





Applications and New Developments

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Outline

- Motivation: Soft and Nanostructured Matter
- AdResS: Adaptive Resolution MD Simulation
 - Method, first Applications
 - Recent developments
- Particle-Continuum: AdResS + Hybrid MD
- Conclusions/Outlook

Soft Matter

"Soft" means:

- low energy density

- nanoscopic length scales (10Å ...1000Å)

- large (conformational) fluctuations large *intra* molecular entropy

- <u>thermal energy k_BT</u> <u>relevant energy scale</u>



Characteristic Time and Length Scales



Local Chemical Properties --- Scaling Behavior of Nanostructures Energy Dominance --- Entropy Dominance of Properties

Energy Scale k_BT forT=300K $E = 1.38 \cdot 10^{-23} J / K \cdot 300 K$ $kT \approx 4.1 \cdot 10^{-21} J$ $kT \approx 2.5 \cdot 10^{-2} eV$ **Electronic structure, CPMD** $kT \approx 9.5 \cdot 10^{-4} E_{H}$ **Quantum Chemistry** $kT \approx 4.1 pNnm$ **Biophysics Membranes, AFM** $kT \Longrightarrow 200 cm^{-1}$ **Spectroscopy** $kT \Rightarrow 0.6kcal / mol$ $kT \Longrightarrow 2.5 kJ / mol$ $E \approx 3 \cdot 10^{-19} J \approx 80 kT$ **Chemical Bond** Hydrogen Bond $E \approx 4kT - 10kT$



Coarse Graining of Macromolecules: Examples

Azo Benzene LCs C. Peter, L. Delle Site, D. Marx

> Polystyrene, (w/wo additives) V. Harmandaris, D. Fritz N. Van der Vegt



BPA-PC L. Delle Site, C. Abrams K. Johnston (1998ff)

> Peptides C. Peter

Application: Diffusion Constant of PS

(two step approach AA->UA->CG)



Standard Approach: Run whole system on one level of resolution.



Do we always need/want to do that?

Andrienko et al, PRL 98, 227402 (2007)

C. Peter et al, 2008ff

M. Deserno et al., Nature, 2007

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Relevant Levels of Resolution Example:Polymer/Nanotube Composites



Aim at: Adsorption – Desorption, Flux of Chains, Additives, Structure Formation, grand canonical MD

AdResS

Adaptive Resolution MD Simulation





Praprotnik, Delle Site, KK, JCP., 123, 224106 (2005).

AdResS: Adaptive Resolution Simulations

Free exchange of molecules/particles between regimes with different levels of resolution:

equilibrium between both regimes, no kinetic barrier



M. Praprotnik, L. Delle Site, KK, JCP 2005, Ann. Rev. Phys. Chem. 2008, 59: 545-71

Adaptive Methods: Changing degrees of freedom (DOFs) on the fly

Requirements

- Same mass density
- Same Pressure (=>Eq. of state, ?)
- Same temperature

Free exchange between regimes

■Same center-center g(r) (?)

- •(Simple two body potential)
- \Rightarrow "Some similarities" to 1st order phase transition
- \Rightarrow "Phase equilibrium"
- ⇒ Thermostat has to provide/take out latent heat due to change in degrees of freedom

VW Foundation Project M. Praprotnik, L. DelleSite, KK, JCP 2005, PRE (2006)



Adaptive Methods: Changing degrees of freedom (DOFs) on the fly



Requirements:

- Free exchange of molecules
- NO (free) energy barriers
- Smooth transition forces
- Structure and dynamics preserved
 - (at least in all atom region)

Newton's 3rd law:

- Force should be antisymmetric on exchange of particles α ↔ β
- Weight must depend on both particles

Transition Regime – Interpolation of Energy $U_{\alpha\beta}$?

$$U_{\alpha\beta} = w(X_{\alpha})w(X_{\beta})U_{\alpha\beta}^{atom} + [1 - w(X_{\alpha})W(X_{\beta})]U_{\alpha\beta}^{cg}$$

Full atomistic potential
Full coarse grained potential

$$\mathbf{F}_{\alpha\beta} = -\nabla_{\alpha}U = \mathbf{F}_{\text{Newton}} - [\nabla_{\alpha}w(\mathbf{X}_{\alpha})]w(\mathbf{X}_{\beta})(U_{\alpha\beta}^{AA} - U_{\alpha\beta}^{CG})$$
$$\mathbf{F}_{\beta\alpha} = -\nabla_{\beta}U = -\mathbf{F}_{\text{Newton}} - w(\mathbf{X}_{\alpha})[\nabla_{\alpha}w(\mathbf{X}_{\beta})](U_{\alpha\beta}^{AA} - U_{\alpha\beta}^{CG})$$

Transition Regime – Interpolation of Energy $U_{\alpha\beta}$?

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Full atomistic potential Full coarse grained potential



- Drift terms from *W*(*x*)
- Violation of Newton's 3rd law
- Mathematical inconsistencies at boundaries
- There exists no *W(x)*, such that forces become conservative (L. Delle Site PRE 2007)

=> Force interpolation

AdResS: Transition Regime - Force Interpolation



* Similar problem already in H.C. Andersen, JCP 72, 2384 (1979)

Theoretical Basis: Temperature... Necessity of Thermostat

Example: Two spherical Particles, no new DOFs



 $p_A(\mu_A, T)V = p_B(\mu_B, T)V; \quad \kappa_A = \kappa_B$

Transition between models/levels of description => change in Free Energy



- Temperature well defined in whole box, fixed by thermostat
- Densities well defined
- Forces well defined => virial pressure well defined

Transition between models/levels of description => change in Free Energy





System will adjust to constant pressure everywhere.

How to keep all atom region unperturbed?

Structure based CG - Compressibility



SPC/E water, cg based on matching g(r)

Pressure

$$P = \rho k T - \frac{2}{3} \pi \rho^2 \int_0^\infty U'(r) g(r) r^3 dr$$

Compressibility

$$\kappa_T = \frac{1}{\rho k_B T} \left(1 + 4\pi \rho \int_0^\infty r^2 [g(r) - 1] dr \right) = \frac{1}{\rho k_B T} \frac{\langle N^2 \rangle - \langle N \rangle^2}{\langle N \rangle}$$

Equation of State: Pressure Correction

Structure based CG, based on g(r) - pressure corrected



Pressure leverage causes density wiggles: special model with $p_{cg}=p_{AA}$



Equation of state in transition regime not the same! (not surprising)

No energy function **but** well defined **forces** and thus well defined **pressures**

Calculate pressure in a plane X (Todd, Evans, Davies)

$$\bar{p}_{\beta\alpha}(\alpha) = \frac{1}{2A_{\alpha}\Delta\alpha} \langle \sum_{\alpha-\Delta\alpha \le \alpha_i \le \alpha+\Delta\alpha} m_i v_{i\beta} v_{i\beta} \rangle + \frac{1}{2A_{\alpha}} \langle \sum_{i=1}^N F_{i\beta} sgn(\alpha_i - \alpha) \rangle$$

S. Poblete, S. Fritsch, G. Ciccotti, L. Delle Site, KK, PRL 2012



Calculate pressure in a plane X (Todd, Evans, Davies)

$$\bar{p}_{\beta\alpha}(\alpha) = \frac{1}{2A_{\alpha}\Delta\alpha} \langle \sum_{\alpha-\Delta\alpha \le \alpha_i \le \alpha+\Delta\alpha} m_i v_{i\beta} v_{i\beta} \rangle + \frac{1}{2A_{\alpha}} \langle \sum_{i=1}^N F_{i\beta} sgn(\alpha_i - \alpha) \rangle$$

If density fixed to constant value

Effective Chemical Potential, at target density

•
$$\phi(x) = \mu_{atom} - \mu(w_i)$$
 (free energy per particle)



Calculating μ(w_i) with i = 2, 3, 4, 5, 6, 7:
 (a): insertion particle method (IPM) for each i ⇒ Excess chemical potential μ^{exc}(w_i)
 (b): fractional formula ⇒ kinetic (ideal gas) contributions μ^{kin}(w)

S. Poblete, M. Praprotnik, KK, L. Delle Site, JCP, 132, 114101 (2010)

Effective Chemical Potential

at target density







(b) Kinetic contribution : $\mu^{kin} \propto \left(\frac{w}{2}\right) lg(T) + lg \frac{\Gamma\left(\frac{w}{2}\right)}{\Gamma(w)}$

S. Poblete, M. Praprotnik, KK, L. Delle Site, JCP, 132, 114101 (2010)

Effective Chemical Potential: Thermodynamic Force F_{thm}

- "latent heat" leads to force: $F_{thm} = -\nabla_x \mu(x)$
- $-\nabla_x \mu^{exc}$ + thermostat for kinetic part



 F_{thm} can perform work on the particles in transition regime

Allows to couple almost any system No need to have same μ , same p in both regimes

S. Poblete, M. Praprotnik, KK, L. Delle Site, JCP, 132, 114101 (2010)

Variable pressure in AA and CG region: Thermodynamic Force F_{thm}



 $p_A(\mu_A, T)V \neq p_B(\mu_B, T)V; \qquad \kappa_A = \kappa_B$

$$\left(p_A(\mu_A, T) + \frac{\rho_0}{M_\alpha} \int_a^b \mathbf{F}_{\rm th}(x) \mathrm{d}x\right) V = p_B(\mu_B, T) V$$

Test case: Coarse Grained Water: SPC/E





Structure based Coarse Graining:

Perfect match of g(r) all atom – coarse grained

 $= \mathbf{K}_{cg}$

 $p_{cg} = 6200 p_{atomistic}$

Katomistic

BUT

 $\mathbf{g}(\mathbf{r}^{*})$



Control of Thermodynamics in Explicit Region

Coarse-grained potentials usually don't match the atomistic system's virial pressure The difference can be balanced via an iteratively-refined thermodynamic force [1] $\mathbf{F}_{th}^{i+1}(x) = \mathbf{F}_{th}^{i}(x) - \frac{M}{\rho_{0}^{2}\kappa_{T}}\nabla\rho^{i}(x)$

Density and particle fluctuations are preserved The explicit region behaves as an open system

[1] S. Fritsch, S. Poblete, C. Junghans, G. Ciccotti, L. Delle Site, and K. Kremer, Phys Rev Lett 17, vol 108, 2012 [Figures from therein]



Some Applications

- Fullerene in Toluene
- Fullerenes in water

Kirkwood Buff integrals:

- Peptides in water urea mixtures
- PNIPAM in water alcohol mixtures





Table 1: Diffusion constants for the C60/toluene center of mass

C60 in Toluene

C. Junghans, S. Fritsch



C ₆₀	Diffusion constants [nm ² /ps]
All-atom	$D = 6.3 \times 10^{-4}$
AdResS	
$r_{\rm at} = 0.75\rm nm$	$D = 9.0 \times 10^{-4}$
$r_{\rm at} = 1.0{ m nm}$	$D = 8.2 \times 10^{-4}$
$r_{\rm at} = 1.5{\rm nm}$	$D = 7.9 \times 10^{-4}$
AdResS with TF	
$r_{\rm at} = 0.75\rm nm$	$D = 7.2 \times 10^{-4}$
Pure toluene	
All-atom	$D = 2.2 \times 10^{-3}$
Coarse-grained	$D = 8.6 \times 10^{-3}$





C60 in Toluene C. Junghans, S. Fritsch





Example for GROMACS implementation





B. P. Lambeth, C. Junghans, KK, C. Clementi, L. Delle Site, JCP 2010



cg water reproduces g(r) but NOT tetrahedral packing!

B. P. Lambeth, C. Junghans, KK, C. Clementi, L. Delle Site, JCP 2010

THE

JOURNAL OF

CHEMICAL

PHYSICS

Hydrophobic Solutes



Influence of bulk H-bond structure on surface layer

two surface potentials
 - standard (weak) Lennard Jones
 (ε_{co} 0.2k_BT, σ_{co} 0.34nm)
 - purely repulsive (r⁻¹²)
 # variable width of explicit layer



AIP

of Water Molecules around Solute, variable all atom water layer d_{ex} (1 1st, 2nd shell, 1)



LJ interaction dominated by surface

Interaction

Repulsive

of waters close to surface
strongly depleted



Fluctuation theory of Kirkwood-Buff

Fluctuation theory: Global thermodynamic properties from microscopic (pair-wise) molecular distribution



 $\Delta N_{ii} = \rho_i G_{ii}$

Excess (depletion) coordination number

$$\begin{split} \mathbf{G}_{\mathrm{ij}} &= V \left[\frac{\langle N_{\mathrm{i}} N_{\mathrm{j}} \rangle - \langle N_{\mathrm{i}} \rangle \langle N_{\mathrm{j}} \rangle}{\langle N_{\mathrm{i}} \rangle \langle N_{\mathrm{j}} \rangle} - \frac{\delta_{\mathrm{ij}}}{\langle N_{\mathrm{j}} \rangle} \right] \\ &= 4\pi \int_{0}^{\infty} \left[\mathbf{g}_{\mathrm{ij}}^{\mu \mathrm{VT}}(r) - 1 \right] r^{2} dr, \end{split}$$

Solvation energy

- Partial molar volume
- Activity coefficient
- Compressibility

Kirkwood and Buff, J. Chem. Phys. 19, 774 (1951).



Fluctuation theory of Kirkwood-Buff



Activity coefficient

$$\gamma_{
m cc} = 1 + \left(rac{\partial \ln \gamma_c}{\partial \ln \rho_c}
ight)_{p,T} = rac{1}{1 +
ho_c \left({
m G}_{cc} - {
m G}_{cw}
ight)}$$
 $k_B T \ln \gamma_c$

Solvation free energies

$$\lim_{\rho_s \to 0} \left(\frac{\partial \Delta \mathcal{G}_s}{\partial x_c} \right)_{p,T} = \frac{RT \left(\rho_w + \rho_c \right)^2}{\eta} \left(\mathbf{G}_{sw} - \mathbf{G}_{sc} \right)$$
$$\eta = \rho_w + \rho_c + \rho_w \rho_c \left(\mathbf{G}_{ww} + \mathbf{G}_{cc} - 2\mathbf{G}_{cw} \right)$$

Kirkwood and Buff, J. Chem. Phys. 19, 774 (1951).



Kirkwood-Buff integrals



Kirkwood and Buff, J. Chem. Phys. 19, 774 (1951).



- Non-ideal mixture (water-cosolvent)
- Biophysical processes are intimately linked with large density fluctuations (conformational transition)
- Excess in one region leads to depletion elsewhere
- KBI does not converge
- Thermodynamics away from a protein structure is ill-defined



Test case: methanol water mixture



Mukherji, van der Vegt, Kremer, and Delle Site, J. Chem. Theory Comp. (Letter) 8, 375 (2012).





- Study solvation of large (bio)macromolecules
- Device an efficient method
- Correct concentration fluctuations
- Solvent equilibrium



"Effective" open boundary

Why not go open boundary? Make use of Kirkwood-Buff theory!

Tri-glycine in Urea-Water Mixture



Mukherji, van der Vegt, and KK, JCTC 8, 3536 (2012).



Urea-Water



Mukherji, van der Vegt, and KK, JCTC 8, 3536 (2012).





Auton and Bolen, PNAS 102, 15065 (2005).

Mukherji, van der Vegt, and Kremer, J. Chem. Theory Comp. 8, 3635 (2012).

Some Applications

- Fullerene in Toluene
- Fullerenes in water

Kirkwood Buff integrals:

- Peptides in water urea mixtures
- PNIPAM in water alcohol mixtures: "Grand Canonical" AdResS



Zhang and Wu, Physical Review Letters 86, 822 (2001). Mukherji and Kremer, submitted (2013).









Poly-NIPAm chemical potential





Poly-NIPAm chemical potential



NIPAm in aqueous methanol



AdResS-HybridMD: Water



R. Delgado Buscalioni, KK, M. Praprotnik, JCP 131, 244107 (2009)

HybridMD: Coupling Particle-Based and Continuum Descriptions

The hybrid particle-continuum scheme (HybridMD) is designed to connect the dynamics of a "molecular domain" with that obtained from a continuum description of the surrounding fluid flow.

The method is based on flux-exchange.

- The system is divided in (at least) two domains, described via classical molecular dynamics (MD) and continuum fluid dynamics (CFD), i.e., solving the Navier-Stokes equations.
- The MD and CFD domains share one unique "hybrid interface", H: Flux balance implies the conservation of mass and momentum across H.

PROBLEM: Particle Insertion into Buffer

G. De Fabritiis, R. Delgado Buscalioni, P. Coveney, Phys. Rev. Lett 97, 134501 (2006). R. Delgado Buscalioni, G. De Fabritiis, Phys. Rev. E 76, 036709 (2007).

AdResS-HybridMD combined



Domain decomposition of the combined scheme. The top part of the figure shows the location of the fluid model layers (cg, hyb and ex) within the HybridMD setup. The bottom part of the figure shows the set of control cells used in the HybridMD setup. setup.

Particle Insertion into Buffer SIMPLE

AdResS-HybridMD: Setups



Heterogeneous model buffer



AdResS-HybridMD combined



Concurrent Triple-Scale Simulation of Molecular Liquids

Simple shear









Conclusion / Challenges

- Dual-Triple... Scale Simulations/Theory
 - Adaptive quantum ⇔ force field ⇔ coarse grained ...
 - Grand Canonical i.e. salt etc
 - Thermodynamic Force/ compensition scheme: couple rather different systems
 - H-AdResS: adaptive Monte Carlo possible
- Nonbonded Interactions: NEMD, Structure Formation, Morphology...
- Conformations <> Electronic Properties
- Structure Formation, Aggregation
- Online Experiments:
 - Nanoscale Experiments, long Times