

# Barcelona September 2013

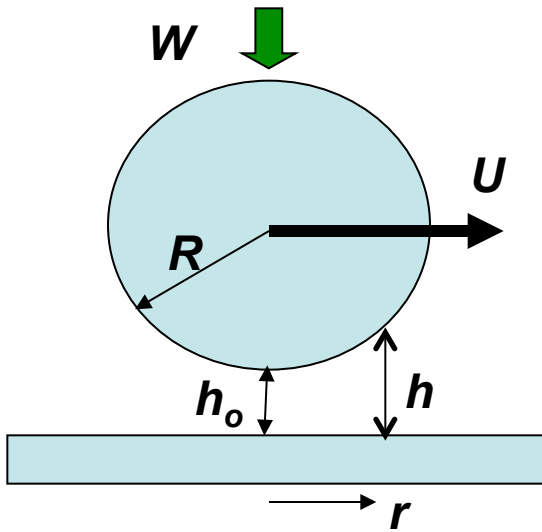
## The Friction between Structured Surfaces

Catarina Mendonça and Dominic Tildesley, CECAM, EPFL,  
Lausanne Switzerland

Patrice Malfreyt University of Clermont Ferrand



# Origins of hydrodynamic lubrication



Gap

$$h = h_0 + \frac{r^2}{2R}$$

Defines a contact area

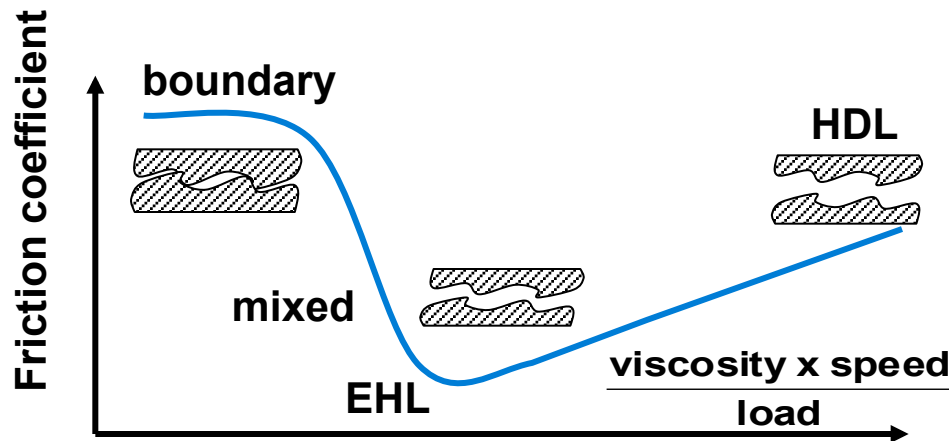
$$r^2 \approx 2Rh_0$$

Tangential force

$$T = \eta \dot{\gamma} \times \pi r^2 \approx \frac{\pi \eta U r^2}{h_0} \quad \left[ \dot{\gamma} \approx \frac{U}{h_0} \right]$$

Friction coefficient

$$\mu = \frac{T}{W} \approx \frac{\pi \eta U r^2}{W h_0} \approx 2\pi R \times \frac{\eta U}{W}$$

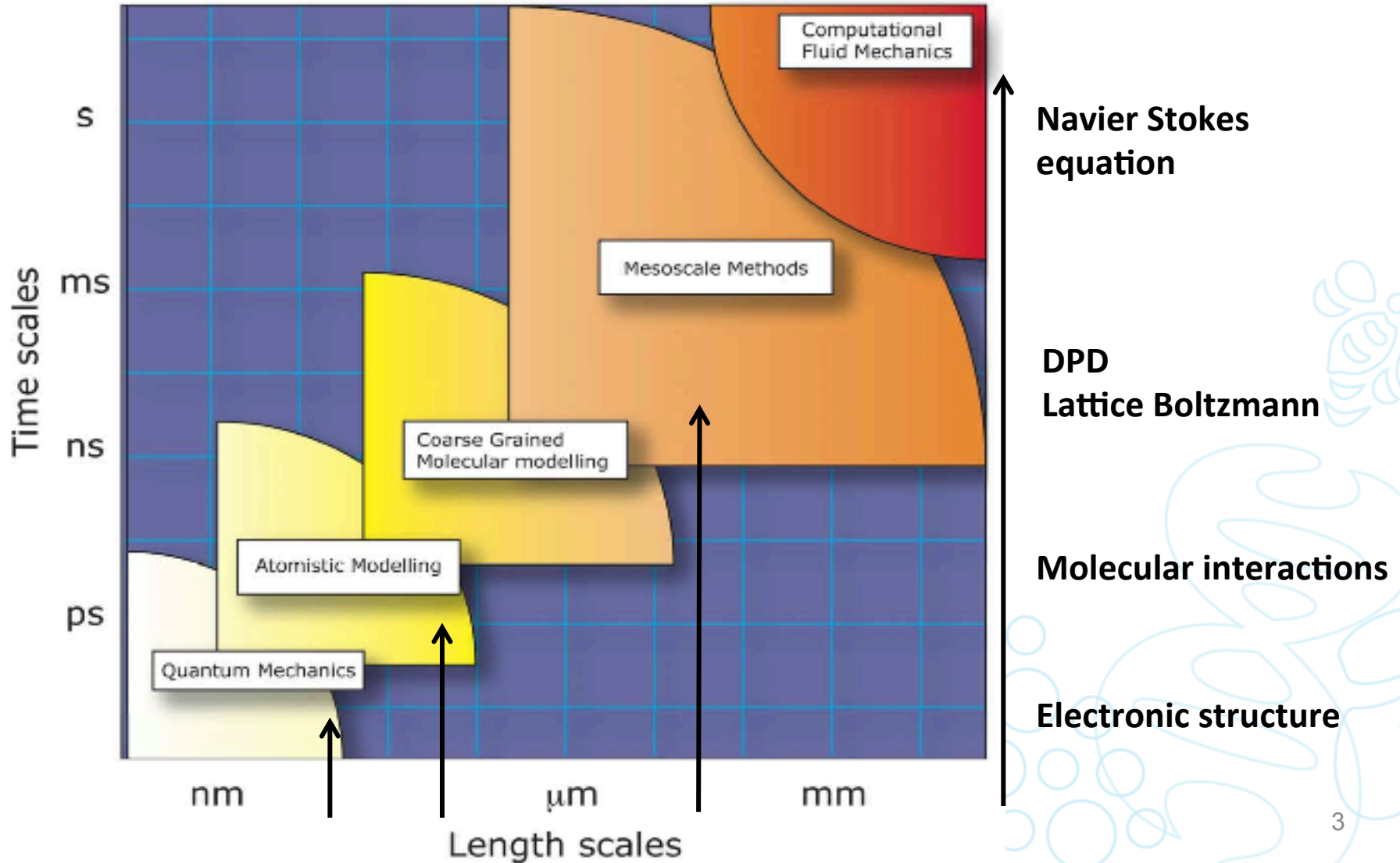


**hydrodynamic part of the Stribeck curve**

Pyotr Kapitza

J Tech Phys 25, 747 (1955)

# Multi-scale Modelling

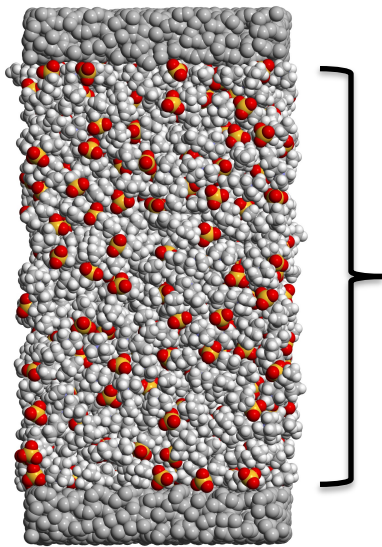


# Atomistic simulations of boundary lubrication

- **Liquids in confinement**

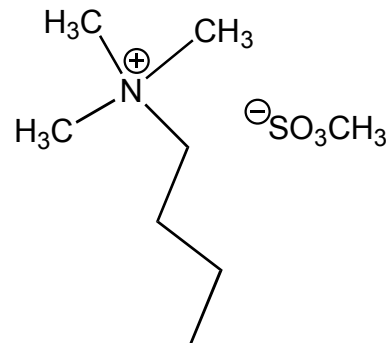
## Ionic lubricants

Carbon surfaces

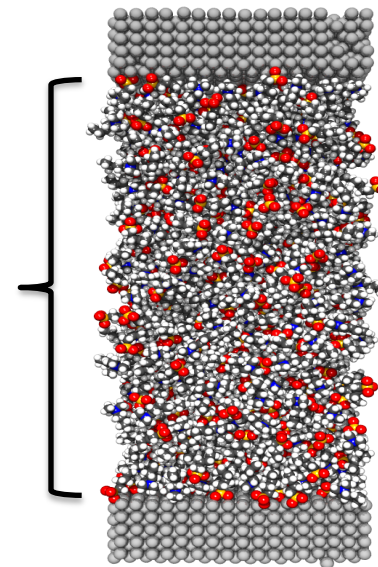


Liquid Lubricant

Ionic liquid





Metallic surfaces



# Force field parameterisation

- **Potential function of the system**

$$U = U_{L-L} + U_{S-S} + U_{S-L}$$

 Force fields available (all-atoms description)  
 Force field NOT available

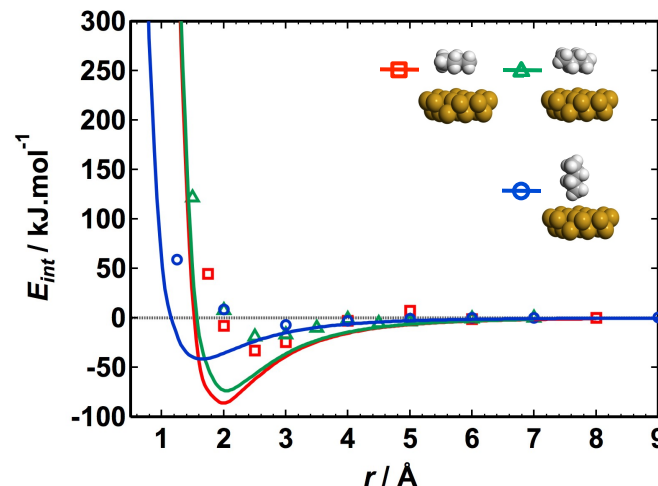
- **Surface-Lubricant interactions are complex to describe**

- Contribution from VDW interactions
- Coulombic interactions from the polarization of the metal surfaces, in the presence of ions

$$U_{LJ} = 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]$$

$$\epsilon_{ij} = \sqrt{\epsilon_i \epsilon_j}$$

$$\sigma_{ij} = \sqrt{\sigma_i \sigma_j}$$



**LJ potential is not adequate to describe such interactions**

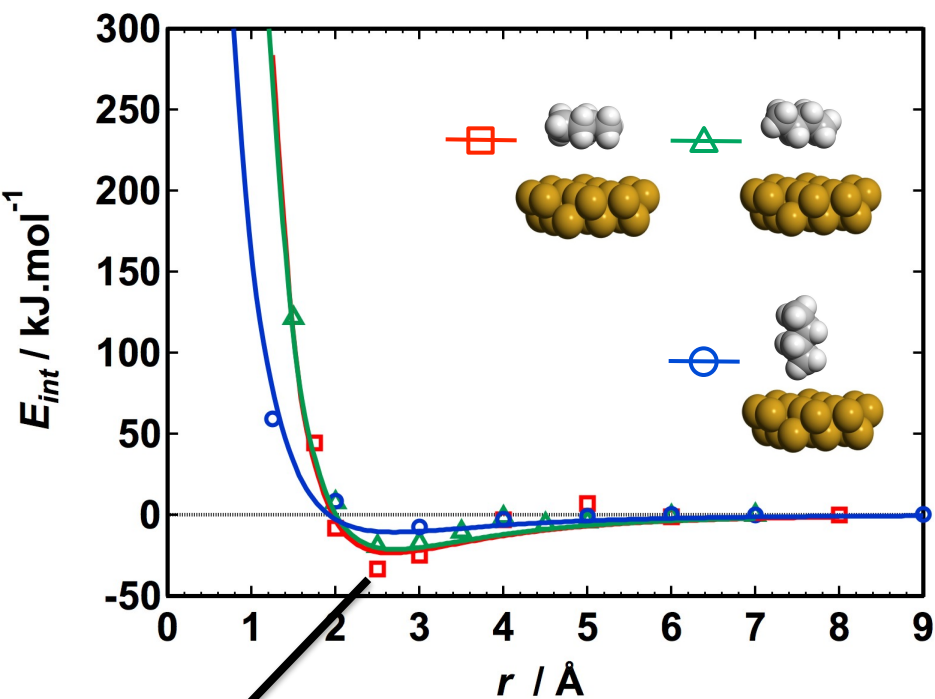


Development of an interaction model based in DFT calculations

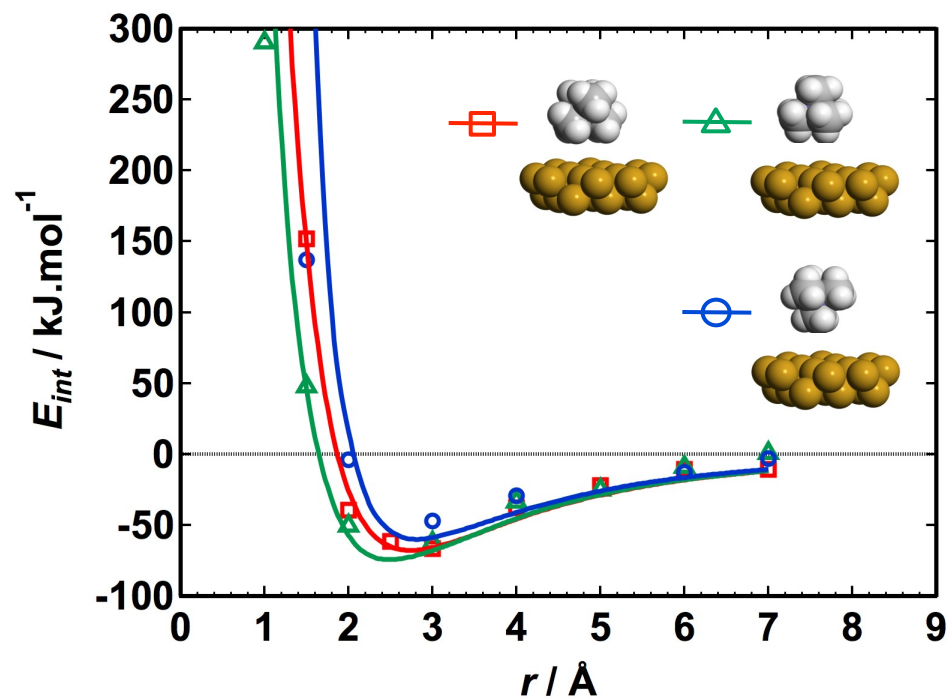
# Energies of interaction

MO6-L/ TZVP, ECP10MHF

Butane



Tetramethylammonium



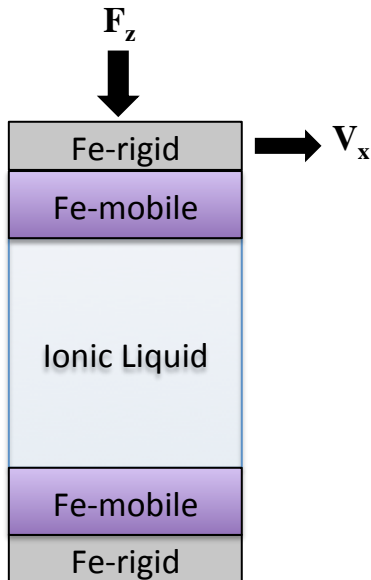
$\Delta H_{\text{ads}}$

$$U_{ij}(r_{ij}) = \sum_i \sum_j \frac{E_0}{(n-m)} \left[ m \left( \frac{r_0}{r_{ij}} \right)^n - n \left( \frac{r_0}{r_{ij}} \right)^m \right]$$

$i =$  Interaction site in the fragment  
 $j =$  Atom in the metal surface

# Non-equilibrium simulations

## • Shear and load conditions



### Simulated conditions:

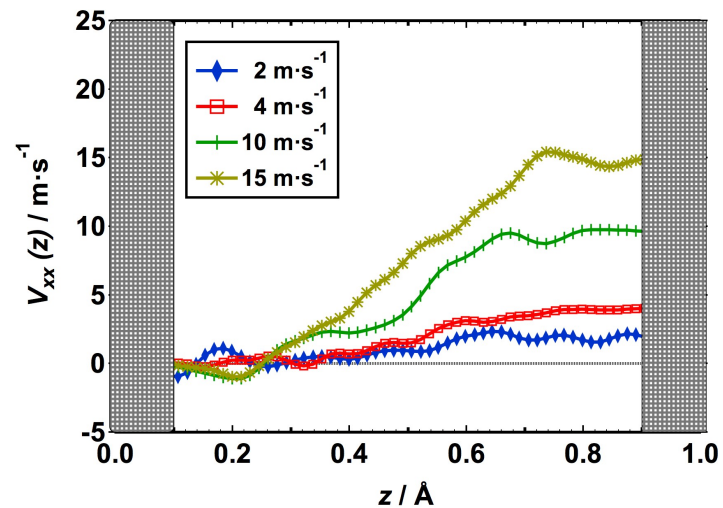
- Normal applied pressure: 90 – 800 Mpa (Experimental value ~ 1 Gpa)
- Shear velocity: 0.01 – 15  $\text{m}\cdot\text{s}^{-1}$  (Experimental value ~ 0.01  $\text{m}\cdot\text{s}^{-1}$ )

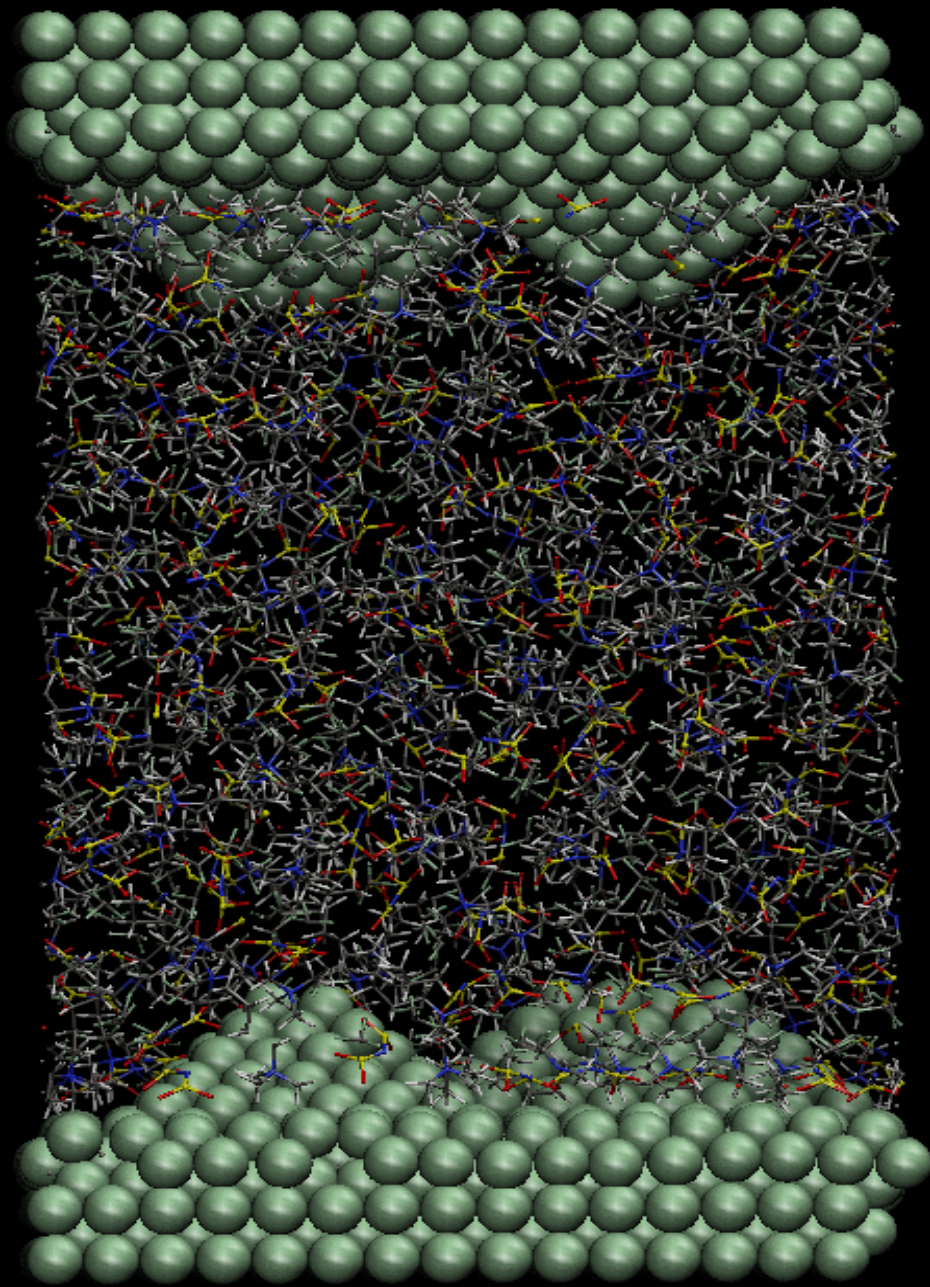
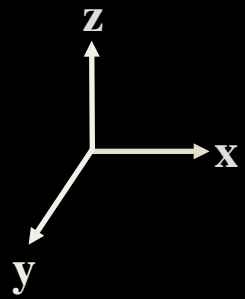
### Experimental conditions:

- Normal applied pressure: 1 GPa
- Shear velocity: 0.01 – 0.1  $\text{m/s}$

**Shear will create a gradient of velocity in the z-direction,  
for the particles in the fluid:**

$$v_{\alpha}(z_k) = \frac{\sum_{i=1}^N H_k(z_i)(v_i)_{\alpha}}{\sum_{i=1}^N H_k(z_i)}$$







# Thermodynamic properties

- **Temperature**

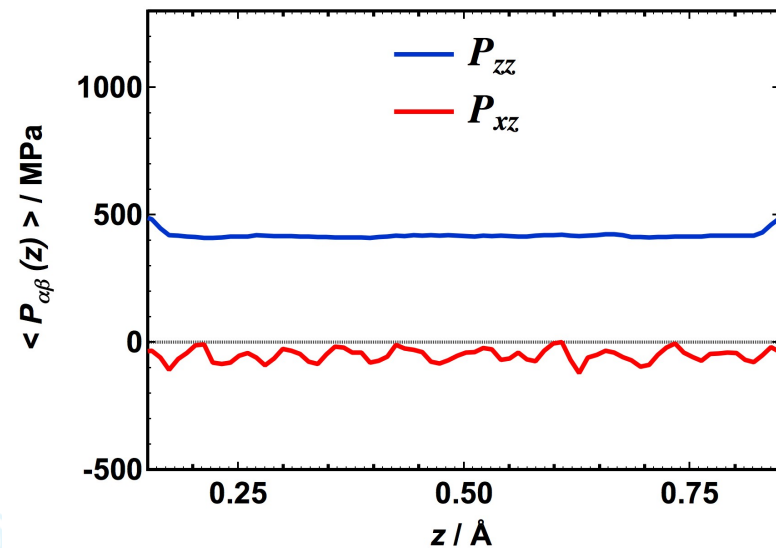
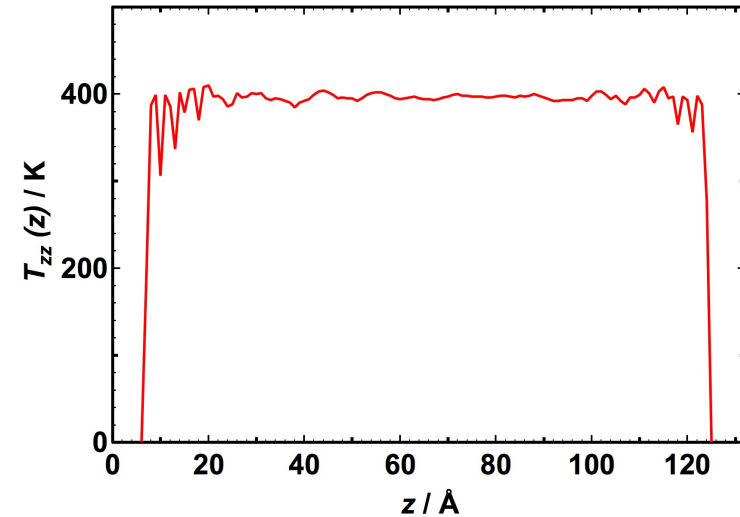
$$k_B T_{\alpha\beta}(z_k) = \left\langle \frac{\sum_{i=1}^N H_k(z_i) m_i [(v_i)_\alpha - u_\alpha(z_k)] [(v_i)_\beta - u_\beta(z_k)]}{\sum_{i=1}^N H_k(z_i)} \right\rangle$$

- **Pressure**

$$P_{\alpha\beta}(z_k) = P_{\alpha\beta}^{kin}(z_k) + P_{\alpha\beta}^{conf}(z_k)$$

$$P_{\alpha\beta}(z_k) = \langle \rho(z_k) \rangle k_B T_{\alpha\beta}(z_k)$$

$$+ \frac{1}{L_x L_y} \left\langle \sum_{i=1}^{N-1} \sum_{j>i}^N \frac{(\mathbf{r}_{ij})_\alpha (\mathbf{F}_{ij})_\beta}{|z_{ij}|} \theta\left(\frac{z_k - z_i}{z_{ij}}\right) \theta\left(\frac{z_j - z_k}{z_{ij}}\right) \right\rangle$$



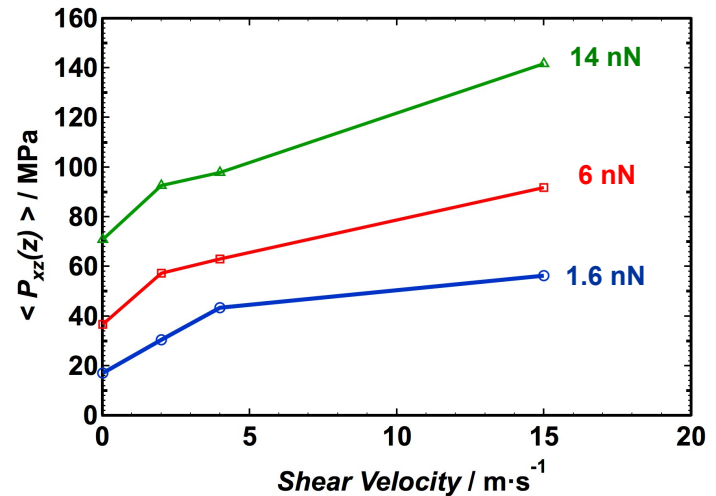
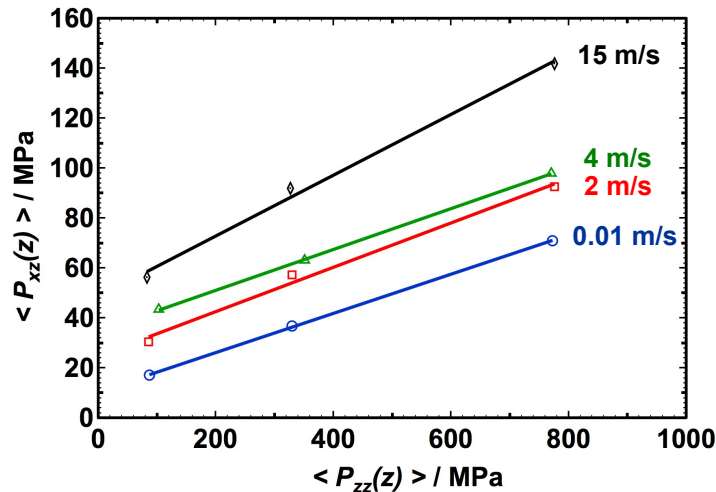
# Kinetic friction coefficient calculation

Amontons' 1<sup>st</sup> Law :  $F_x = \mu F_z$

Modified Amontons' 1<sup>st</sup> Law (for adhering surfaces) :  $F_x = F_0 + \mu F_z$

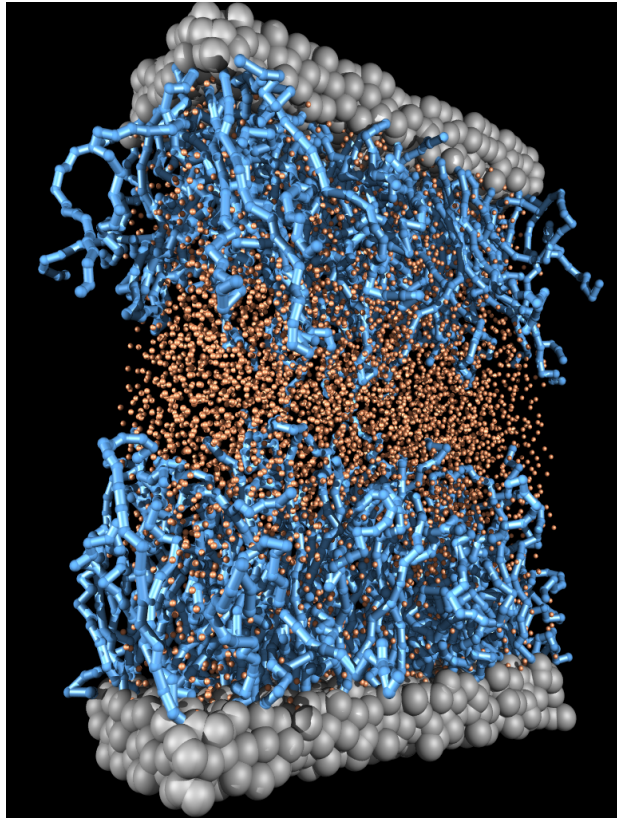
**Definition in terms of pressure**

$$\langle P_{xz}(z_k) \rangle = P_0 + \mu \langle P_{zz}(z_k) \rangle$$

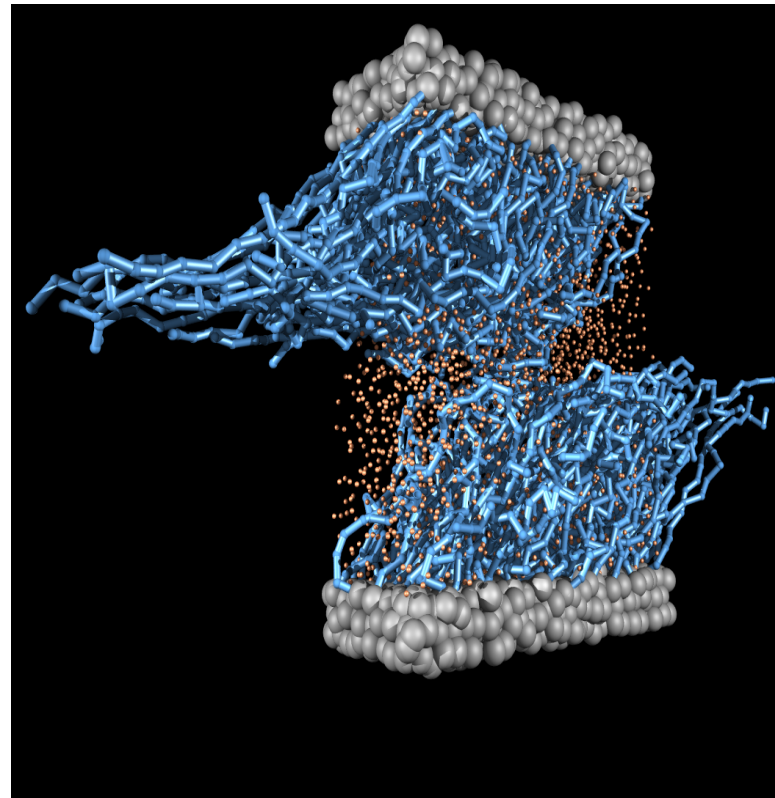


Shear velocity (m·s <sup>-1</sup> )	$\mu$
0.01	0.078
2	0.089
4	0.082
15	0.122

# Polymer brushes under shear a structured surface

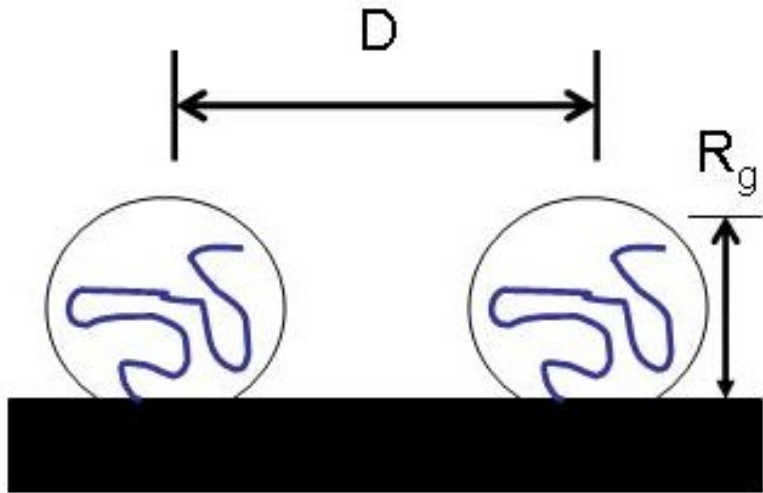


At equilibrium



Under shear

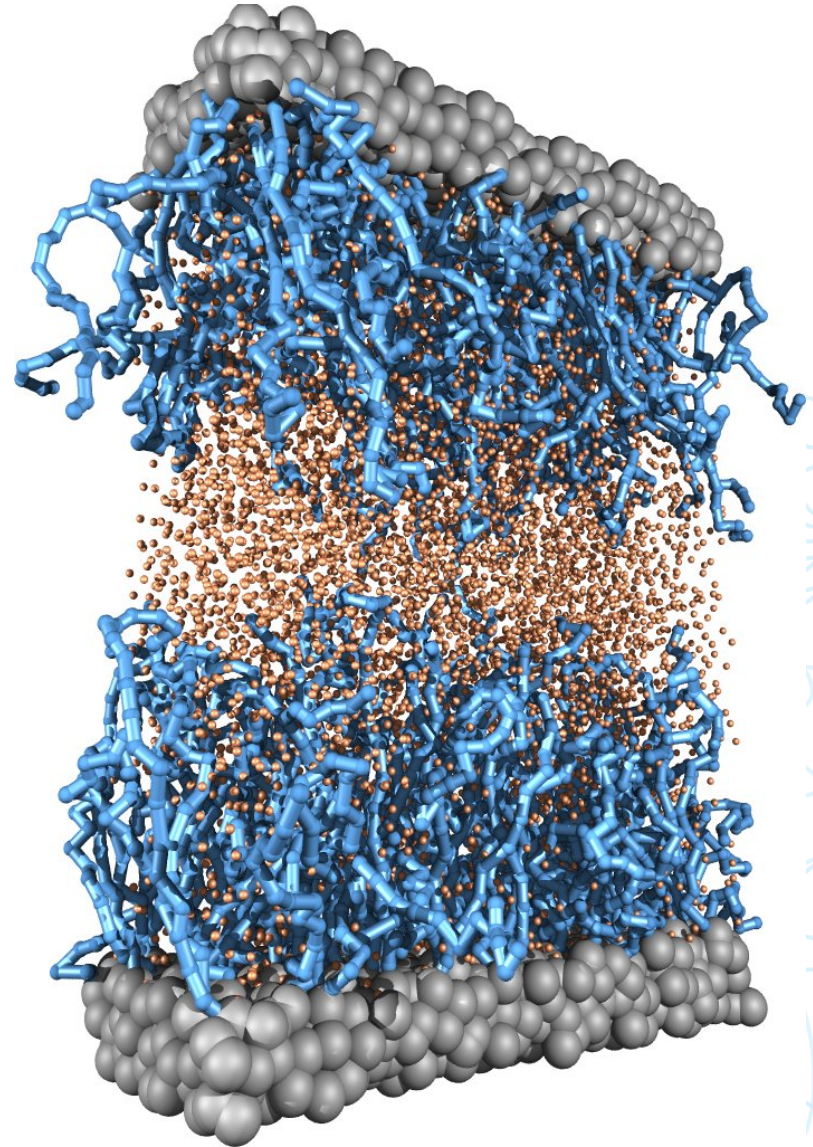
# Polymer brushes



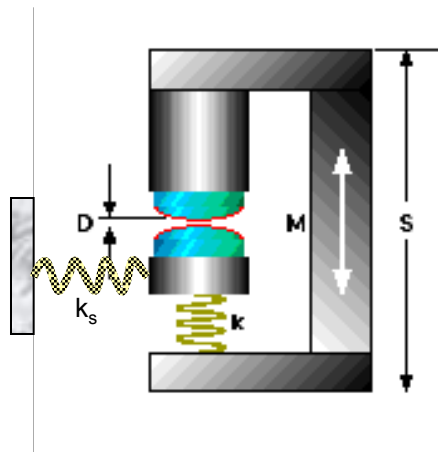
Polymer mushroom

The excluded volume repulsion (in a good solvent) balances the elastic pressure

Alexander, de Gennes 1977



# The surface forces apparatus



D. Tabor, R.H.S. Winterton,  
J.N. Israelachvili in the early 1970s  
at Cambridge University

## SFA of Polyelectrolyte brushes

U. Raviv, S. Giasson, N. Kampf, J. F. Gohy, R. Jerome, J. Klein, Nature 2003, 425, 163. **(PMMA)<sub>41</sub>(PSGMA)<sub>115</sub> physisorbed on to mica  $\epsilon_{\text{exp}} = 0.0006-0.001$**

B. Liberelle, S. Giasson, Langmuir 2008, 24, 1550. **PS-b-PAA covalent bound to mica  $\epsilon_{\text{exp}} = 0.05-0.25$**

**Fully charged polyelectrolyte brushes show friction coefficient ca. 40% lower Than neutral brushes (shear rate  $10^4 \text{ s}^{-1}$ )**

# Dissipative particle dynamics (DPD)

$$\mathbf{f}_{ij}^C = \begin{cases} a_{ij} \omega_C(r_{ij}) \hat{\mathbf{r}}_{ij} & (r_{ij} < r_c) \\ 0 & (r_{ij} \geq r_c) \end{cases}$$

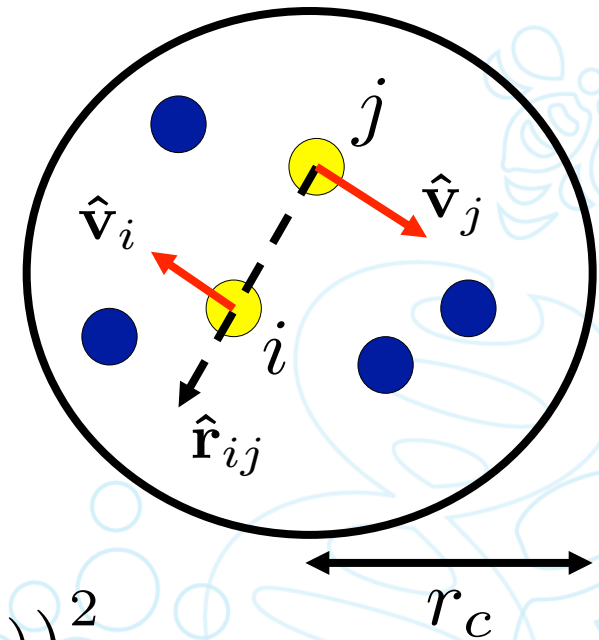
$$\omega_c(r_{ij}) = (1 - r_{ij}/r_c) \quad (r_{ij} < r_c)$$

$$\mathbf{f}_{ij}^D = -\gamma \omega^D(r_{ij}) (\hat{\mathbf{r}}_{ij} \cdot \mathbf{v}_{ij}) \hat{\mathbf{r}}_{ij}$$

$$\mathbf{f}_{ij}^R = \sigma \omega^R(r_{ij}) \theta_{ij} \frac{1}{\sqrt{\delta t}} \hat{\mathbf{r}}_{ij}$$

Fluctuation-dissipation theorem:

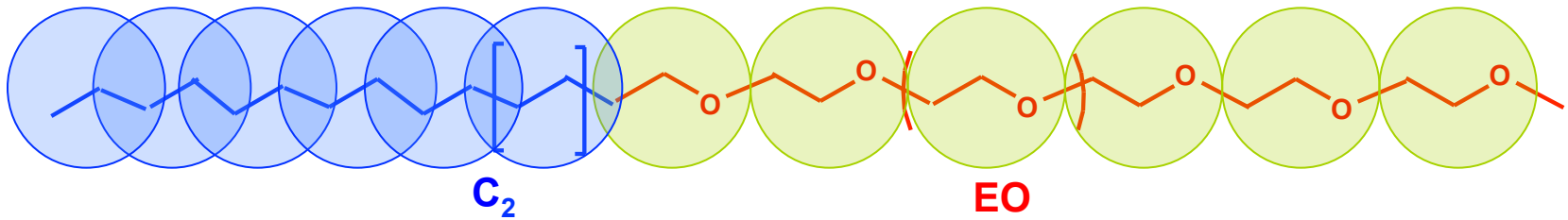
$$\gamma = \frac{\sigma^2}{2k_B T} \quad \text{et} \quad \omega^D(r_{ij}) = (\omega^R(r_{ij}))^2$$



# Can we use a longer timestep?

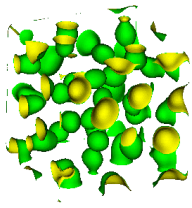
- By fitting to the water diffusion coefficient, we obtain timesteps of ca. 10ps. We are routinely performing runs of 10 $\mu$ s on 20,000 dpd particles.
- The lowest shear rates that we can study are between 10<sup>5</sup> and 10<sup>6</sup> s<sup>-1</sup> (perhaps one order of magnitude higher than the experimental oscillatory shear rates)
- The ratio of the Flory of the radius of the polymer to interpolymer spacing is the same in experiment and the dpd model. 1 dpd unit of pressure corresponds to 10 MPa
- A water bead contain 3-4 molecules, the polymer dpd 6-8 momomers.

# DPD parameter fitting: the mixing of water and a surfactant

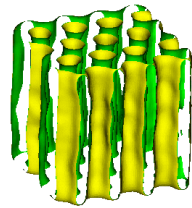


Water

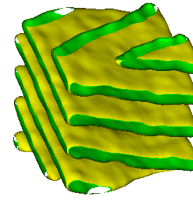
Surfactant



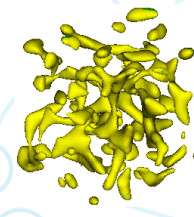
micellar



hexagonal

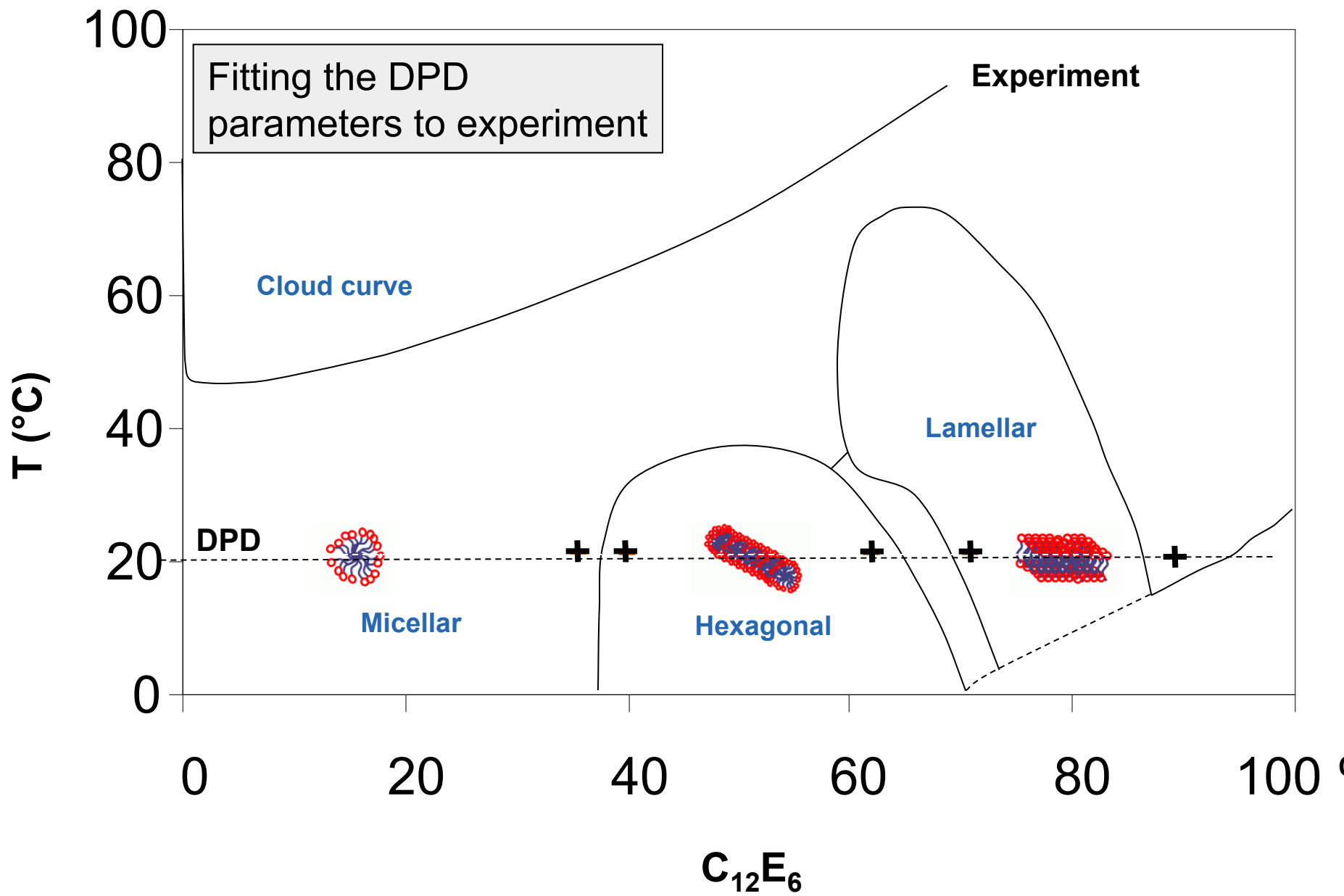


lamellar

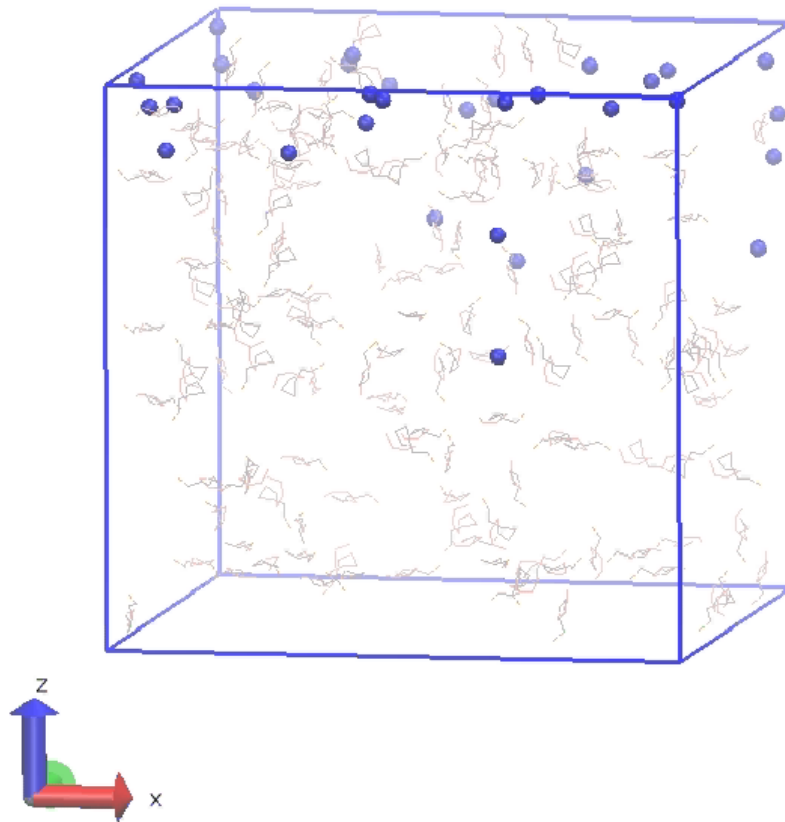


Inverse micellar

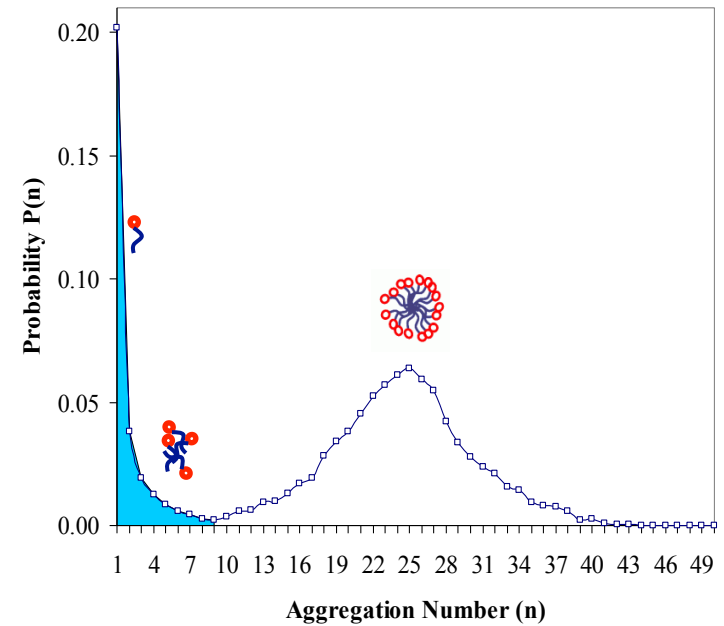




# Micellisation

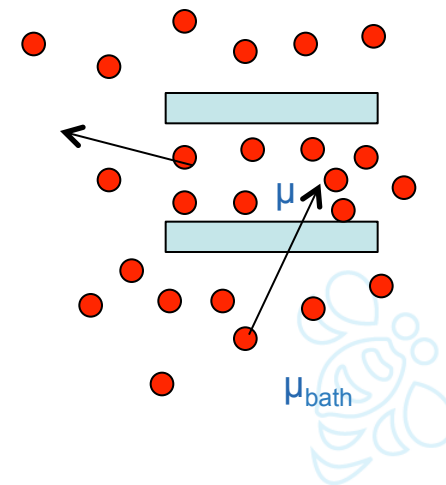
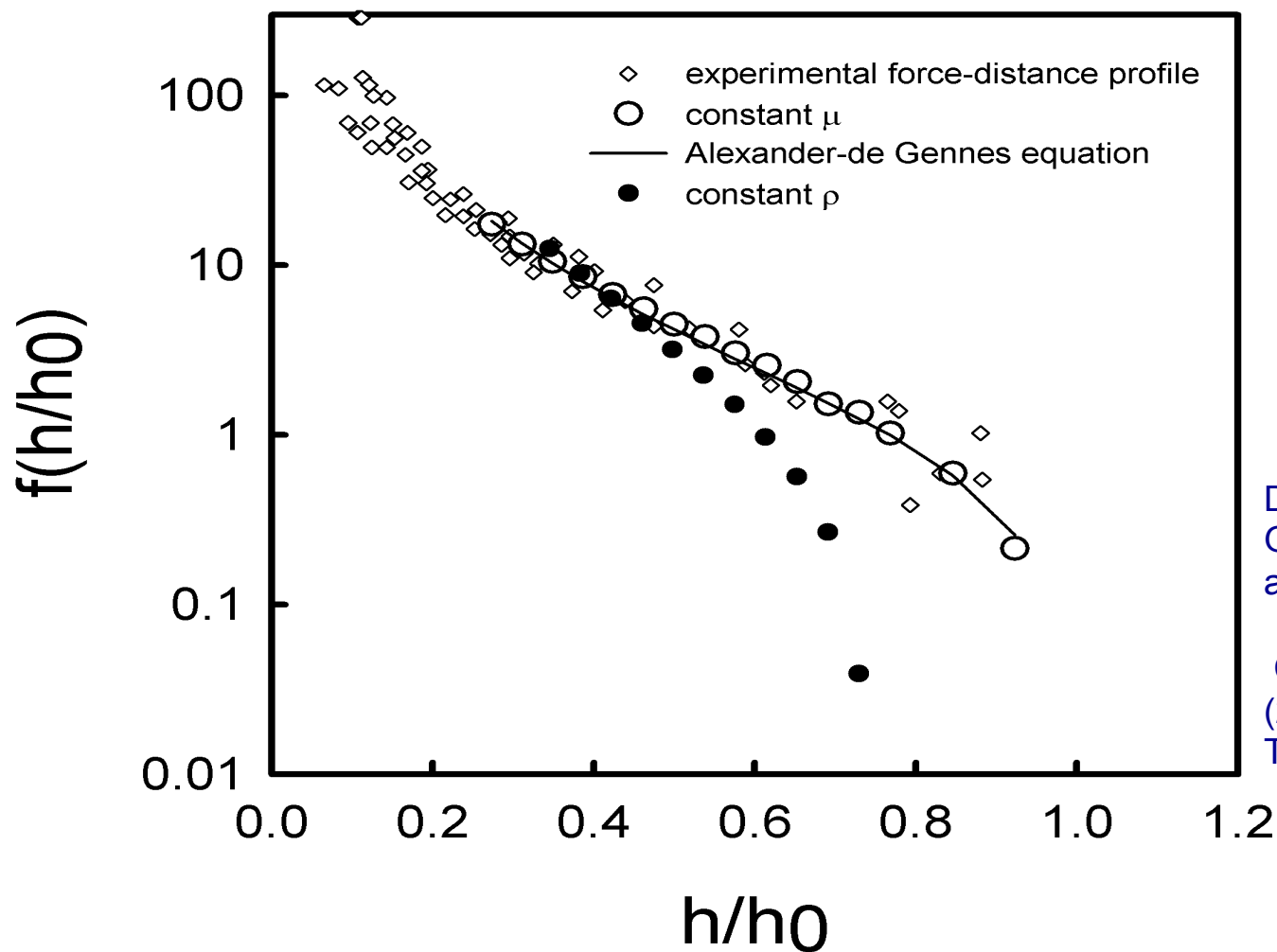


Massimo Noro  
And Patrick Warren  
Unilever Port Sunlight



$\text{CH}_3(\text{CH}_2)_{11}\text{PO}_6\text{EO}_2\text{SO}_3^- \text{Na}^+$   
calculated cmc      0.000082 wt  
experimental cmc    0.0001 wt.

# Force-distance curve for neutral polymer brushes



Dissipative dynamics in the Grand Canonical Ensemble: application to polymer brushes,

ChemPhysChem, **5**, 457-464 (2004) Gujon, Malfreyt and Tildesley

# Electrostatic potential

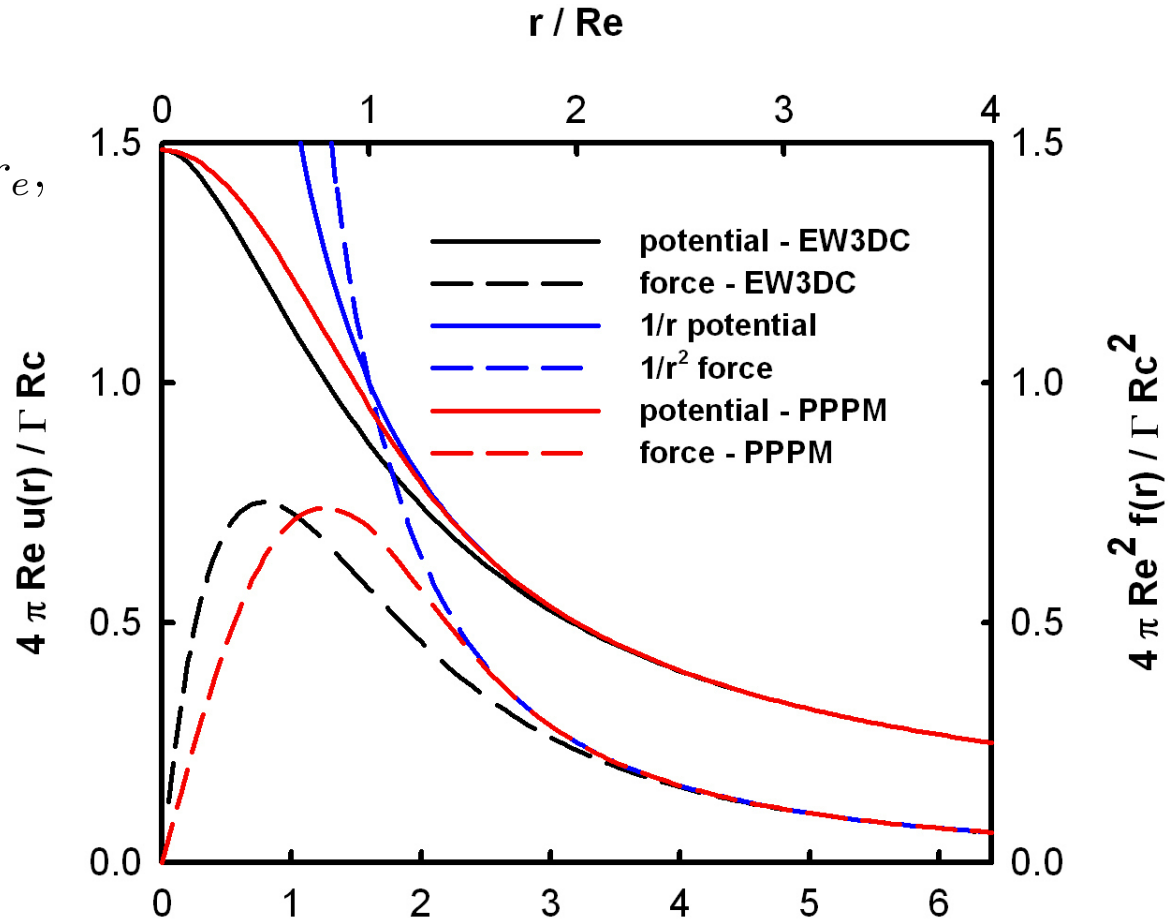
## PPPM method:

$$f(r) = \frac{3}{\pi r_e^3} (1 - r/r_e) \text{ for } r < r_e,$$

## Ewald method:

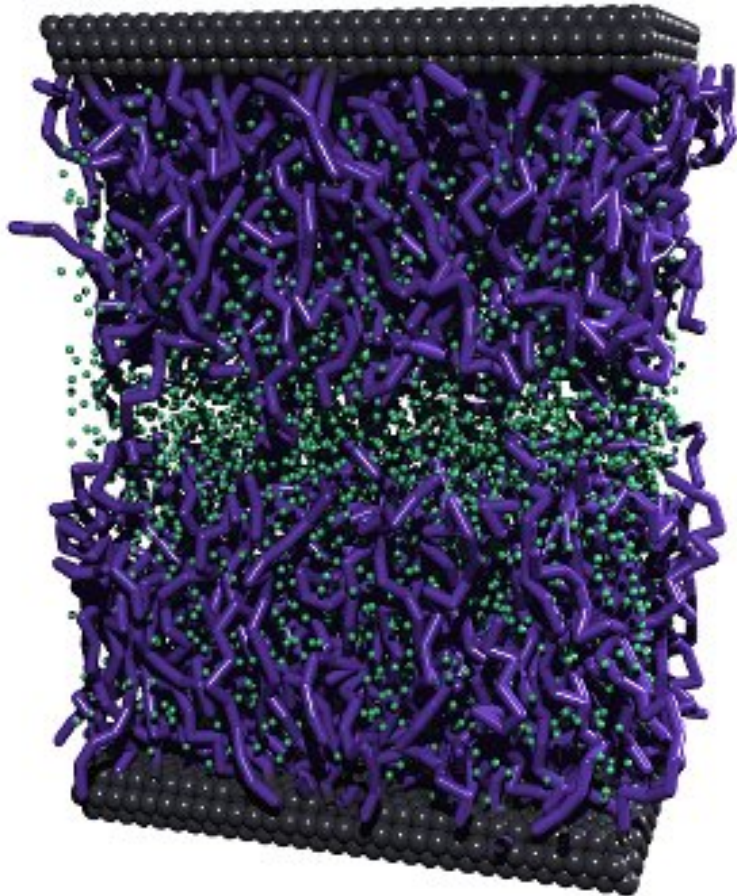
$$\rho(r) = \frac{q}{\pi \lambda^3} \exp(-2r/\lambda)$$

Comparison of PPM and Ewald for slab geometries



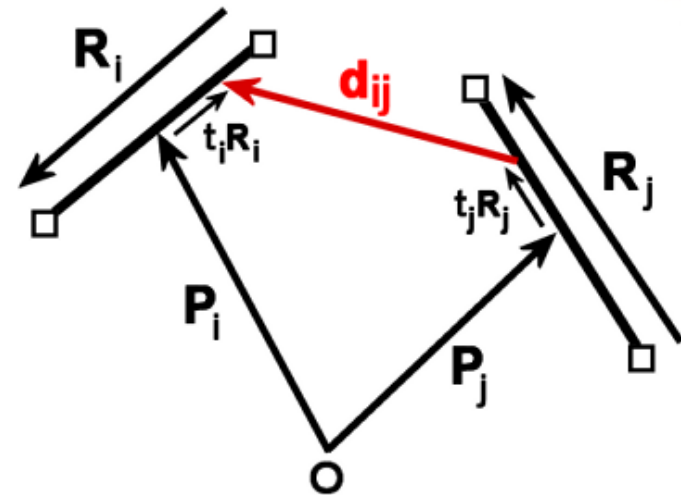
Electrostatic interactions in dissipative particle dynamics: toward a mesoscale modeling of the polyelectrolyte brushes. *Journal of Chemical Theory and Computation*, **5**, 3245-3259, (2009) Ibergay, Malfreyt and Tildesley

# Entanglement of DPD Polymers



Bilayer simulations

Calculate the minimum separation



Additional Entanglement Force

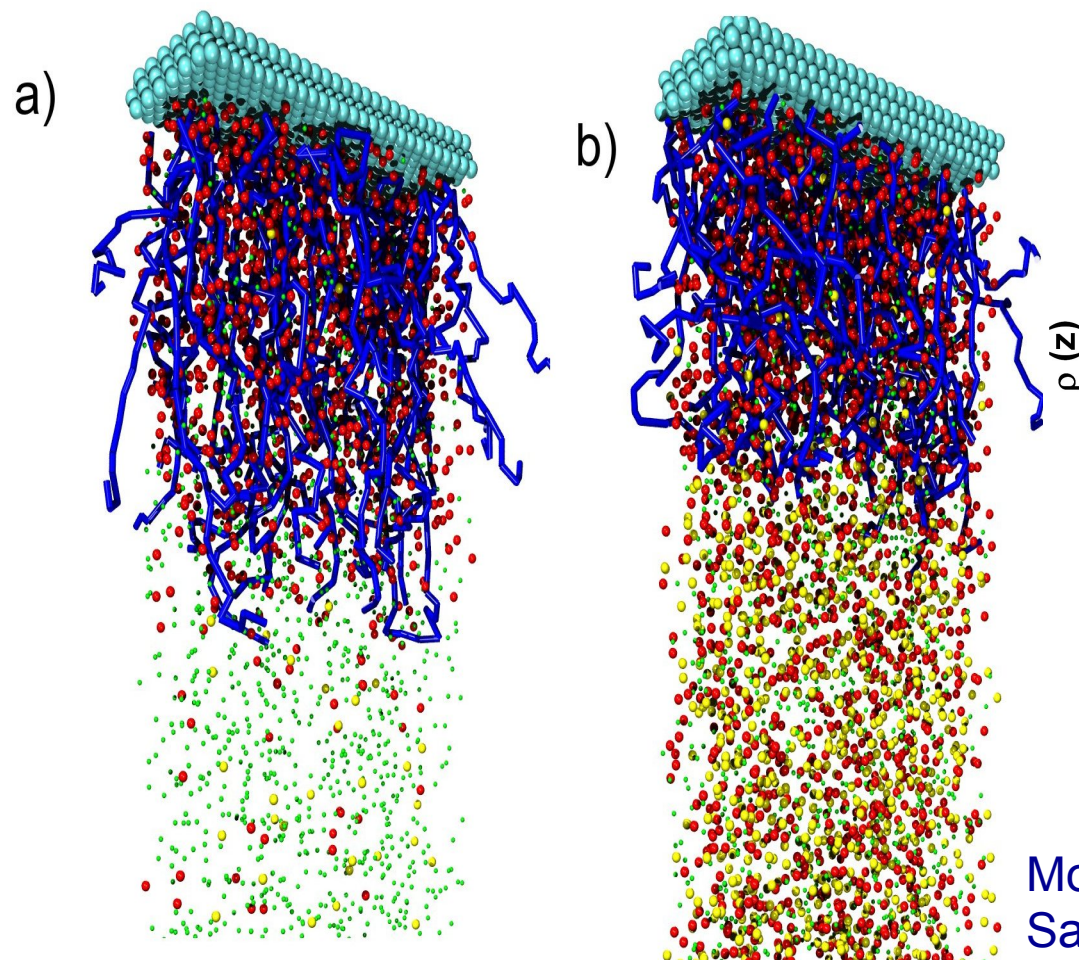
$$\mathbf{f}_{ij}^E = a_{ij}^E \left( 1 - \frac{d_{ij}}{r_c^E} \right) \hat{\mathbf{d}}_{ij} \quad d_{ij} \prec r_c^E$$

Mesoscopic simulation of entangled polymer brushes under shear: compression and rheological properties, *Macromolecules*, **42**, 4310–4318 (2009) ( Goujon, Malfreyt and Tildesley)

# The interaction of polyelectrolyte brushes

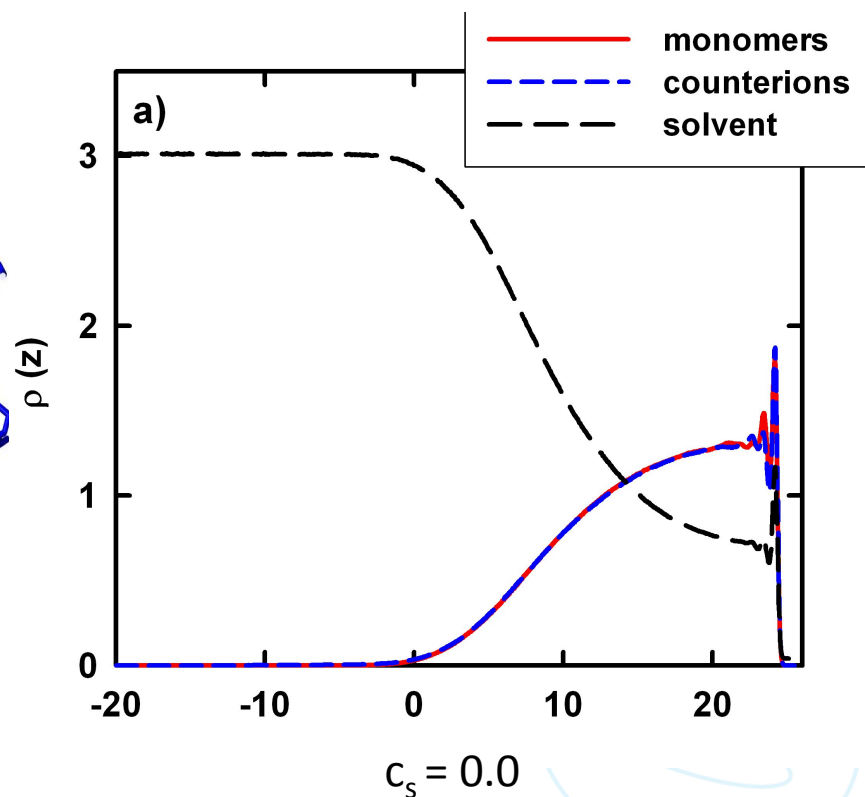
- Simulation in the grand canonical ensemble
  - Do not destroy the dynamics or hydrodynamics
- Modelling of chain crossing
  - Do not lose the speed advantage of DPD
- Electrostatics through distributed charge
  - Use modified Ewald over PPM
- Explicit modelling of counterions and solvent

# Modelling of polyelectrolytes single brush



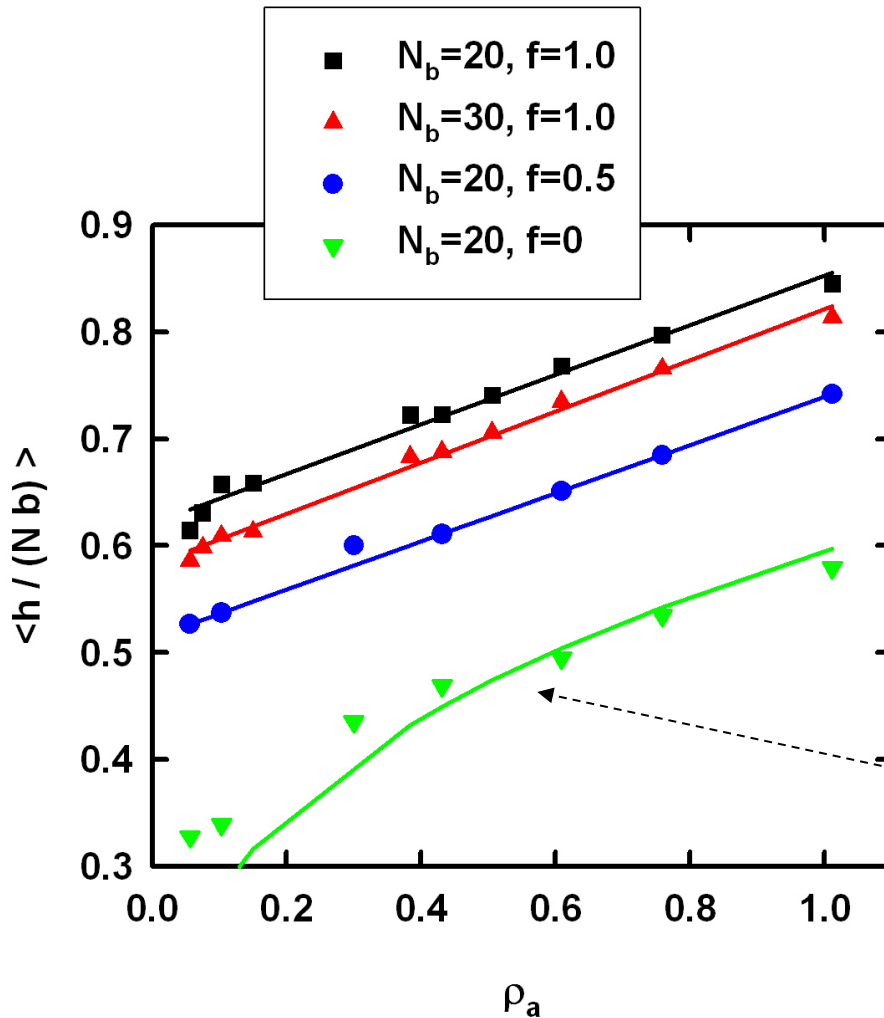
$c_s = 0.012$

$c_s = 0.239$



Modeling of Polyelectrolyte Brushes with Salt *Journal of Physical Chemistry B*, **114**, 7274-7285, (2010) (with Cyrille Ibergay and Patrice Malfreyt)

# Height of brush with grafting density



Charged brush

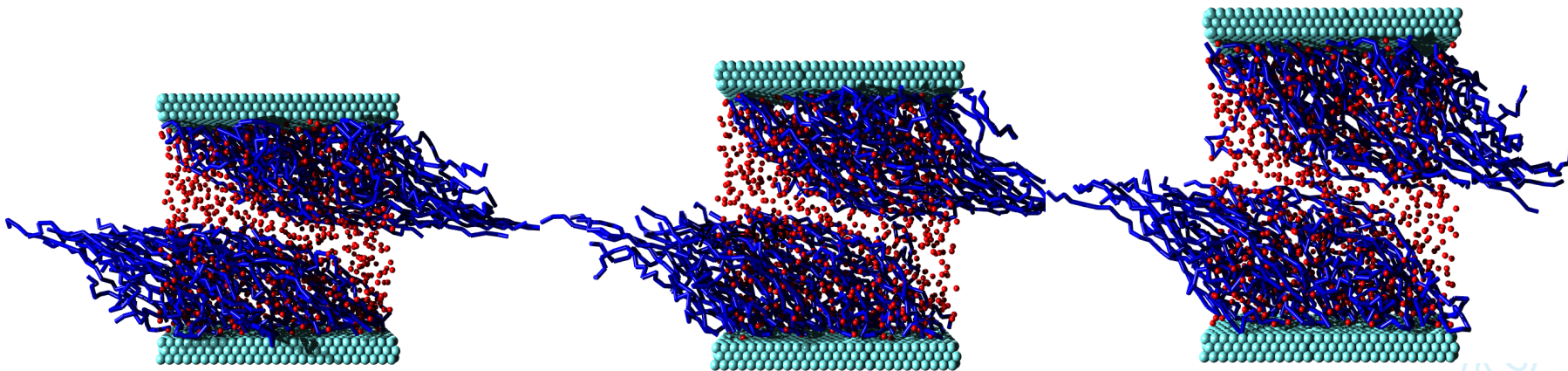
$$\frac{h}{N_b b} \approx \frac{f + d^2 \rho_a}{1 + f}$$

Neutral brush

$$\frac{h}{(N_b b)} \approx \rho_a^{1/3}$$



# Configurations of charged bilayers under shear



$D = 13$

$f=0.5$

$\dot{\gamma}_a = 0.6$

$D = 17$

$f=0.5$

$\dot{\gamma}_a = 0.6$

$D = 21$

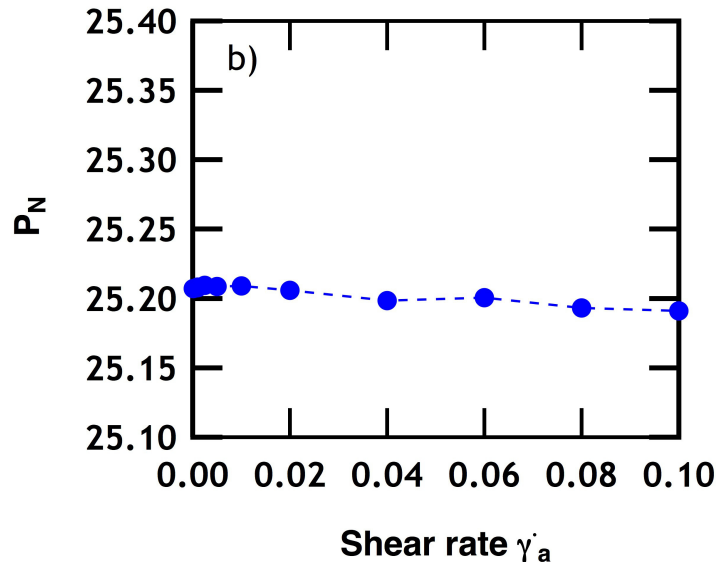
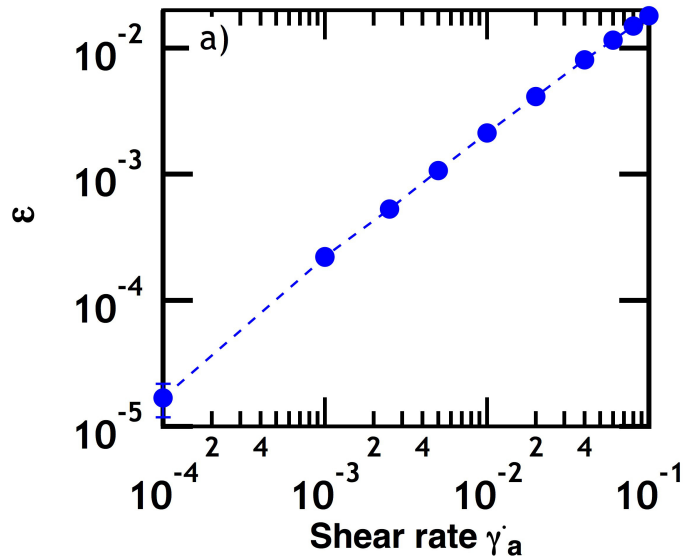
$f=0.5$

$\dot{\gamma}_a = 0.6$

The kinetic friction coefficient of neutral and charged polymer brushes  
Soft Matter **9** 2966-2972, 2013 (Goujon, Malfreyt, Ghoufi and Tildesley)

What has the lower friction coefficient,  
a neutral or fully charged polymer?

# The effect of shear rate on friction coefficient



$$\varepsilon = -P_{xz} / P_{zz}$$

The friction coefficient decreases to be within the observed experimental range for low shear (a shear rate of  $10^{-4}$  in DPD units corresponds to ca.  $10^6 \text{ s}^{-1}$ )

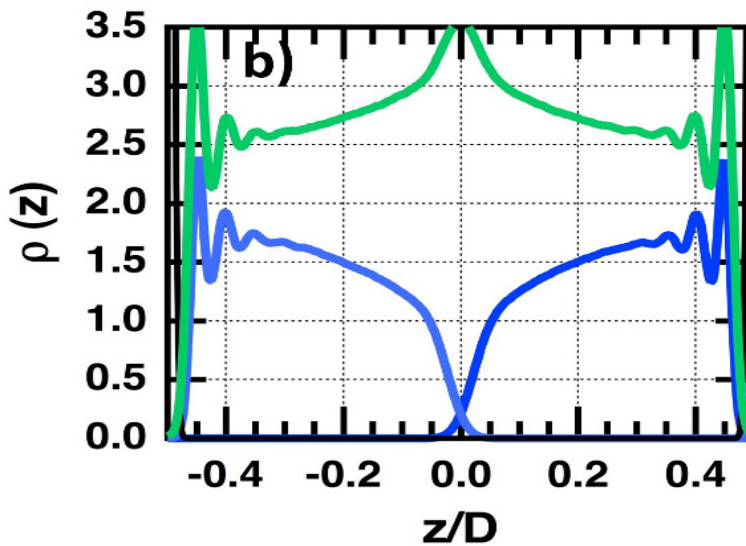
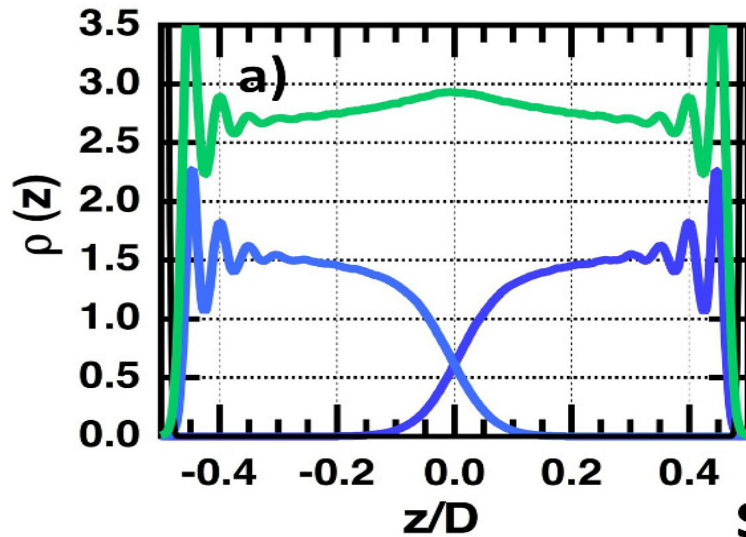
$$\varepsilon_{\text{exp}} = 0.0006-0.001 \quad 298\text{K}$$

$$\varepsilon_{\text{dpd}} = 0.00002-0.0003 \quad 298\text{K}$$

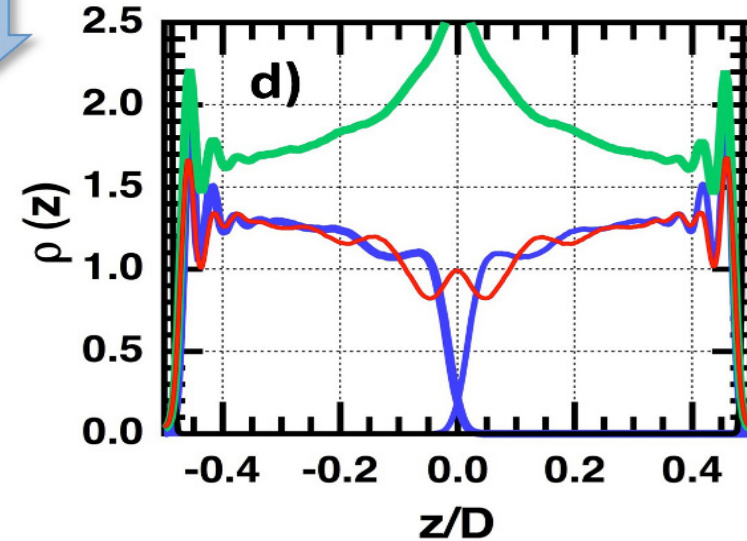
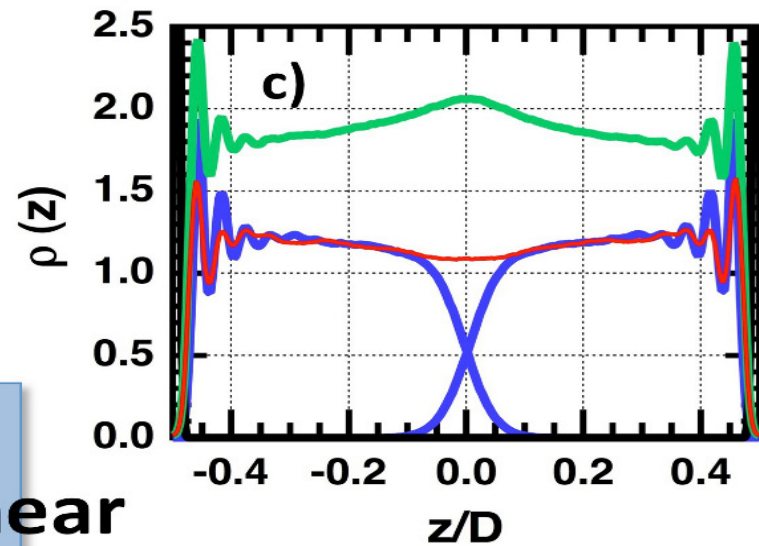
The higher values are for the higher compressions with  $D/D_0=0.2$ . This behaviour requires a more detailed consideration at even lower shear rates

# The effect of charge

## Neutral brushes

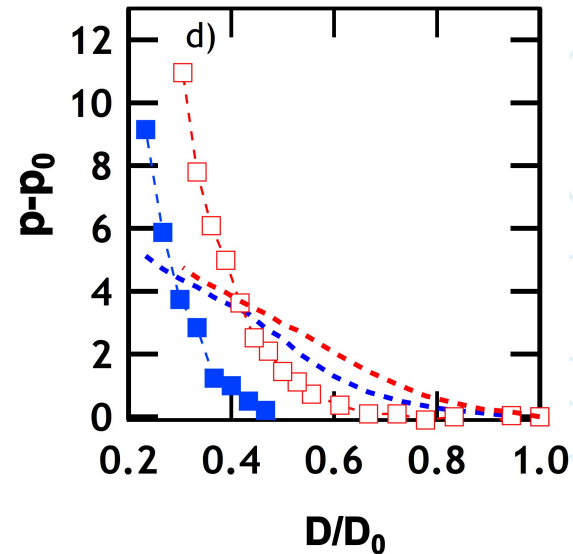
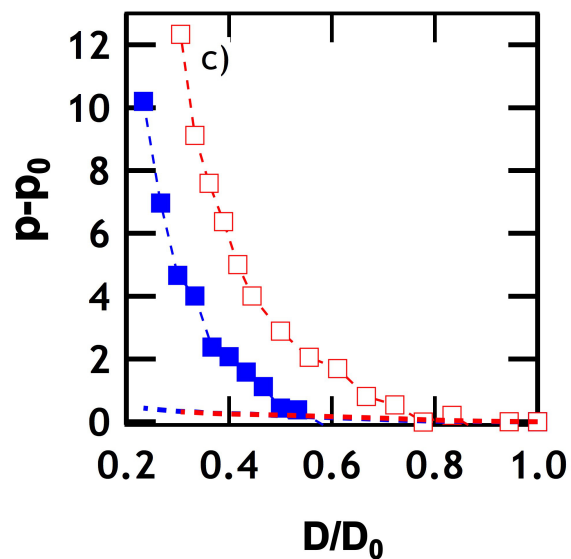
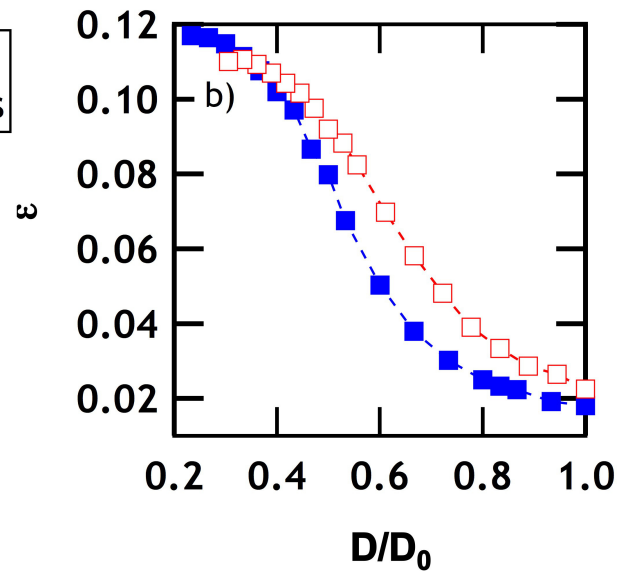
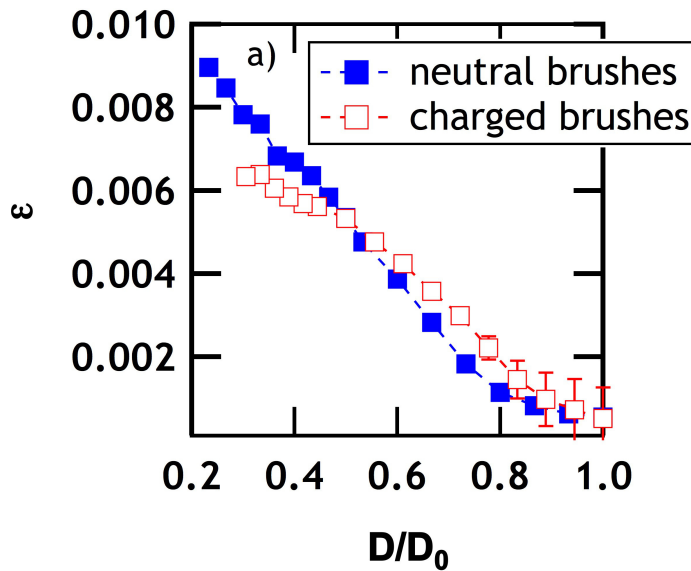


## Charged brushes

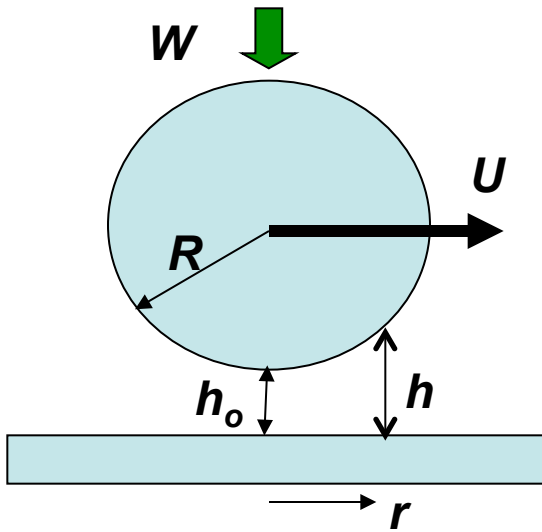


shear

# Charged and neutral brushes



# Reminder



Gap

$$h = h_0 + \frac{r^2}{2R}$$

Defines a contact area

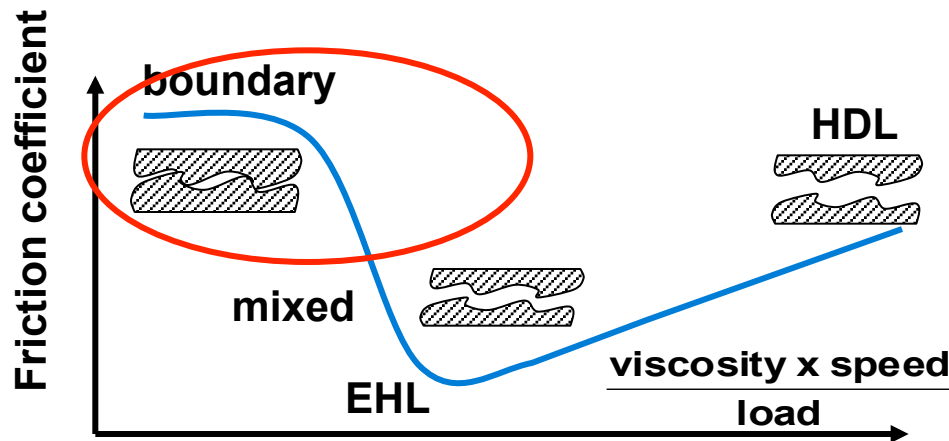
$$r^2 \approx 2Rh_0$$

Tangential force

$$T = \eta \dot{\gamma} \times \pi r^2 \approx \frac{\pi \eta U r^2}{h_0} \quad \left[ \dot{\gamma} \approx \frac{U}{h_0} \right]$$

Friction coefficient

$$\mu = \frac{T}{W} \approx \frac{\pi \eta U r^2}{W h_0} \approx 2\pi R \times \frac{\eta U}{W}$$



hydrodynamic part of the Stribeck curve

Pyotr Kapitza

J Tech Phys 25, 747 (1955)

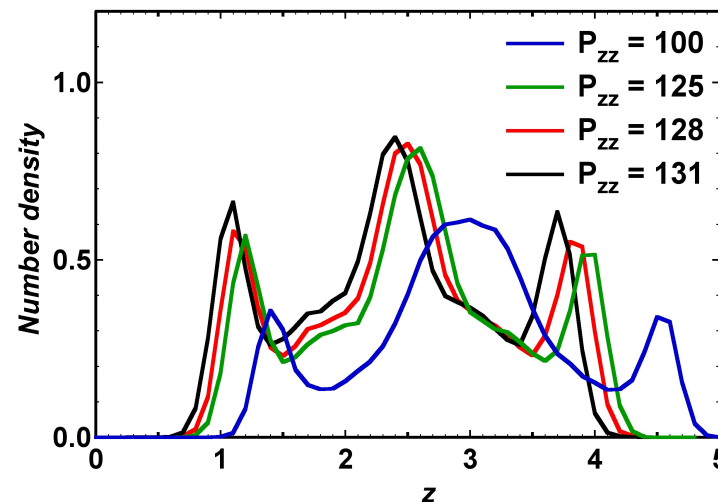
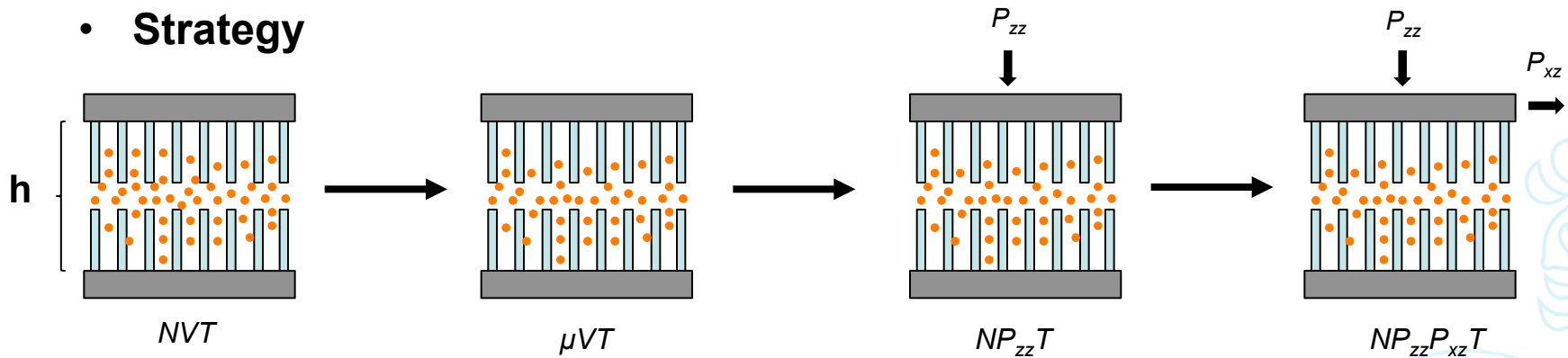
# Static friction of using Monte Carlo Methods

- **Isostress-Isostrain** ensemble with **configurational bias** methods

- Fixed variables:  $P_{zz}$ ,  $P_{xz}$ ,  $N$ ,  $T$

- DPD soft potential

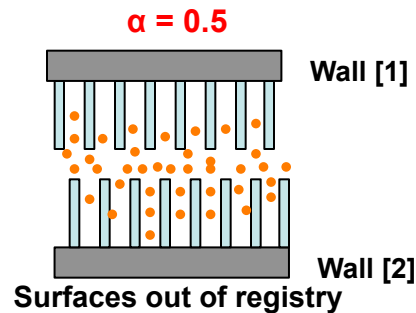
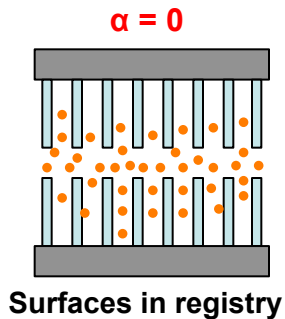
- **Strategy**



# Calculating Static friction of polymer brushes

- Quasi-static approach for shear** (Chusman *et al*, *Phys. Rev. B*, 1993; Fuchs *et al*, *Phys. Rev. E*, 1998)

The thermodynamic state of the film passes through a succession of equilibrium states, each having a different average alignment of the walls ( $\alpha$ )



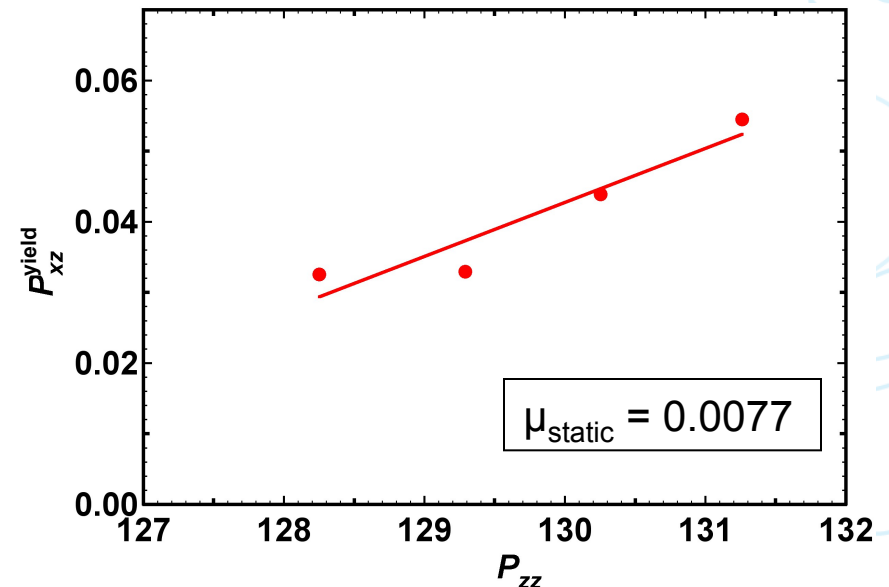
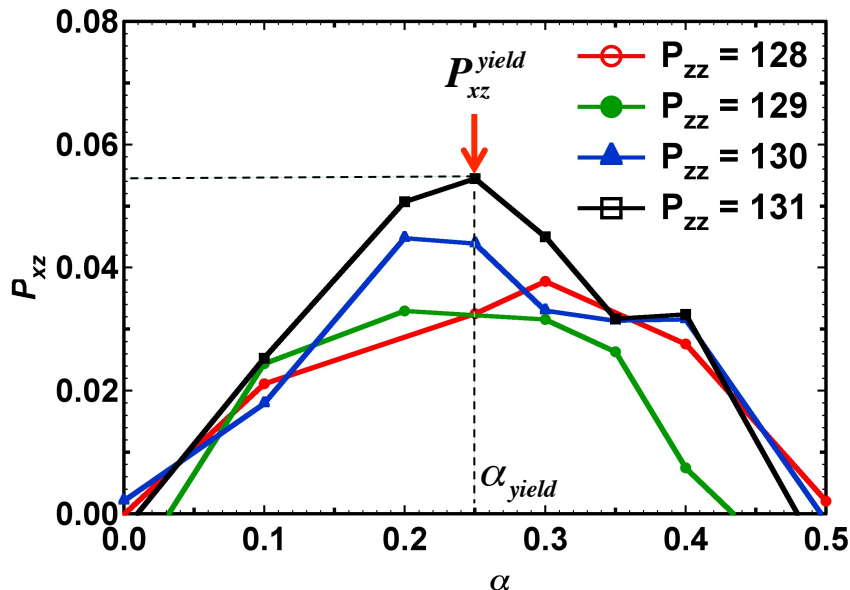
Relative position of the wall atoms in both walls

$$x_i^{[2]} = x_i^{[1]} + \alpha \times l$$

$$y_i^{[2]} = y_i^{[1]}$$

$$z_i^{[2]} = z_i^{[1]} + \delta h$$

$l =$  lattice constant



# Conclusion

- DPD simulation of neutral polymer brushes reproduce the experimental force-distance curves
- Simulation of polyelectrolytes show that the brush height depends on charge and grafting density and the behaviour is in the non-linear osmotic brush regime .In excess salt, small dipoles are created at the upper limit of the brush. Scaling of brush height with salt concentration is observed (index  $-1/3$ )
- The simulated frictions coefficients from dpd are of the same order of magnitude as the experimental estimates, but no better than this - strongly shear rate dependent.
- Friction decreases with increasing charge fraction at fixed surface separation at high compressions in the model and in experiment

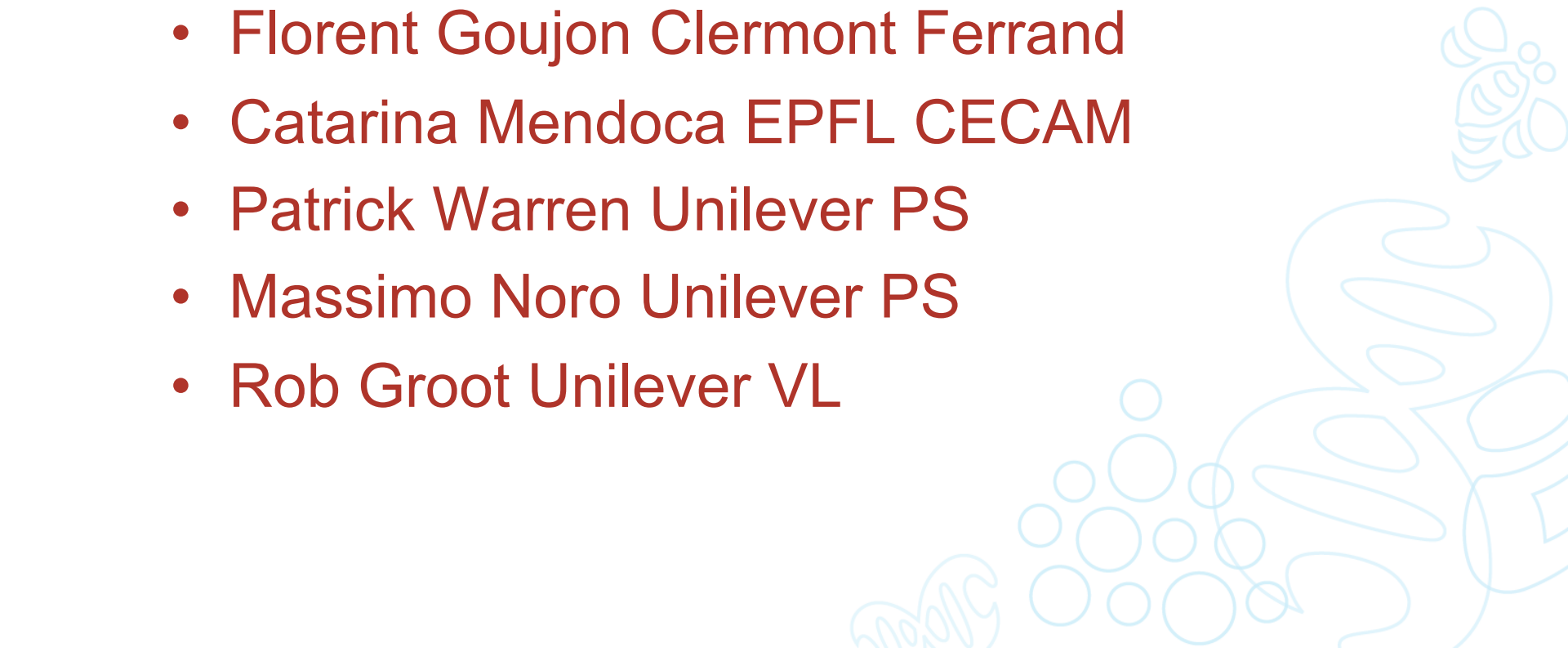


# Opportunities

- Static friction coefficients could be calculated using iso-stress Monte Carlo simulations?
- Much more work needs to be done on finding the force field correspondence between the atomistic and dpd levels. This may be case by case dependent
- We need to include surface irregularities in a controlled way
- We need to find a mapping that accommodates lower shear rates
- We need to developed polarizable models for dpd

# Thanks again



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# DFT calculations

