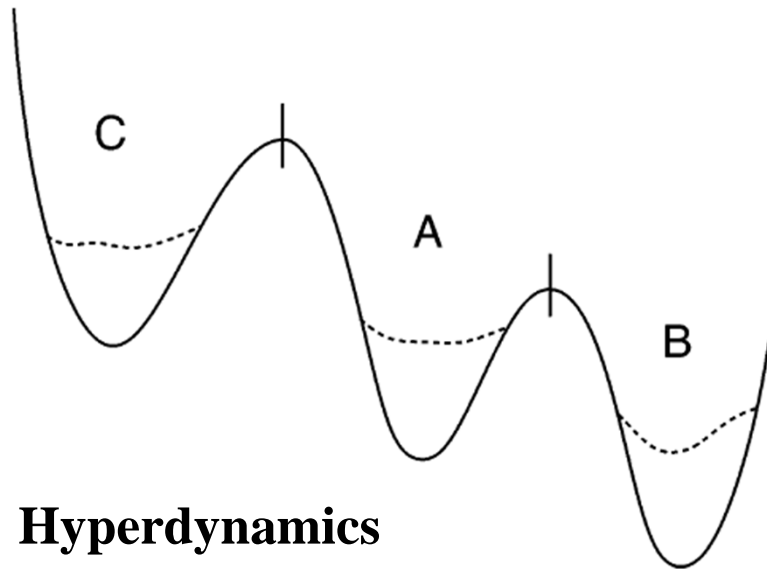
Exchange mechanism

Ag(100) $\Delta E = 0.73$ eV

Au(100) $\Delta E = 0.65$ eV

Automatized process identification

Accelerated molecular dynamics:



Other approaches:

- metadynamics

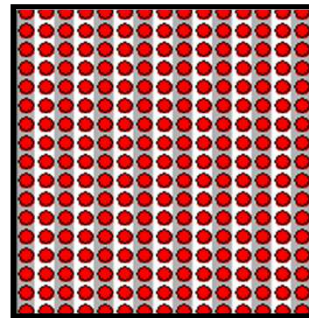
- dimer method

...

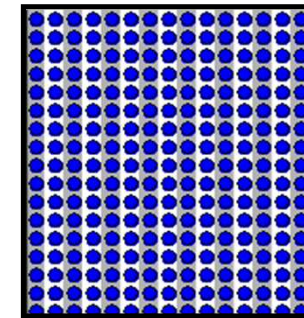
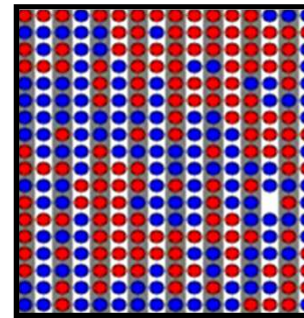
Extending the Time Scale in Atomistic Simulation of Materials,
A.F. Voter, F. Montalenti and T.C. Germann,
Annu. Rev. Mater. Res. 32, 321 (2002)

Error propagation through rate-determining steps

CO oxidation
at RuO₂(110)



O-poisoned

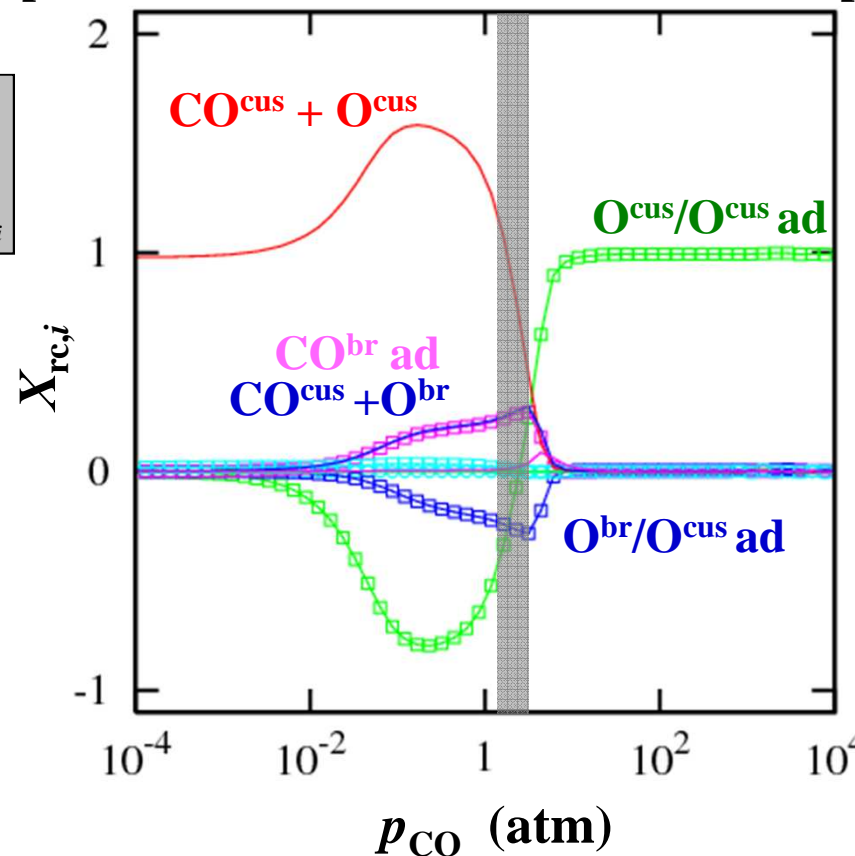


CO-poisoned

Sensitivity analysis:

$$X_{rc,i} = \left(\frac{k_i}{\text{TOF}} \right) \left(\frac{\partial \text{TOF}}{\partial k_i} \right)_{k_j, K_i}$$

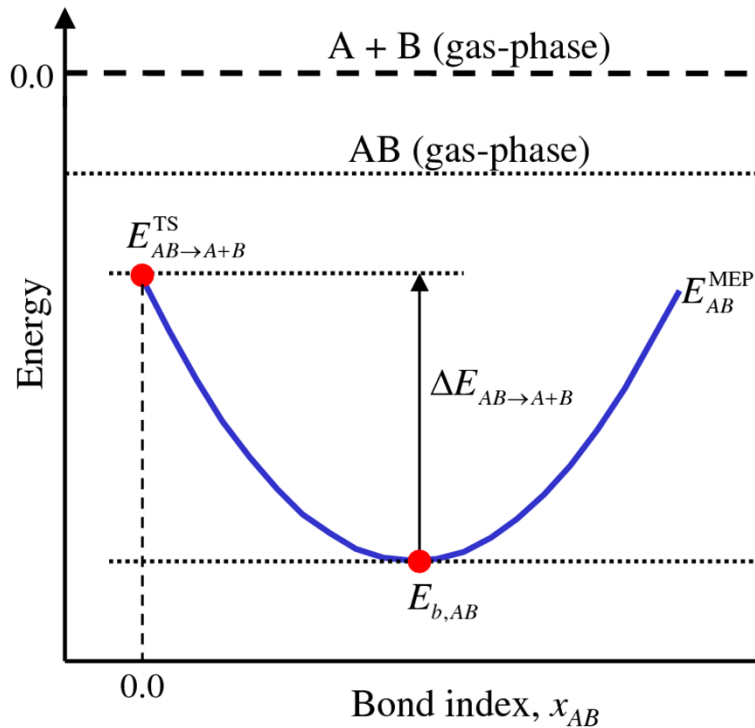
C.T. Campbell,
J. Catal. 204, 520 (2001);
Nature 432, 282 (2004)



$p_{\text{O}_2} = 1 \text{ atm}$
 $T = 600 \text{ K}$

H. Meskine *et al.*,
Ertl Special Issue
Surf. Sci. 603, 1724 (2009)

Source for „rough“ rate constants: Hybrid UBI-QEP ?!

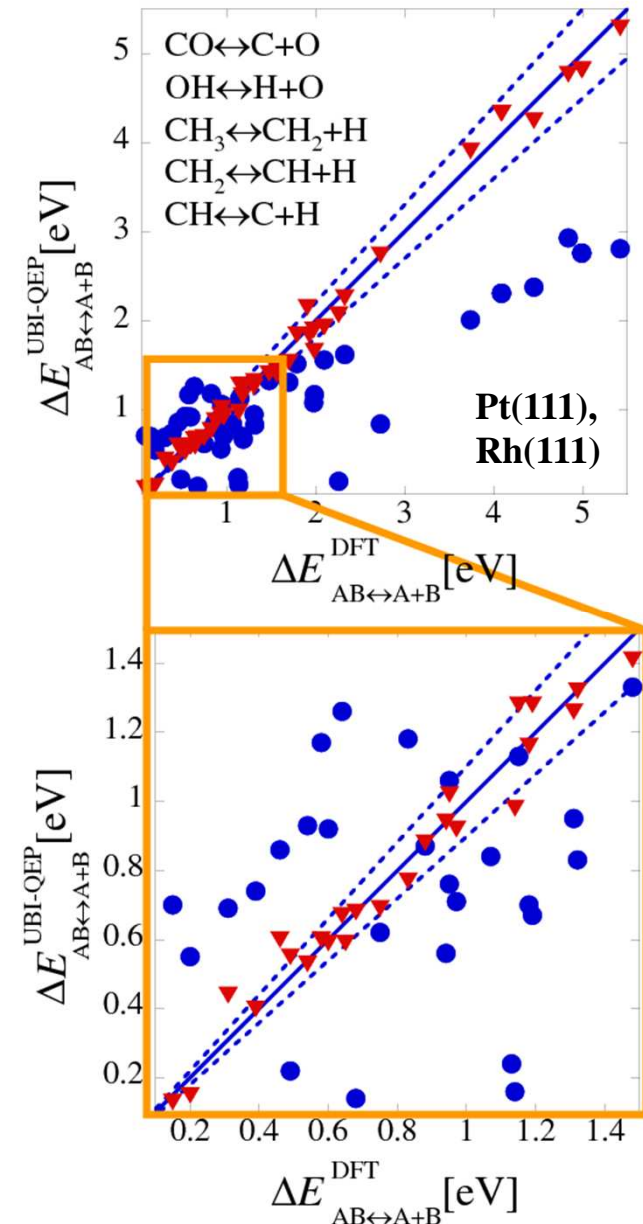


Unity Bond-Index Quadratic Exponential Potential

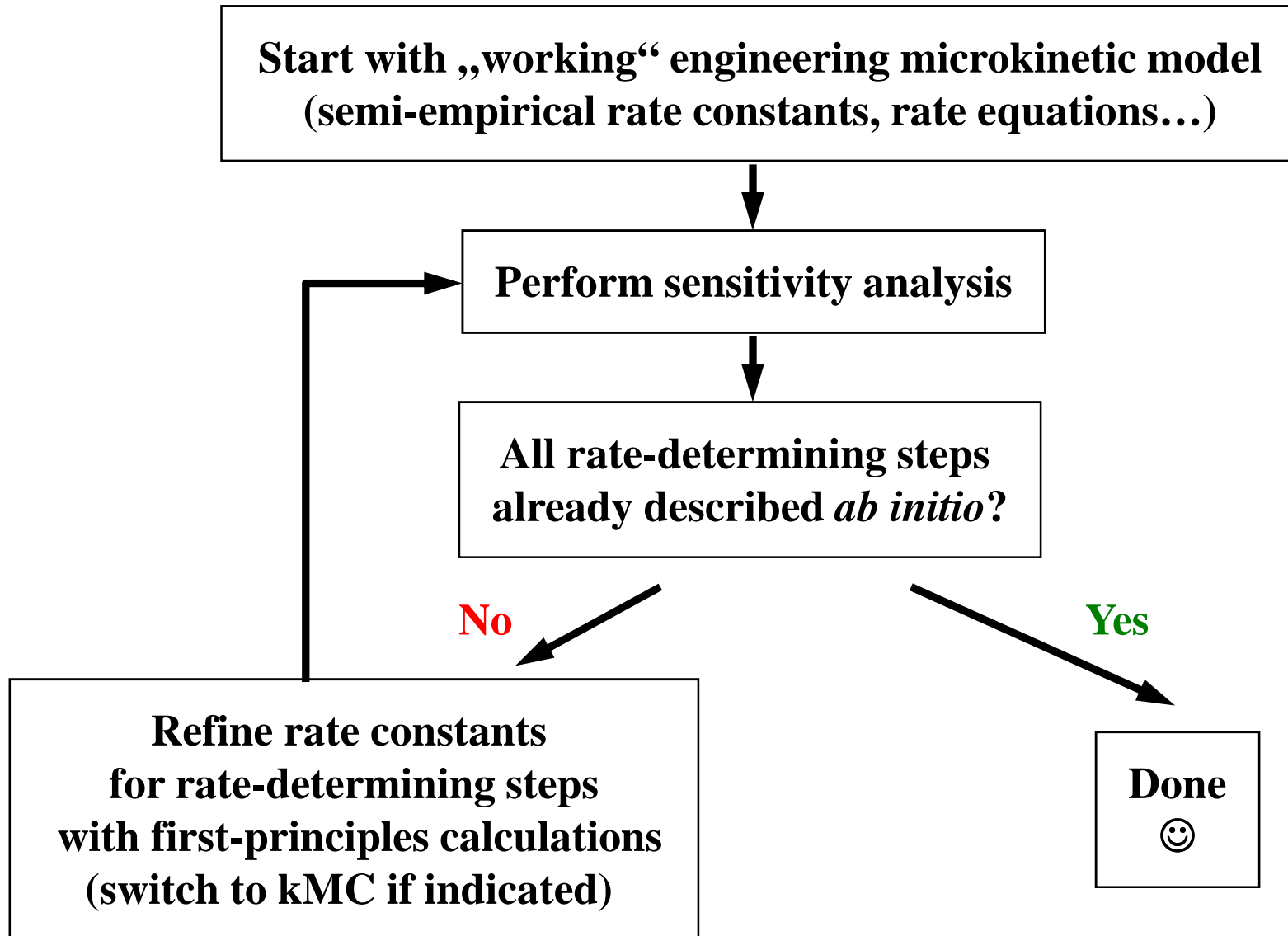
$$\Delta E_{AB \rightarrow A+B}^{UBI-QEP} = \phi \left[E_{AB \rightarrow A+B}^{TS} - \min_{x_{AB}} (E_{AB}^{MEP}) \right] = \phi \left[\frac{(P - D_{AB})^2}{(P + D_{AB})} \right]$$

E. Shustorovich and H. Sellers, Surf. Sci. Rep. 31, 5 (1998)

M. Maestri and K. Reuter, Angew. Chemie 123, 1226 (2011)



Tackling complexity: Bottom-up meets top-down



C1 microkinetic model for methane conversion to syngas on Rh/Al₂O₃

No.	Reaction	A (unitless or s ⁻¹)	beta	Bond index	Activation Energy [kcal/mol]
1	H ₂ + 2* → 2H*	7.73E-01	0.9387	0.50	0.0
2	2H* → H ₂ + 2*	5.56E+11	-0.4347	0.50	20.5+f(T)
3	O ₂ + 2* → 2O*	4.81E-02	1.9965	0.50	0.0
4	2O* → O ₂ + 2*	4.31E+12	1.1995	0.50	81.0 - 52.0θ _O +f(T)
5	OH* + * → H* + O*	5.20E+12	-0.2659	0.30	24.2 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)
6	H* + O* → OH* + *	4.69E+12	-0.8196	0.30	14.2 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)
7	H ₂ O* + * → H* + OH*	5.74E+11	0.0281	0.55	24.6 + f(θ _O , θ _{OH} , θ _H , θ _{CO} , θ _{H₂O} , T)
8	H* + OH* → H ₂ O* + *	1.80E+09	1.2972	0.55	26.8 + f(θ _O , θ _{OH} , θ _H , θ _{CO} , θ _{H₂O} , T)
9	H ₂ O* + O* → 2OH*	2.08E+13	-2.1130	0.30	11.4 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
10	2OH* → H ₂ O* + O*	7.22E+10	-0.2902	0.30	23.6 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
11	OH + * → OH*	2.66E-01	-0.2891	0.50	0.0
12	OH* → OH + *	1.14E+13	-0.9500	0.50	70.0 - 33.0θ _O - 25.0θ _{H₂O} +f(T)
13	H ₂ O + * → H ₂ O*	7.72E-02	1.4067	0.50	0.0
14	H ₂ O* → H ₂ O + *	2.06E+13	-1.8613	0.50	10.8 - 25.0θ _{OH} - 4.5θ _{H₂O} +f(T)
15	H + * → H*	1.93E-01	1.5313	0.50	0.0
16	H* → H + *	2.40E+12	1.3208	0.50	62.3 - 2.5θ _H - 3.7θ _{CO} +f(T)
17	O + * → O*	4.46E-02	-1.9236	0.50	0.0
18	O* → O + *	9.74E+12	-1.9701	0.50	100.0 - 26.0θ _O +f(T)
19	CO + * → CO*	5.00E-01	-2.0000	0.50	0.0
20	CO* → CO + *	5.65E+12	1.9879	0.50	38.5 - 3.7θ _H - 15.0θ _{CO} +f(T)
21	CO ₂ + * → CO ₂ *	3.67E-01	-2.3294	0.50	0.0
22	CO ₂ * → CO ₂ + *	7.54E+10	2.1831	0.50	5.2 +f(T)
23	CO ₂ * + * → CO* + O*	4.12E+09	1.9698	0.90	19.5 + f(θ _O , θ _H , θ _{CO} , T)
24	CO* + O* → CO ₂ * + *	3.27E+09	1.3560	0.90	25.6 + f(θ _O , θ _H , θ _{CO} , T)
25	COOH + * → COOH*	5.34E-01	-1.0767	0.50	0.0
26	COOH* → COOH + *	1.12E+11	1.6803	0.50	62.2+f(T)
27	HCOO + 2* → HCOO**	1.89E-02	-0.5548	0.50	0.0
28	HCOO** → HCOO + 2*	3.74E+13	0.5548	0.50	69.2+f(T)
29	CO ₂ * + H* → CO* + OH*	1.60E+13	0.0301	0.70	6.1 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)
30	CO* + OH* → CO ₂ * + H*	1.40E+13	-0.0301	0.70	22.2 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)

**H₂
oxidation**

**CO
oxidation**

**coupling
H₂ & CO**

C1 microkinetic model for methane conversion to syngas on Rh/Al₂O₃

No.	Reaction	A (unitless or s ⁻¹)	beta	Bond index	Activation Energy [kcal/mol]
31	COOH** → CO*+OH*	1.07E+12	-0.4123	0.50	6.2 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)
32	CO*+OH* → COOH**	9.37E+11	0.4123	0.50	18.6 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)
33	COOH** → CO ₂ *+H*	1.00E+10	-0.4424	0.80	6.8 + f(θ _H , θ _{CO} , T)
34	CO ₂ *+H* → COOH**	9.99E+09	0.4424	0.80	3.1 + f(θ _H , θ _{CO} , T)
35	CO* + H ₂ O* → COOH* + H*	3.34E+11	-0.2222	0.80	33.1 + f(θ _{OH} , θ _H , θ _{CO} , θ _{H₂O} , T)
36	COOH* + H* → CO* + H ₂ O*	1.20E+09	0.2223	0.80	22.9 + f(θ _{OH} , θ _H , θ _{CO} , θ _{H₂O} , T)
37	CO ₂ * + OH* → COOH* + O*	1.05E+11	0.7192	0.50	22.3 + f(θ _O , θ _{H₂O} , T)
38	COOH* + O* → CO ₂ * + OH*	9.51E+10	-0.7192	0.50	16.0 + f(θ _O , θ _{H₂O} , T)
39	CO ₂ * + H ₂ O* → COOH* + OH*	1.78E+12	-0.1922	0.50	13.5 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
40	COOH* + OH* → CO ₂ * + H ₂ O*	5.60E+09	0.1922	0.50	19.4 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
41	CO ₂ *+H* → HCOO**	1.04E+09	1.1254	0.50	4.3 + f(θ _H , θ _{CO} , T)
42	HCOO** → CO ₂ *+H*	3.86E+13	-1.1253	0.50	0.0 + f(θ _H , θ _{CO} , T)
43	CO ₂ * + OH* + * → HCOO** + O*	1.09E+09	1.4022	0.50	27.6 + f(θ _O , θ _{H₂O} , T)
44	HCOO** + O* → CO ₂ * + OH* + *	3.67E+13	-1.4022	0.50	13.4 + f(θ _O , θ _{H₂O} , T)
45	CO ₂ * + H ₂ O* + * → HCOO** + OH*	9.24E+09	0.4908	0.50	18.4 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
46	HCOO** + OH* → CO ₂ * + H ₂ O* + *	1.08E+12	-0.4908	0.50	16.4 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
47	C* → C + *	3.54E+04	1.8618	0.50	159.0 + f(T)
48	C* → C + *	3.54E+04	1.8618	0.50	159.0 + f(T)
49	CH + * → CH*	2.29E-02	-1.0798	0.50	0.0
50	CH* → CH + *	3.08E+13	1.0798	0.50	151.2 + f(T)
51	CH ₂ + * → CH ₂ *	4.09E-02	-0.4265	0.50	0.0
52	CH ₂ * → CH ₂ + *	1.73E+13	0.4265	0.50	109.3 + f(T)

coupling H₂ & CO

CH₄
pyro-
lisis

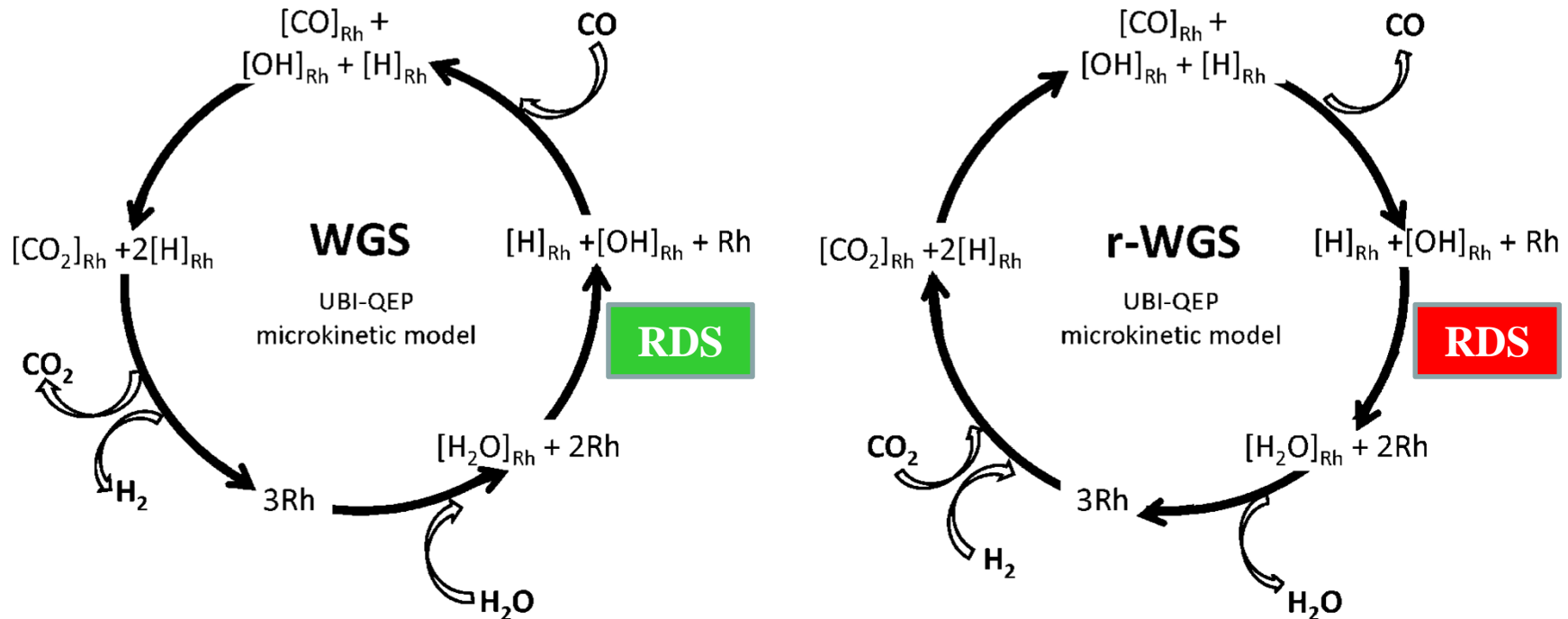
C1 microkinetic model for methane conversion to syngas on Rh/Al₂O₃

No.	Reaction	A (unitless or s ⁻¹)	beta	Bond index	Activation Energy [kcal/mol]
53	CH ₃ * → CH ₃ *	1.35E-01	0.0326	0.50	0.0
54	CH ₃ * → CH ₃ * + *	5.22E+12	-0.0325	0.50	42.4 + f(T)
55	CH ₄ + 2* → CH ₃ * + H*	5.72E-01	0.7883	0.50	9.7 + f(θ _H , θ _{CO} , T)
56	CH ₃ * + H* → CH ₄ + 2*	7.72E+10	-0.7883	0.50	9.5 + f(θ _H , θ _{CO} , T)
57	CH ₃ * + * → CH ₂ * + H*	2.49E+10	0.0862	0.50	10.6 + f(θ _H , θ _{CO} , T)
58	CH ₂ * + H* → CH ₃ * + *	2.57E+09	-0.0862	0.50	29.1 + f(θ _H , θ _{CO} , T)
59	CH ₂ * + * → CH* + H*	5.50E+10	-0.1312	0.50	20.5 + f(θ _H , θ _{CO} , T)
60	CH* + H* → CH ₂ * + *	7.27E+09	0.1312	0.50	23.6 + f(θ _H , θ _{CO} , T)
61	CH* + * → C* + H*	4.58E+12	-0.2464	0.50	27.6 + f(θ _H , θ _{CO} , T)
62	C* + H* → CH* + *	2.18E+11	0.2464	0.50	17.1 + f(θ _H , θ _{CO} , T)
63	CH ₃ * + O* → CH ₂ * + OH*	2.96E+11	-0.1906	0.70	10.0 + f(θ _O , θ _{H₂O} , T)
64	CH ₂ * + OH* → CH ₃ * + O*	3.38E+10	0.1906	0.70	38.4 + f(θ _O , θ _{H₂O} , T)
65	CH* + OH* → CH ₂ * + O*	3.83E+10	0.4081	0.70	45.7 + f(θ _O , θ _{H₂O} , T)
66	CH ₂ * + O* → CH* + OH*	2.61E+11	-0.4081	0.70	32.6 + f(θ _O , θ _{H₂O} , T)
67	C* + OH* → CH* + O*	2.30E+10	0.5232	0.50	29.8 + f(θ _O , θ _{H₂O} , T)
68	CH* + O* → C* + OH*	4.35E+11	-0.5232	0.50	30.4 + f(θ _O , θ _{H₂O} , T)
69	CH ₂ * + H ₂ O* → CH ₃ * + OH*	5.73E+10	-0.7208	0.70	29.9 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
70	CH ₃ * + OH* → CH ₂ * + H ₂ O*	1.74E+09	0.7208	0.70	13.6 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
71	CH* + H ₂ O* → CH ₂ * + OH*	6.49E+11	-0.5033	0.70	21.8 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
72	CH ₂ * + OH* → CH* + H ₂ O*	1.54E+10	0.5033	0.70	20.9 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
73	C* + H ₂ O* → CH* + OH*	9.74E+11	-0.3882	0.50	10.5 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
74	CH* + OH* → C* + H ₂ O*	6.41E+10	0.3882	0.50	23.3 + f(θ _O , θ _{OH} , θ _{H₂O} , T)
75	CO* + * → C* + O*	1.25E+09	0.5712	0.50	49.1 + f(θ _O , θ _H , θ _{CO} , T)
76	C* + O* → CO* + *	7.22E+09	-0.5712	0.50	12.3 + f(θ _O , θ _H , θ _{CO} , T)
77	CO* + H* → CH* + O*	9.07E+09	0.8176	0.80	69.1 + f(θ _O , θ _H , θ _{CO} , T)
78	CH* + O* → CO* + H*	1.10E+12	-0.8176	0.80	42.9 + f(θ _O , θ _H , θ _{CO} , T)
79	CO* + H* → C* + OH*	1.18E+12	0.2944	0.15	26.8 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)
80	C* + OH* → CO* + H*	7.60E+12	-0.2944	0.15	0.0 + f(θ _O , θ _H , θ _{CO} , θ _{H₂O} , T)
81	2CO* → C* + CO ₂ *	1.11E+09	0.2644	0.50	42.9 + f(θ _H , θ _{CO} , T)
82	C* + CO ₂ * → 2CO*	8.10E+09	-0.2644	0.50	0.0 + f(θ _H , θ _{CO} , T)

CH₄ pyrolysis

CH₄ oxidation

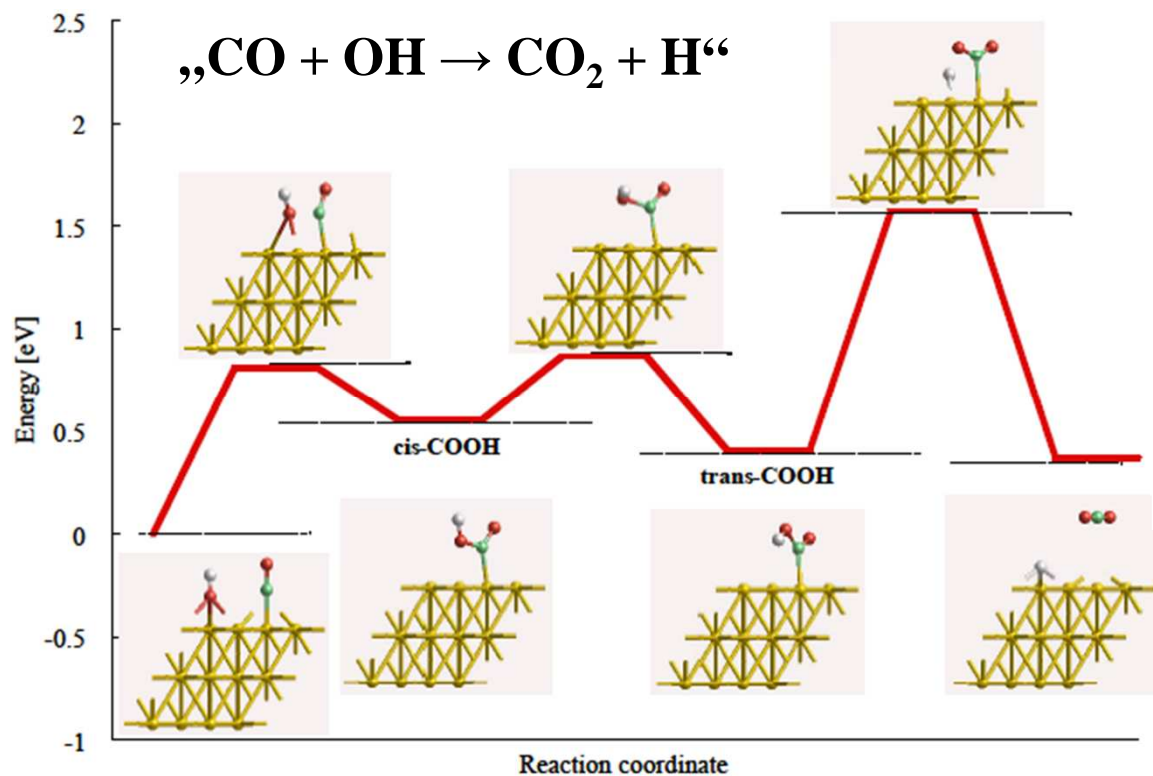
Identified key issues: Water-gas shift and r-WGS



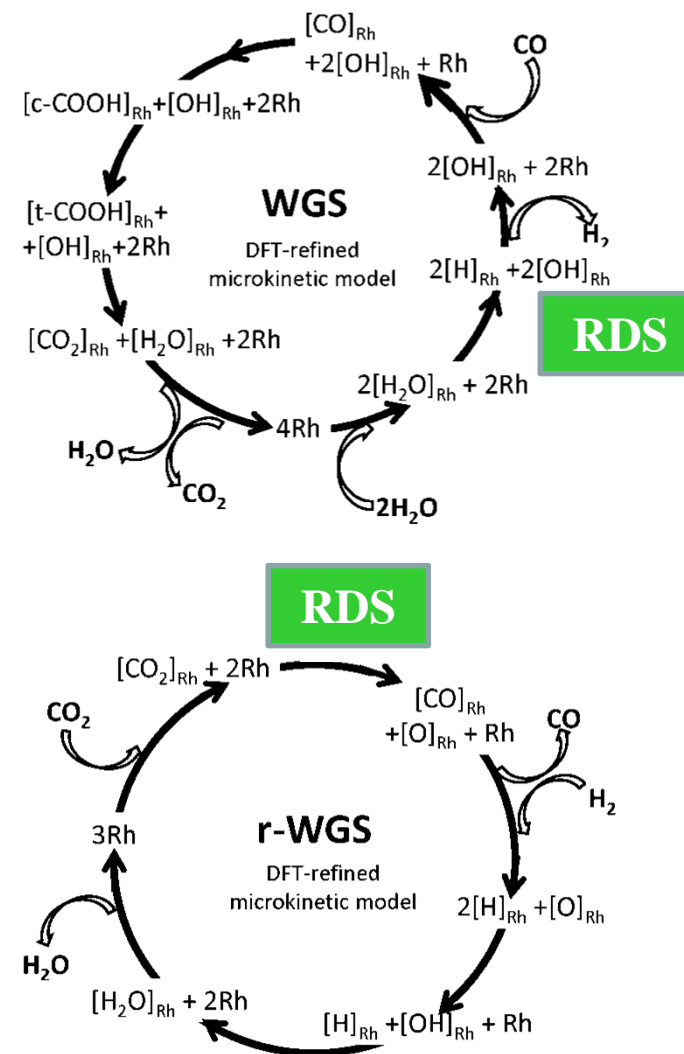
**CO_2/CO ratio not well captured by the model,
pointing at an incorrect description of WGS pathways**

Same RDS for WGS/r-WGS inconsistent with experimental data

First-principles refinement: When an „elementary step“ is not elementary...



WGS proceeds through carboxyl mechanism
New RDS consistent with all experimental data



Multiscale catalysis modeling: From hype to reality

State-of-the-art in catalysis modeling:

- **Prevalence of highly coarse-grained models based on effective parameters without true microscopic meaning**

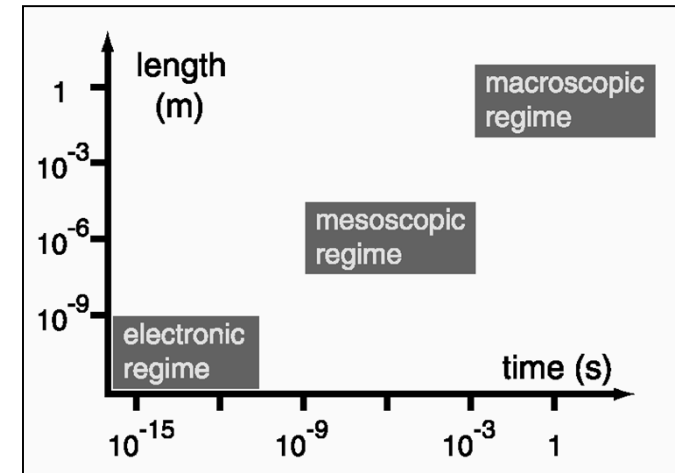
rate equation theory

based on empirical rate constants

- **Emergence of *ad-hoc* dual-scale modeling**

first-principles kinetic Monte Carlo

simulations for heterogeneous catalysis



Steps towards a predictive character multiscale catalysis modeling:

- **Replace effective parameters by first-principles data**

fitted vs. DFT-based rate constants

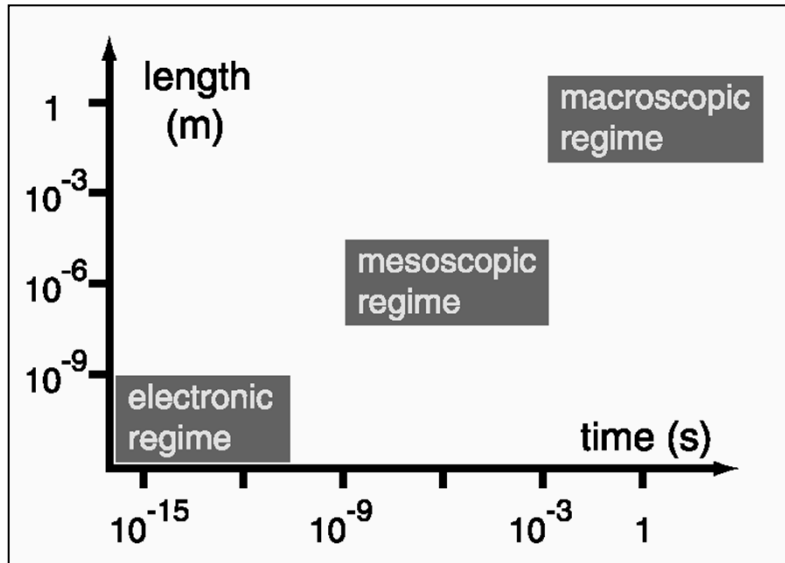
- **Refined modeling at each individual level**

necessity to resolve spatial arrangement at surface

integrate first-principles surface chemistry into reactor models

- **Robust links between theories that enable reverse-mapping**

sensitivity analysis to control flow of error across scales



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