

# **(Spin) bulk band structure calculations with SFHIngX**

**Session D3**

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**Workshop on application of Density-Functional Theory in Condensed-Matter  
Physics, Surface Physics, Chemistry, Engineering, and Biology**

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**Fritz-Haber-Institut der Max-Planck-Gesellschaft,  
Berlin, Germany**

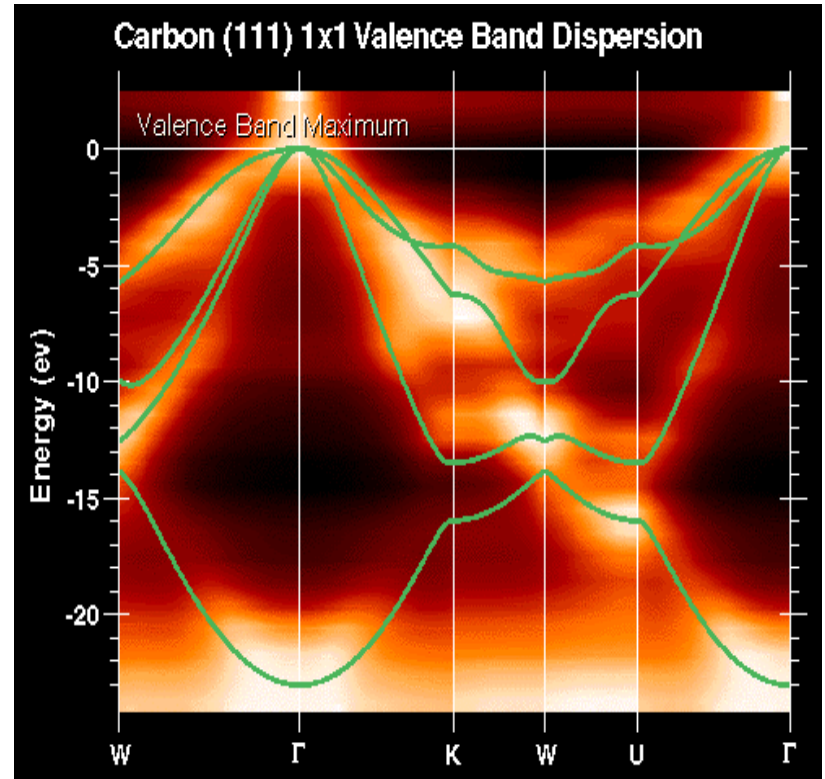
## Talk / session flow

### *List of tasks:*

- Recall how to setup SCF run
- Learn how to setup band structure calculations
- Learn how to analyze band structure output
  
- Magnetic systems
- How to setup initial magnetic structures
- Band structure for magnetic system

# Why should one care about band structure?

- **Understanding of physics at nanoscale**
- **Deep understanding of material properties → engineering of new materials, feasibility of its application in industry (optical / electronic / magnetic / spintronic / catalytic devices)**
- **Direct comparison with experiment →**



**Comparison between angle-resolved photoelectron spectroscopy and theoretically predicted band structure \***

# How to obtain band structure?

1 •

Have full description of the system = know Hamiltonian operator  
In frame of Kohn-Sham theory means to get converged ground-state charge density

SCF charge density  
SCF wave-functions

2 •

Diagonalize Hamiltonian employing specified k-point set →  
One-particle eigenspectrum (band structure)

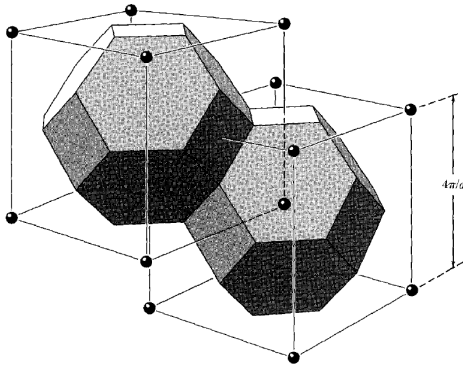
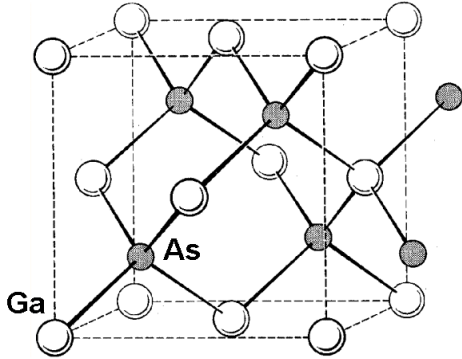
3 •

Density of allowed states in given energy interval (TDOS)

4 •

Atom resolved contributions to density of allowed states in given energy interval (PDOS)

# 1 • How to get full description of the system?



GaAs crystal structure  
and corresponding  
(fcc) Brillouin zones

**structure** { ... }     $\beta$  Can be checked with pxviewer

```
basis {  
  eCut = 10; // Ry  
  kPoint { coords = [1/2, 1/2, 1/2]; weight = 1; relative; }  
  folding = [4, 4, 4];  
}
```

**Converged**

**Hamiltonian** { ... }

**initialGuess** { ... }

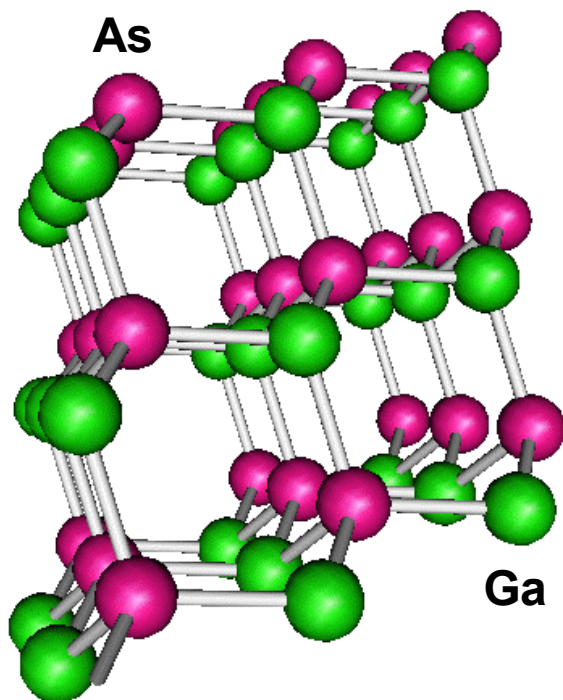
**main** {

```
  DIIS_CCG {  
    ...  
    dEnergy = 1e-04; // Hartree  
  }  
}
```

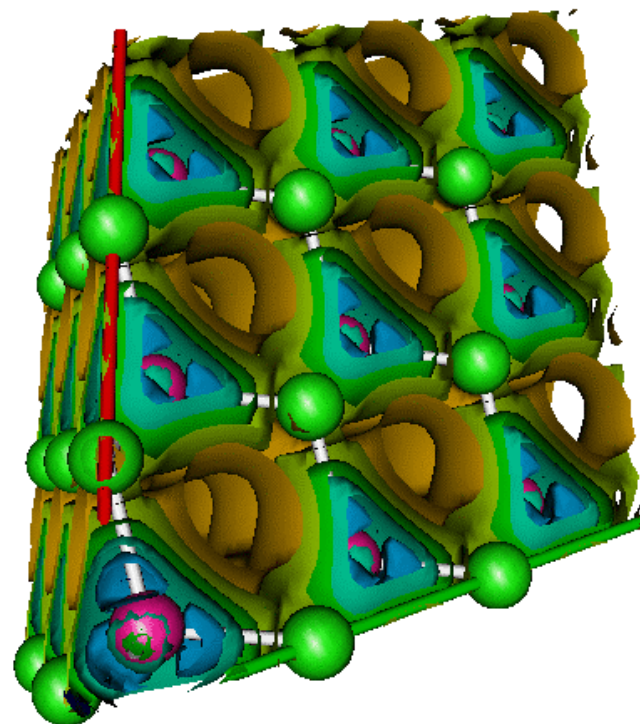
**Updates charge density**

Schematic structure of input.sx (SCF)

# What one gets after SCF calculation?



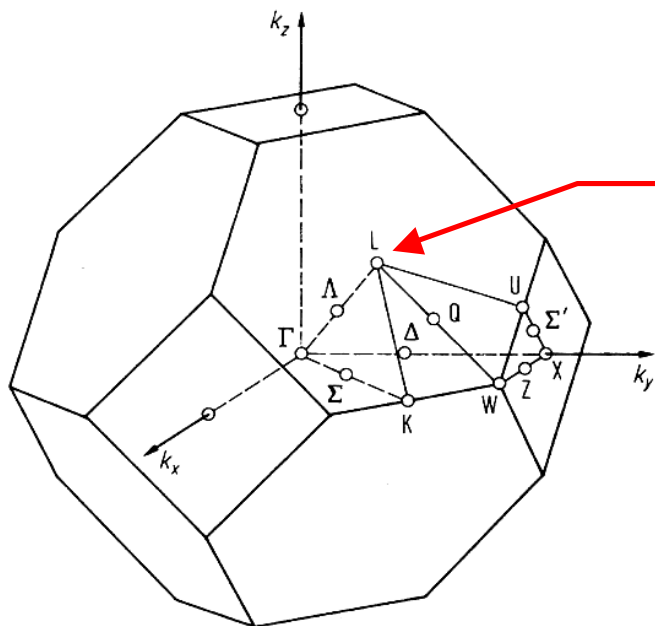
GaAs atomic structure



GaAs SCF charge density

**Self-consistent (SCF) converged charge density**  
**Set of SCF wave-functions**  
**Fermi energy and occupations**

# How to diagonalize SCF Hamiltonian?



GaAs crystal structure  
and corresponding  
(fcc) Brillouin zone

```
structure { ... }  $\beta$  Can be checked with pviewer
```

```
basis {
```

```
  eCut = 10; // Ry  $\beta$  Must be as in SCF
```

```
  kPoints {
```

```
    from { coords = L; label = "L";}
```

Any set

```
    to { coords = G; label = "Gamma"; nPoints = 9; }
```

```
    ...
```

```
    to { coords = G; label = "Gamma"; nPoints = 11; }
```

```
  }
```

```
}
```

```
Hamiltonian { ... }
```

```
initialGuess { rho = "scf-rho.sxb"; ... } Read-in SCF
```

```
main {
```

```
  DIIS_CCG { Keep SCF charge density
```

```
  ...
```

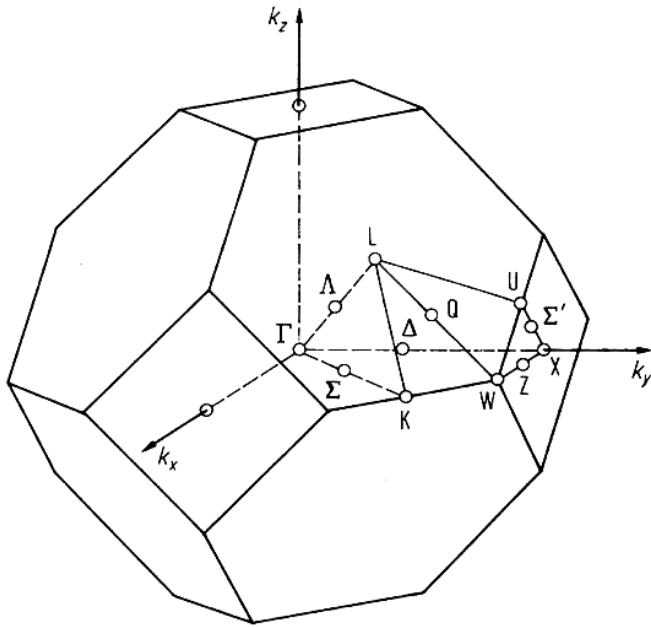
```
  keepRhoFixed;  $\beta$  VERY IMPORTANT
```

```
  dEnergy = 1e-04; // Hartree
```

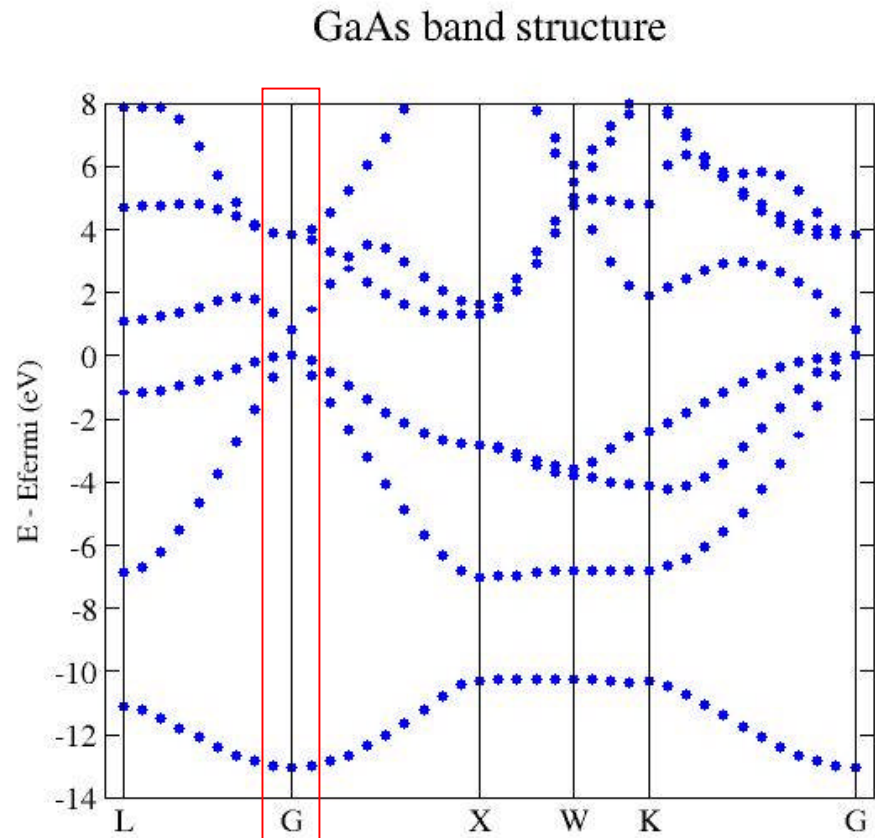
```
}
```

```
}
```

# What we get after band structure calculation?



GaAs crystal structure  
and corresponding  
(fcc) first Brillouin zone



What we have discovered:

- Semiconductor
- Direct band gap
- Band gap width 0.90 eV

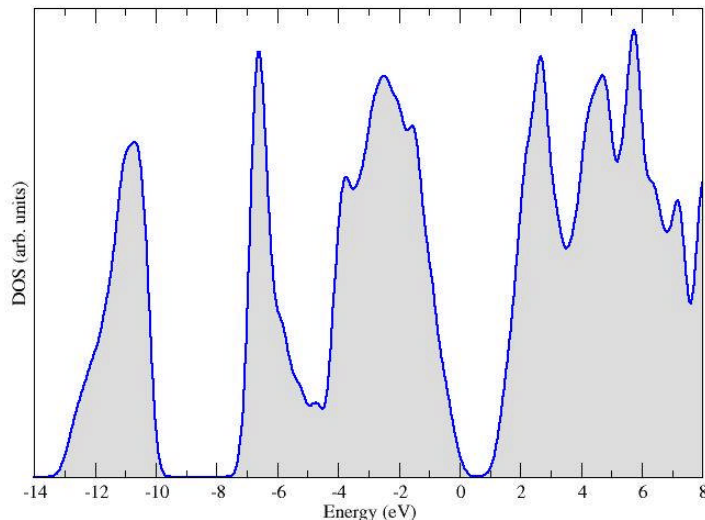


### 3 • Can one do more?

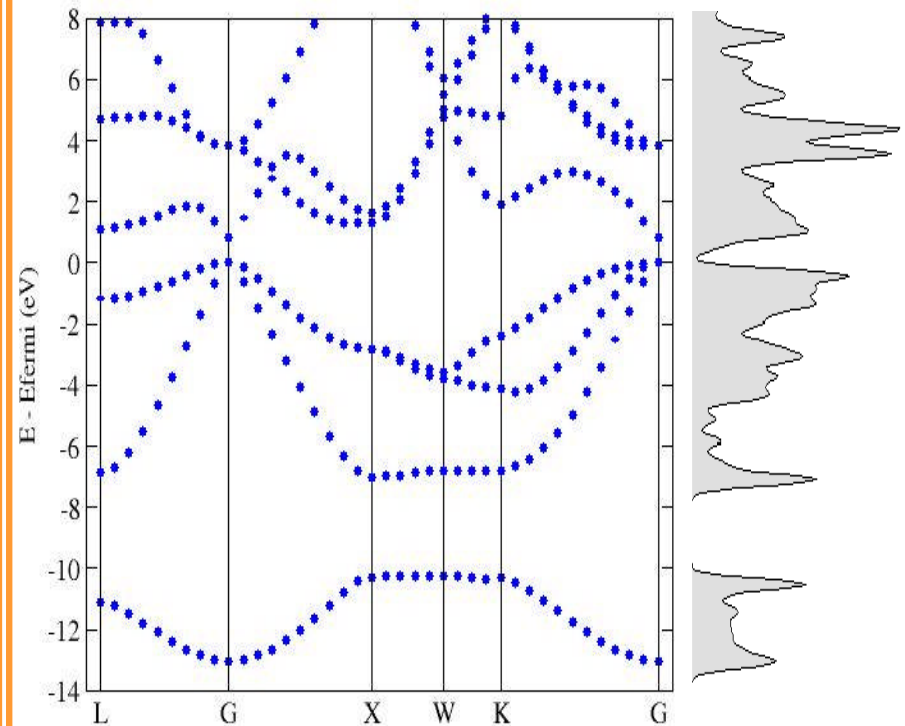
Total density of states (TDOS)  
→ number of available states  
at given energy

$$TDOS(e) = \sum_{i,k} w_k G(e - e_{ik})$$

GaAs total density of states



GaAs band structure



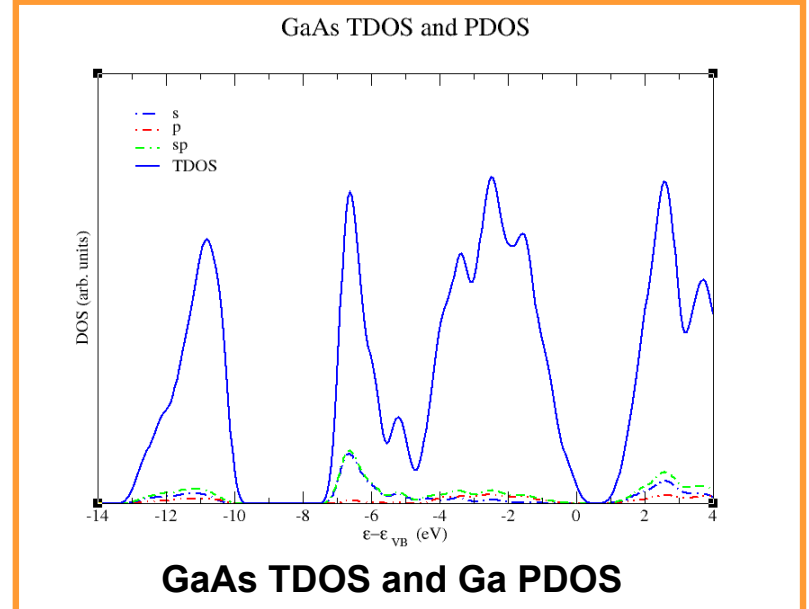
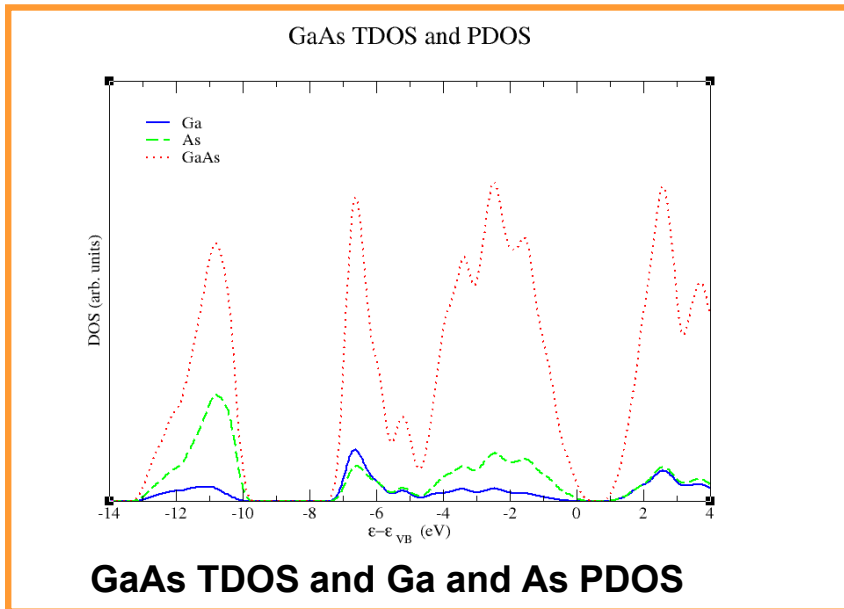
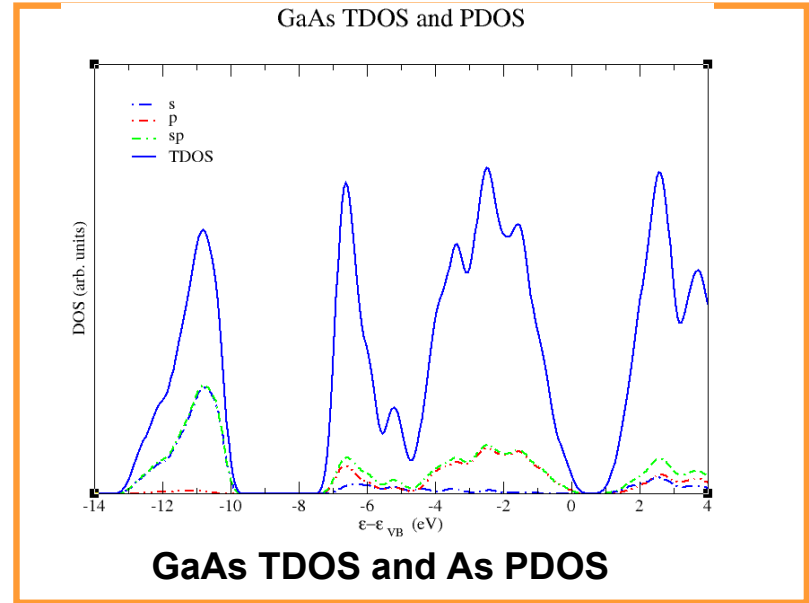
Band structure of GaAs at equilibrium

Attention – broadening is artificial → convergence tests needed

# (3 • + 4 •) Can we learn more?

Projected density of states (PDOS)  
 → overlap of localized atomic orbitals with SCF wavefunction at given energy

$$PDOS_{iOrb}(e) = \sum_{i,k} w_k G(e - e_{ik}) \left| \langle m_{iOrb} | R | y_{ik} \rangle \right|^2$$



## Task on one's own

With the same machinery as applied to GaAs perform careful analysis of aluminum face-centered cubic structure, that is at thermodynamical equilibrium:

- Analyze atomic structure
- Obtain SCF charge density
- Visualize structure and SCF charge density
- Get aluminum band structure → answer question whether fcc-Al is metal or not?
- Calculate converged TDOS

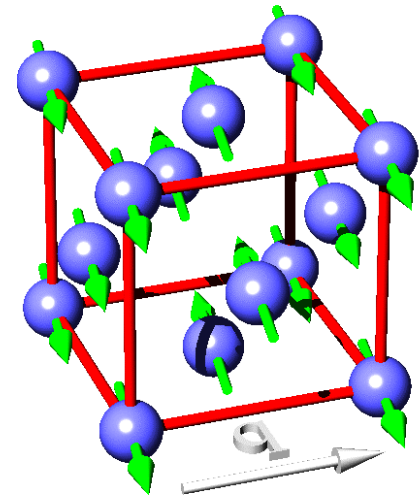
# Magnetism in SFHIngX

## Current treatment of the magnetism in SFHIngX

- no spin-orbit coupling included
- only collinear magnetic structures can be treated → have only two spin channels – spin up and spin down

## Questions to learn:

- Magnetic structure initialization
- Fixed magnetization calculations
- Spin-density visualization
- Magnetic electronic structure analysis



# Magnetic structure initialization

How to switch spin on →

```
Hamiltonian {  
  ...  
  spinPolarized;  $\beta$   
}
```

Initial magnetic structure initialized with LCAO

Total magnetization  
of the cell (all atoms  
are spin polarized)

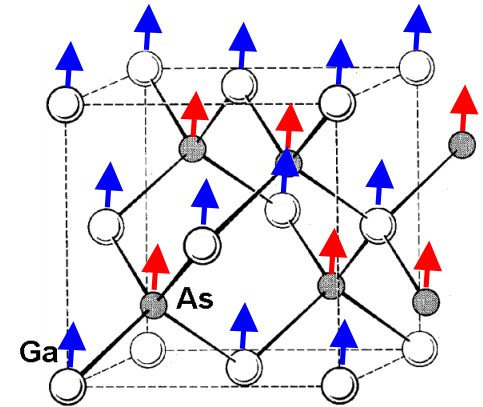
Explicit occupation  
numbers for LCAO  
charge density

Mixed initialization  
(only part of atoms  
is spin-polarized)

# Magnetic structure initialization

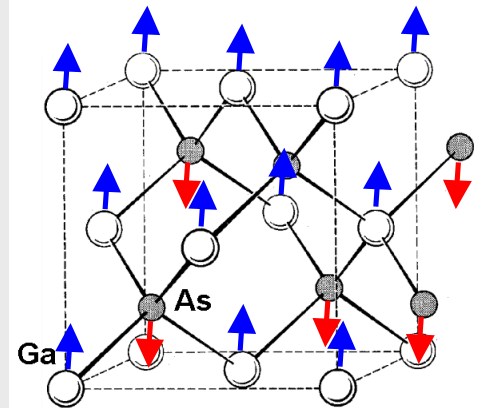
Total magnetization of the cell (all atoms are spin polarized)

```
initialGuess {  
  ...  
  rho { atomicOrbitals; spinMoment = 1; }  $\beta$   
}
```



Explicit occupation numbers for LCAO charge density

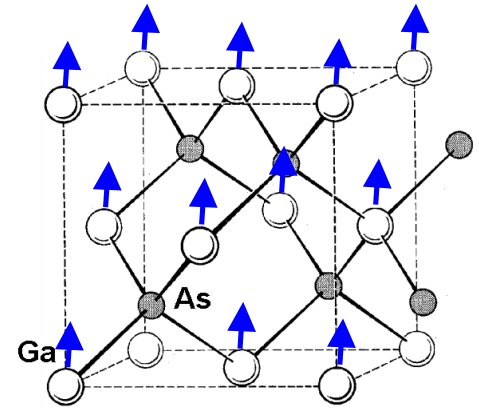
```
species {  
  ...  
  lcaoOrbitals = [s,p,d];  
  atomicRhoOcc = [[1,2,0],[1,1,0]];  $\beta$  ( $\uparrow s^1 p^2 d^0, \downarrow s^1 p^1 d^0$ )  
  ...  
}
```



# Magnetic structure initialization

## Mixed initialization

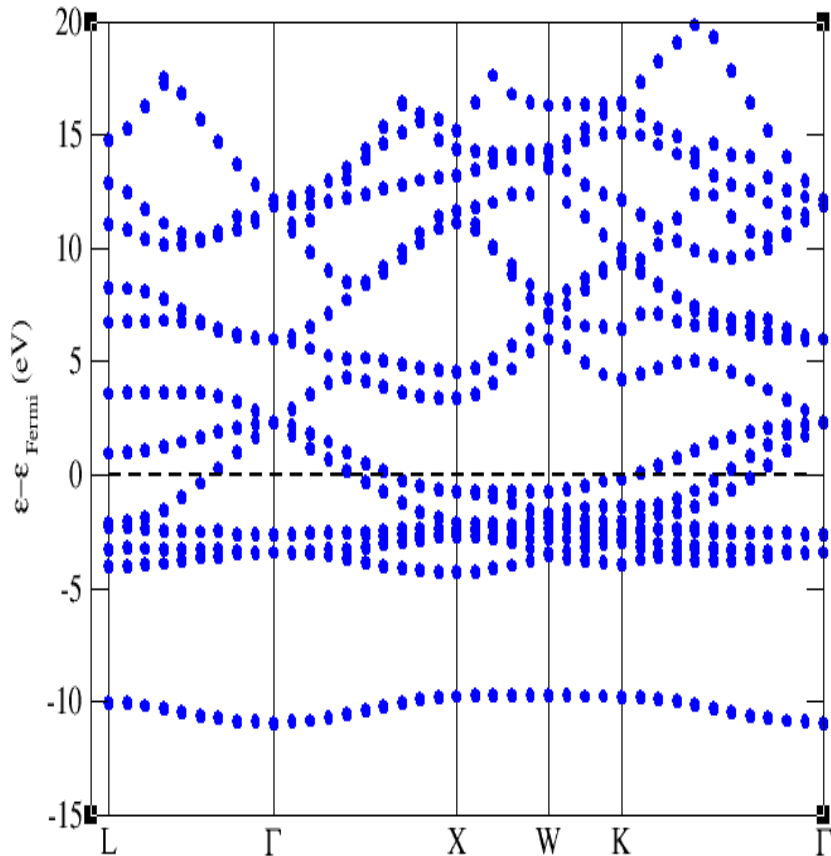
```
species {  
  ...  
  lcaoOrbitals = [s,p,d];  
  atomicRhoOcc = [[1,2,0],[1,1,0]];  $\beta$   $(\uparrow s^1 p^2 d^0, \downarrow s^1 p^1 d^0)$   
  ...  
}  
species {  
  ...  
  lcaoOrbitals = [s,p,d];  
  atomicRhoOcc = [2,3,0];  $\beta$   $(s^2 p^3 d^0)$   
  ...  
}  $\uparrow$   
  $(\uparrow s^1 p^{1.5} d^0, \downarrow s^1 p^{1.5} d^0)$ 
```



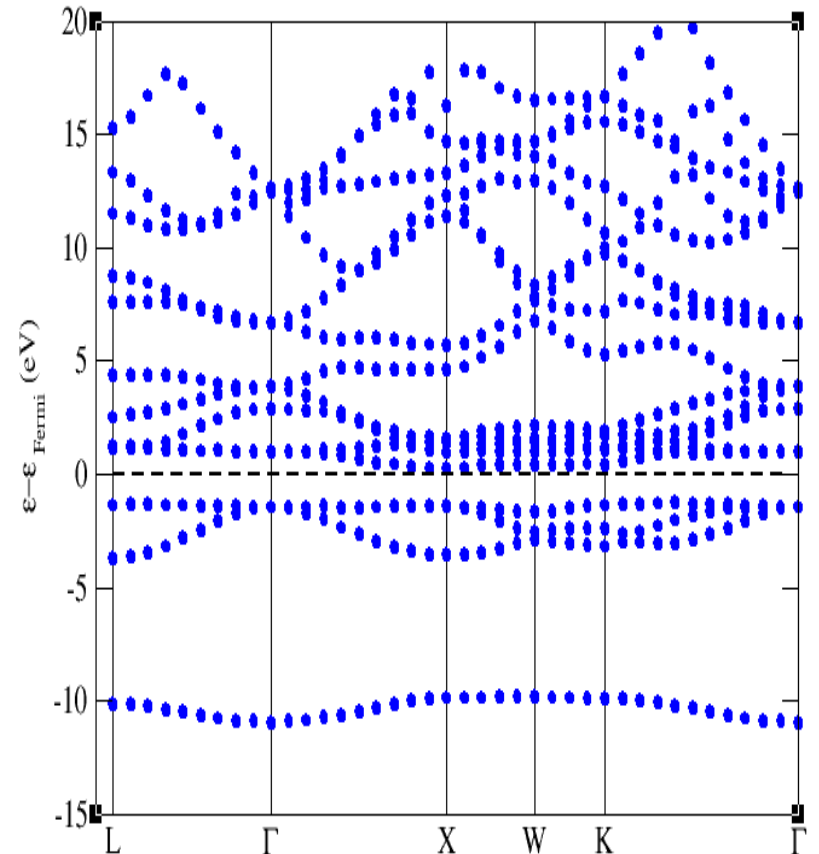
Hint: to get nonzero spin density system must be metallic  $\rightarrow$  all-state-CCG can not be used

# Magnetic structure analysis

MnAs band structure



MnAs band structure

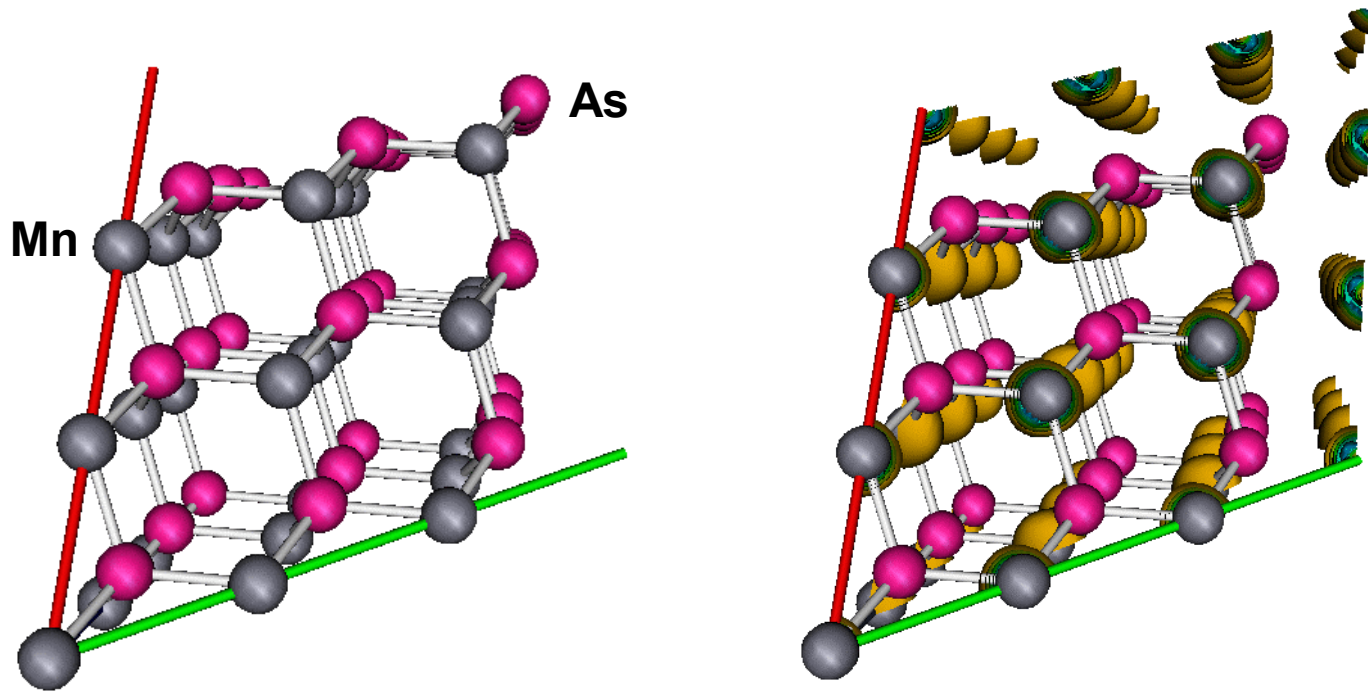


MnAs(zinc blende) band structure for majority and minority spin channels



# Visualization of spin density

$$r_{SPIN}(\vec{r}) = r_{\uparrow}(\vec{r}) - r_{\downarrow}(\vec{r})$$



MnAs (zinc blende) atomic structure

MnAs (zinc blende) spin density

## Tasks on one's own

Using different initial magnetic structure initialization schemes calculate:

- Isolated As atom (spin-polarized / spin-neutral)
- Isolated Ga atom (spin-polarized / spin-neutral)

Analyze obtained electronic structures (TDOS and PDOS) and draw conclusion about importance of spin-polarization

Perform analysis of MnAs (zinc blende) magnetic crystal:

- Analyze atomic structure
- Obtain SCF charge density
- Visualize structure and SCF charge density, spin density
- Get and analyze band structure
- Calculate converged TDOS

## What one should learn in this session

- Setup nonmagnetic SCF run
- Setup band structure calculations
- Analyze band structure output
  
- Setup magnetic SCF run
- Different ways how to setup initial magnetic structures
- Visualization of spin density
- Band structure for magnetic system