

# Critical assessment of the performance of mBEEF and RPBE XC functionals for C<sub>2</sub>H<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> adsorption on transition metal surfaces

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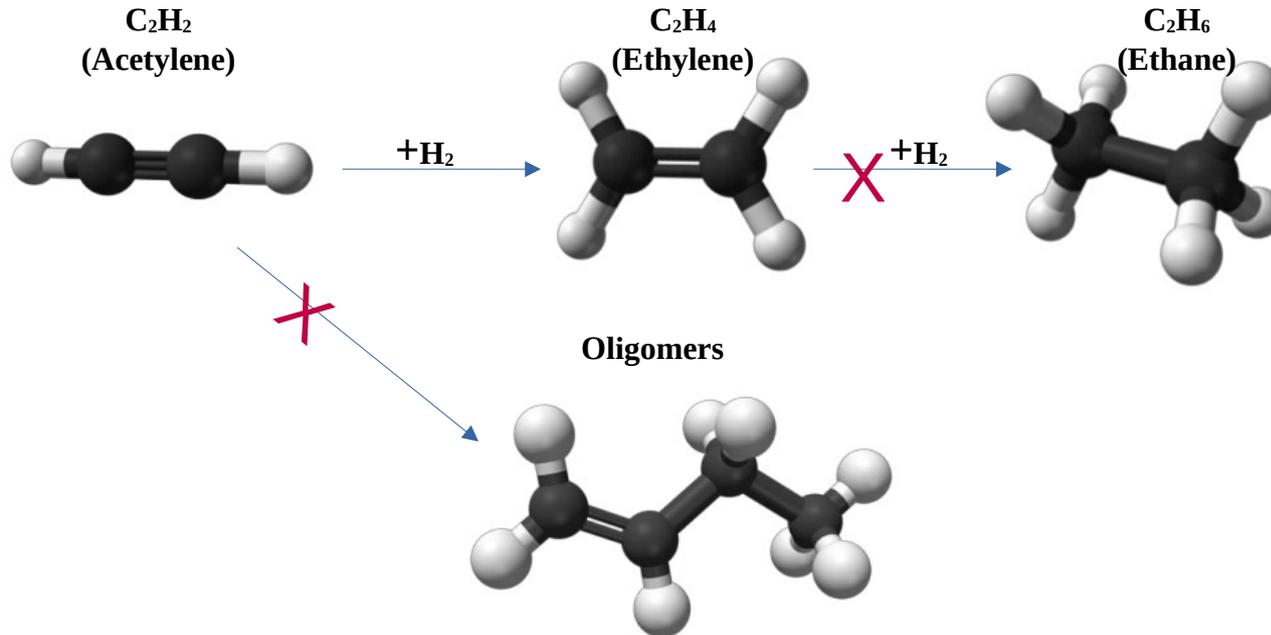
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# Outline

- The importance of the adsorption of  $C_2H_2$  and  $C_2H_4$  molecules on TMSs
- Why focusing on mBEEF and RPBE XC functionals
- Investigated properties to evaluate the selected XC functionals
  - Vibrational frequencies
  - Adsorption energy

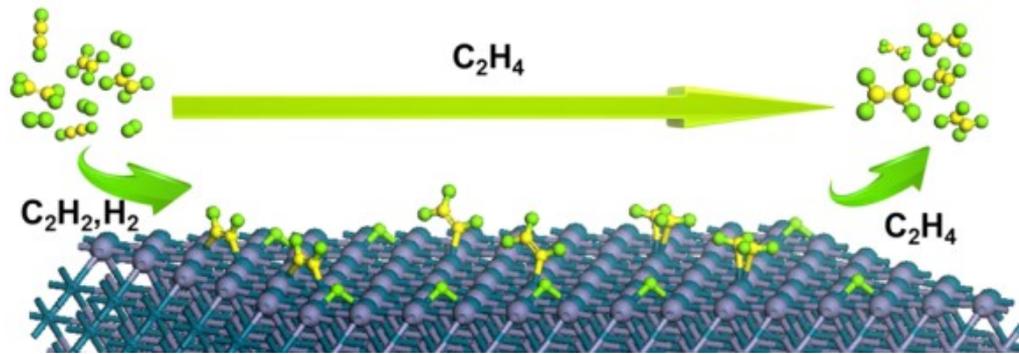
# The importance of $C_2H_2$ and $C_2H_4$ adsorption on TMSs

- $C_2H_4$  is one of the largest chemical building blocks for polymers production
- $C_2H_2$  presents in many  $C_2H_4$ 's synthesis ways which deactivates the catalyst that is used for the polymerization of  $C_2H_4$
- Using TM-based heterogeneous catalysts for selective hydrogenation:
  - A highly selective catalyst to convert all of the  $C_2H_2$  to  $C_2H_4$
  - Prevent over-hydrogenation and oligomerization of  $C_2H_2$  to form higher molecular weight compounds



# Why focusing on mBEEF and RPBE XC functionals

- Computational study is one of the powerful tools to investigate such processes



<sup>1</sup> Photo is taken from: H. Zhou, X. Yang, L. Li, X. Liu, Y. Huang, X. Pan, A. Wang, J. Li, and T. Zhang, ACS Catal. 6, 1054–1061 (2016).

# Why focusing on mBEEF and RPBE XC functionals

- Computational study is one of the powerful tools to investigate processes
  - Among them, DFT is a useful theoretical approach in condensed matter physics for the catalytic systems
  - The reliability of DFT results strongly depends on the choice of XC functional
    - **RPBE** GGA-XC functional which is specifically developed to treat **adsorption properties** can accurately predict chemisorption energies<sup>1-4</sup>
    - A recently work on TM surfaces shows **mBEEF** metaGGA-XC functional provides good agreement of **surface energies** and **work functions** with related experimental data<sup>5</sup>
    - Previous benchmark studies show that the challenge of finding an optimal functional that could simultaneously capture both covalent and non-covalent interactions persists

<sup>1</sup> B.-T. Teng, X.-D. Wen, M. Fan, F.-M. Wu, and Y. Zhang, Physical Chemistry Chemical Physics 16, 18563 (2014).

<sup>2</sup> J. Wellendorff, T. L. Silbaugh, D. Garcia-Pintos, J. K. Nørskov, T. Bligaard, F. Studt, and C. T. Campbell, Surface Science 640, 36 (2015).

<sup>3</sup> J. Wellendorff, K. T. Lundgaard, A. Møgelhøj, V. Petzold, D. D. Landis, J. K. Nørskov, T. Bligaard, and K. W. Jacobsen, Phys. Rev. B 85, 235149 (2012).

<sup>4</sup> S. M. Sharada, R. K. Karlsson, Y. Maimaiti, J. Voss, and T. Bligaard, Physical Review B 100, 035439 (2019).

<sup>5</sup> L. Kaban, I. Kowalec, R. Catlow, and A. Logsdail, (2021).

# Vibrational Mode Analysis for $C_2H_2$ and $C_2H_4$ on molecules

## **Problem:**

*Limitation/Lack of enough experimental results for simple properties of  $C_2H_2$  and  $C_2H_4$  on the pure and alloy TM surfaces (e.g., adsorption energy)*

## **Question:**

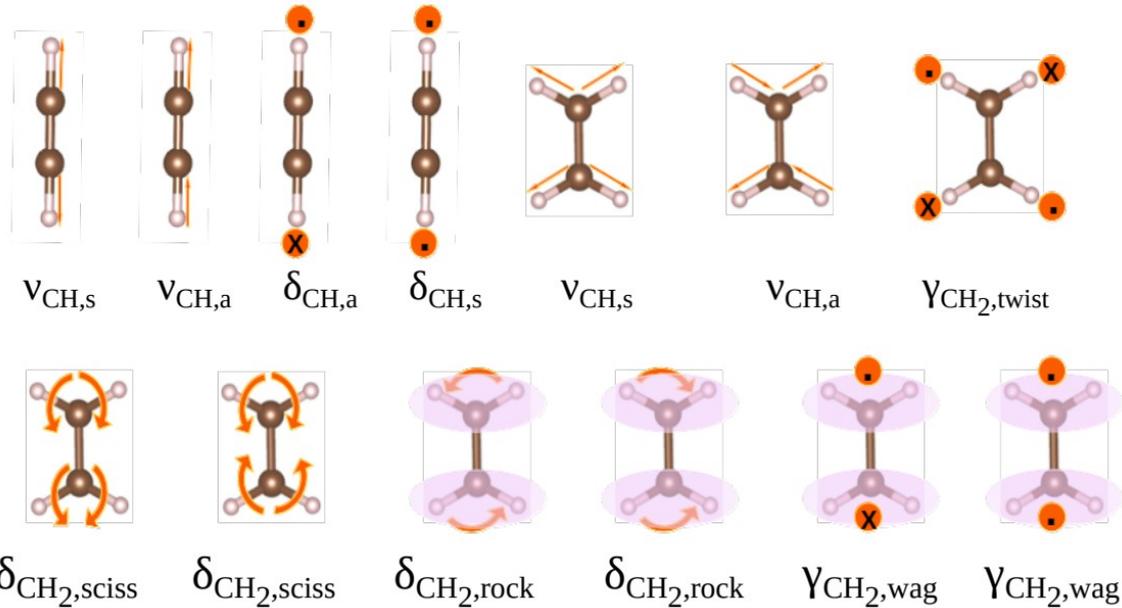
*What other properties can also be compared with the experimental results?*

## **Idea:**

*The vibrational modes of  $C_2H_2$  and  $C_2H_4$  molecules on the mono-metal surface had been measured mainly by EELS (electron energy loss spectroscopy) and actively reported in 1980~90s.*

*The XC functional that can describe the vibrational modes of  $C_2H_2$  and  $C_2H_4$  on the mono-metal surfaces can also describe those on the corresponding alloy surface.*

# Vibrational Modes of C<sub>2</sub>H<sub>2</sub> and C<sub>2</sub>H<sub>4</sub>



$\nu$  : stretching modes  
 $s$  : symmetry modes

$\delta$  : in-plane bending modes  
 $a$  : asymmetry modes

$\gamma$  : out-of-plane bending modes

# Computational details

- DFT calculations:

FHI-aims, tight setting, applying dipole correction, scalar-relativistic (atomic ZORA)

- Seven-layer (111) slabs of Pd, Pt, Cu, and Rh: four bottom-layer fixed

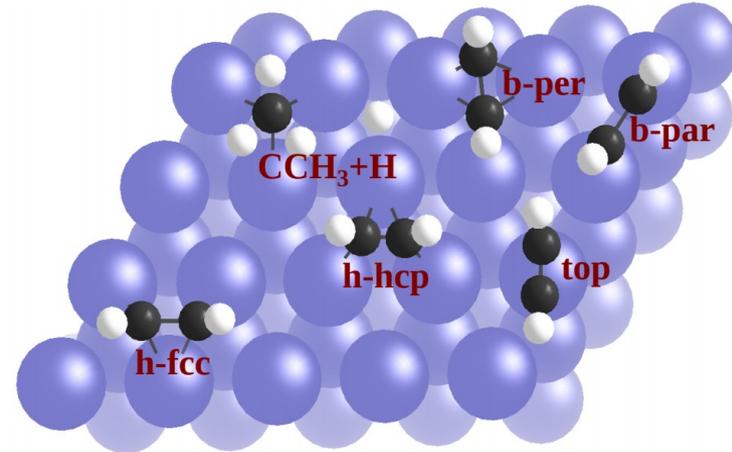
- Vacuum: at least 15 Å

- Employing Phonopy

- Adsorption energy:

$$E_{\text{ads}} = E_{\text{mol+slab}} - E_{\text{slab}} - E_{\text{mol}}$$

- C<sub>2</sub>H<sub>4</sub> dissociation on Pt(111) under the reaction:



# Vibrational Frequencies of gas-phase C<sub>2</sub>H<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> molecules

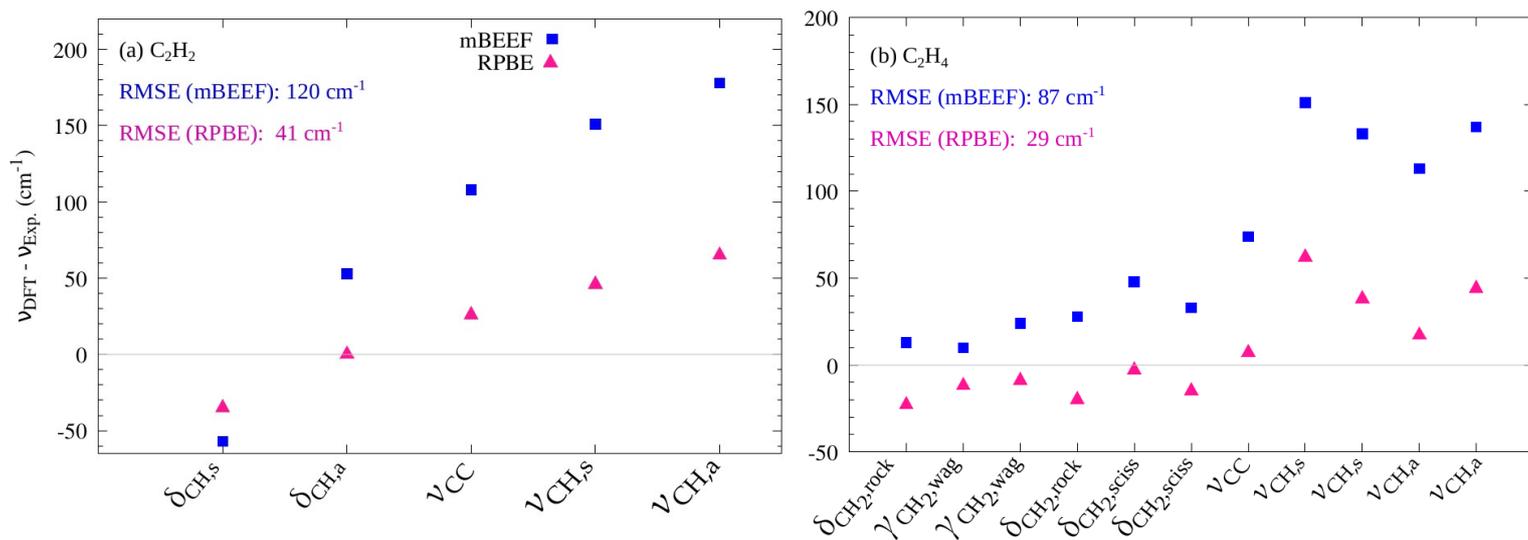
The vibrational frequencies (in cm<sup>-1</sup>) of the C<sub>2</sub>H<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> molecules obtained by mBEEF and RPBE XC functionals along with the experimental data.

C <sub>2</sub> H <sub>2</sub>	mBEEF	RPBE	Exp. <sup>a</sup>
$\delta_{CH,s}$	555	578	612
$\delta_{CH,a}$	782	730	729
$\nu_{CC}$	2082	2001	1974
$\nu_{CH,s}$	3446	3342	3295
$\nu_{CH,a}$	3551	3439	3373
RMSE (cm <sup>-1</sup> )	120	41	
C <sub>2</sub> H <sub>4</sub>			Exp. <sup>b</sup>
$\delta_{CH_2,rocking}$	839	804	826
$\gamma_{CH_2,wagging}$	950	929	940
$\gamma_{CH_2,wagging}$	973	941	949
$\gamma_{CH_2,twisting}$	1080	1032	—
$\delta_{CH_2,rocking}$	1250	1203	1222
$\delta_{CH_2,scisoring}$	1390	1340	1342
$\delta_{CH_2,scisoring}$	1477	1430	1444
$\nu_{C-C}$	1697	1631	1623
$\nu_{CH,s}$	3140	3052	2989
$\nu_{CH,s}$	3159	3065	3026
$\nu_{CH,a}$	3216	3121	3103
$\nu_{CH,a}$	3242	3150	3105
RMSE (cm <sup>-1</sup> )	87	29	

<sup>a</sup> G. Herzberg, Electronic spectra and electronic structure of polyatomic molecules, Vol. 3 (van Nostrand, 1966).

<sup>b</sup> D. Van Lerberghe, I. Wright, and J. Duncan, Journal of Molecular Spectroscopy 42, 251 (1972).

# Vibrational Frequencies of gas-phase $C_2H_2$ and $C_2H_4$ molecules



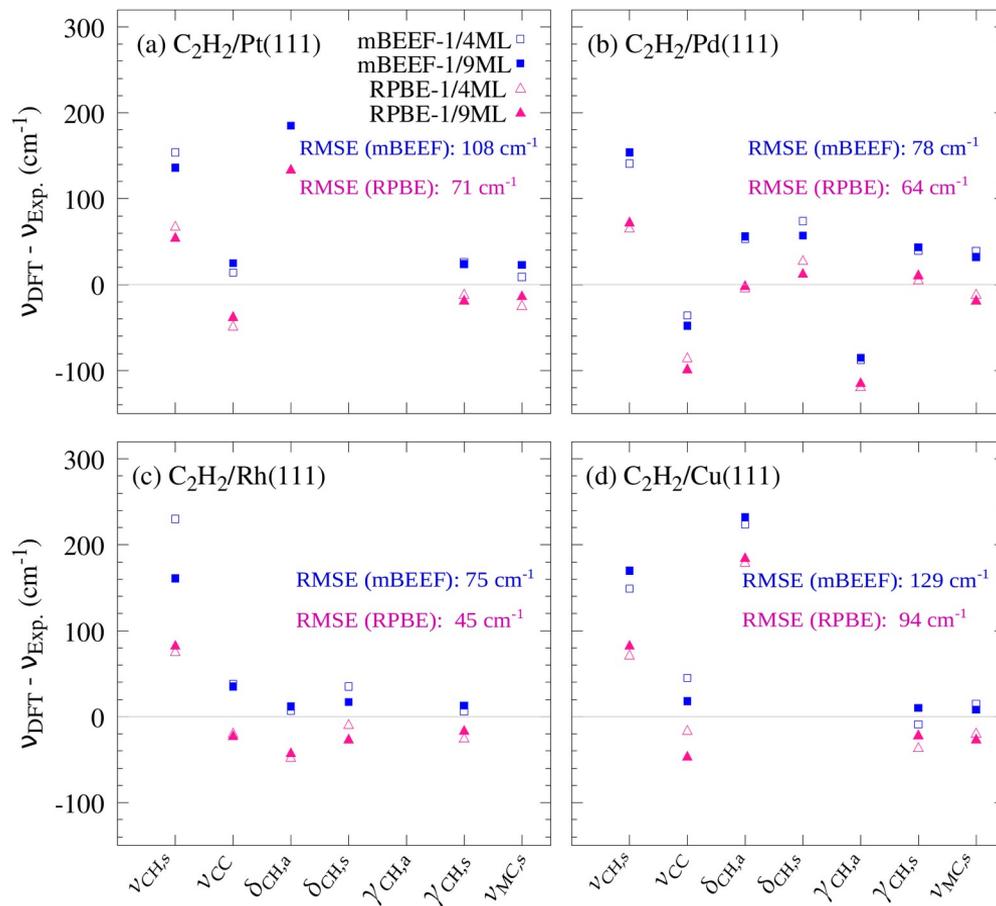
Frequency differences of different vibrational modes of gas-phase  $C_2H_2$  and  $C_2H_4$  molecules with the related experimental values.

# Stretching force constants of the gas-phase $C_2H_2$ and $C_2H_4$ molecules

The stretching C-C and C-H force constants  $k$  (in N/m) obtained by mBEEF and RPBE. The related experimental values are obtained from the experimental vibrational frequencies.

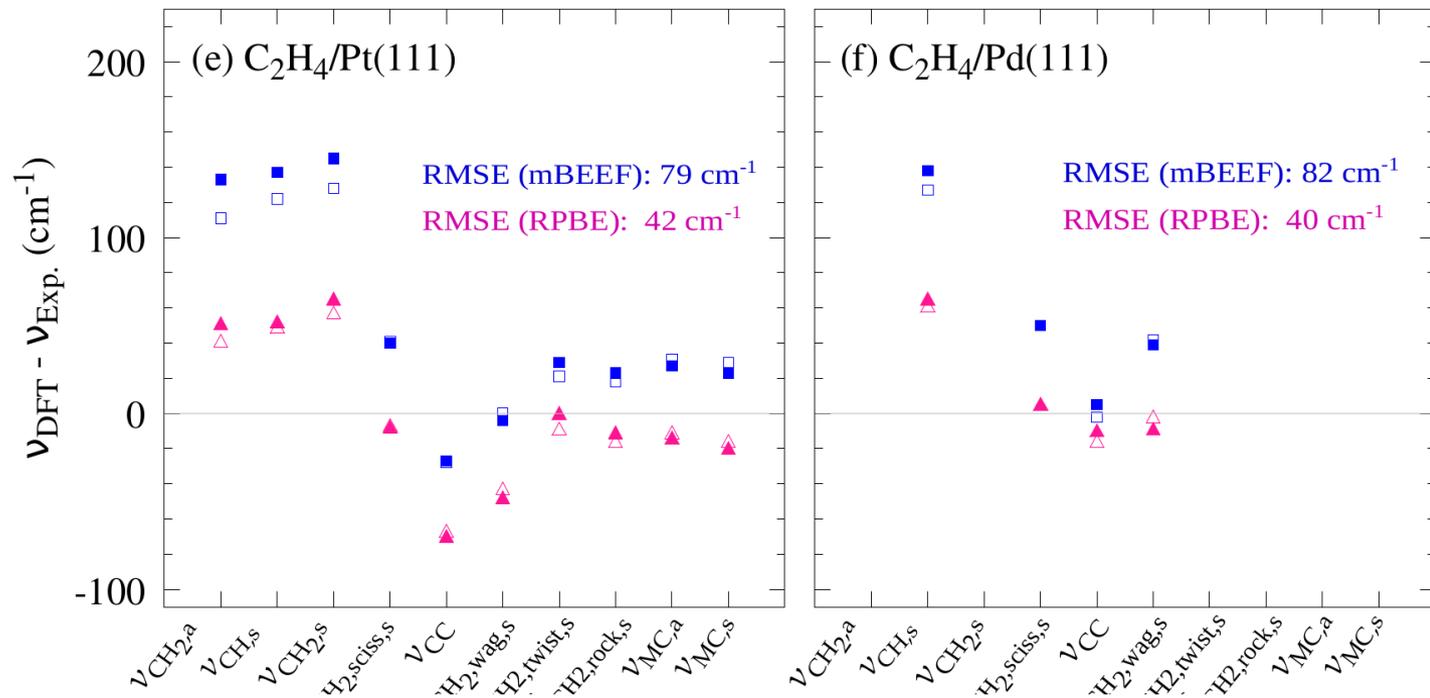
$C_2H_2$	mBEEF	RPBE	Exp.
$k_{C-C}$	1533	1416	1378
$k_{C-H}(s)$	691	648	623
$k_{C-H}(a)$	650	612	595
$C_2H_4$			
$k_{C-C}$	1019	941	932
$k_{C-H}(s)$	540	510	489
$k_{C-H}(s)$	547	514	502
$k_{C-H}(a)$	566	534	527
$k_{C-H}(a)$	576	544	528

# Vibrational Frequencies of adsorbed C<sub>2</sub>H<sub>2</sub> molecule



Frequency differences of different vibrational modes of adsorbed C<sub>2</sub>H<sub>2</sub> molecule with the related experimental values.

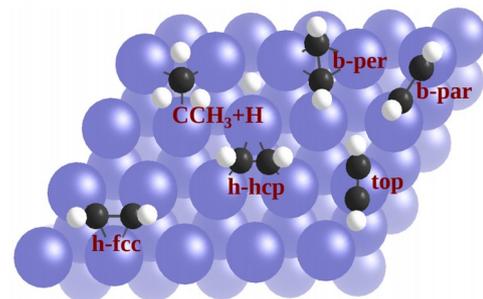
# Vibrational Frequencies of adsorbed C<sub>2</sub>H<sub>4</sub> molecule



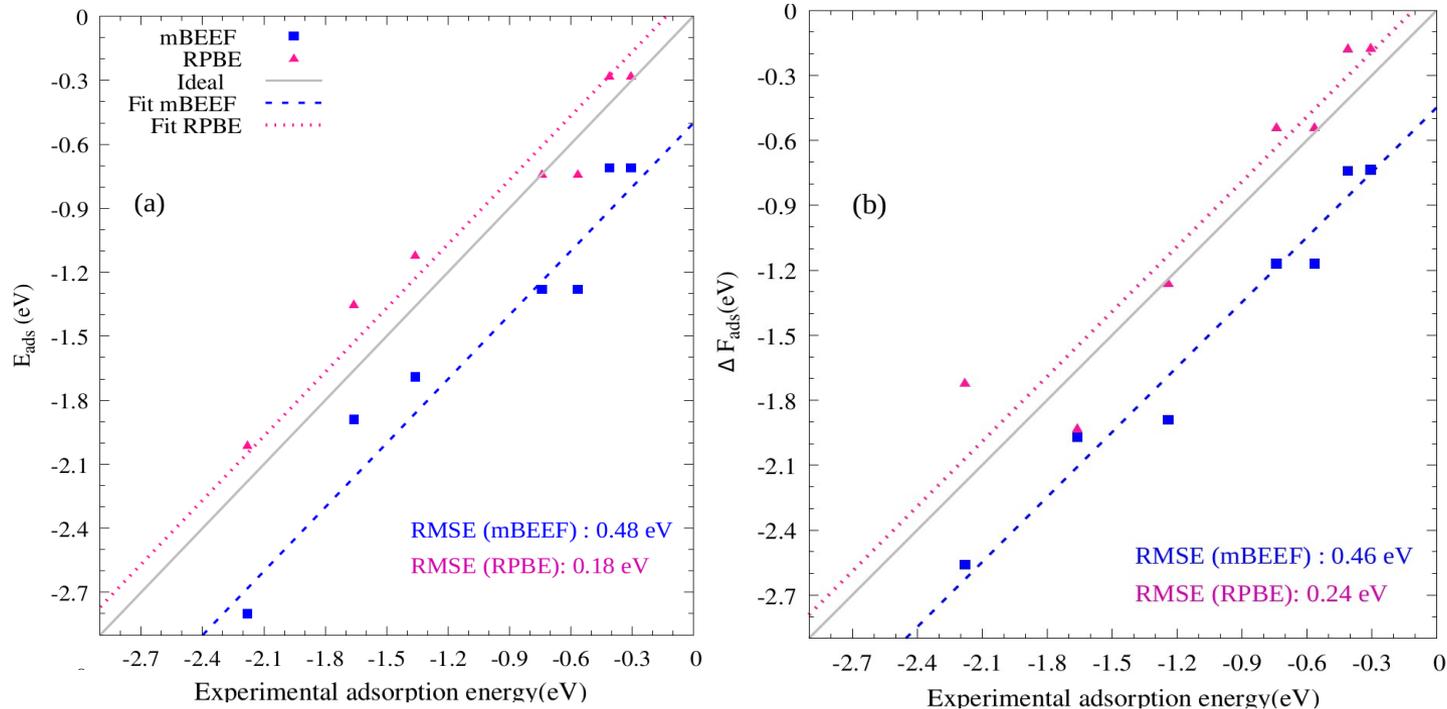
Frequency differences of different vibrational modes of adsorbed C<sub>2</sub>H<sub>4</sub> molecule with the related experimental values. The blue and pink colors indicate the differences obtained from mBEEF and RPBE functionals, respectively.

# Adsorption energy and geometry to evaluate the mBEEF and RPBE XC functionals

system	site	$\theta$ (ML)	mBEEF	RPBE	Exp.	Others.
C <sub>2</sub> H <sub>2</sub> /Pt(111)	h-fcc	1/4	-2.58	-1.80		-2.37 <sup>[42]</sup> (PW91), -2.26 <sup>[47]</sup> (PW91)
	1/9		-2.60	-1.90		-2.11 <sup>[51]</sup> (BEEF-vdW)
	1/16		-2.80	-2.01	-2.18 (initial, 173K) <sup>[50]</sup>	
	cluster					-2.17 <sup>[52]</sup> (B3LYP)
	b-par	1/4	changed	-1.39		-1.99 <sup>[42]</sup> (PW91)
	top	1/4	-0.69	-0.23		-0.73 <sup>[42]</sup> (PW91)
C <sub>2</sub> H <sub>4</sub> /Pt(111)	top	1/4	-0.71	-0.28	-0.41 ± 0.1 (112K) <sup>[48]</sup>	-0.76 <sup>[43]</sup> (PW91)
		1/4			-0.22 -- -0.39 (110K) <sup>[54]</sup>	-0.55 <sup>[55]</sup> (PW)
		1/4				-0.40 <sup>[60]</sup> (Tight-Binding)
		1/9	-0.93	-0.36		-0.87 <sup>[57]</sup> (PW91)
		cluster				-1.07 <sup>[52]</sup> (B3LYP)
	b-par	1/4	-1.28	-0.74	-0.39 -- -0.74 (110K) <sup>[61]</sup>	-1.21 <sup>[63]</sup> (PW91)
		1/4			-0.74 (100K) <sup>[36]</sup>	-1.26 <sup>[65]</sup> (PW)
		1/4				-0.58 <sup>[60]</sup> (Tight-Binding)
		1/9			-1.24 (initial) <sup>[50]</sup>	-1.25 <sup>[57]</sup> (PW91)
		cluster				-1.77 <sup>[52]</sup> (B3LYP)
		0.6 < $\theta$ < 1.2			-1.41 <sup>[58]</sup>	
	CCH <sub>3</sub> +H	1/9	-1.69	-1.12	-1.36 (300K) <sup>[49]</sup>	-1.65 <sup>[12]</sup> -1.74 <sup>[49]</sup> (PBE)
		1/9			-1.24 (300K) <sup>[59]</sup> <sup>a</sup>	-1.20 <sup>[12]</sup> (RPBE)
		1/9				-1.75 <sup>[49]</sup> (optPBE)
		1/9				-1.83 <sup>[42]</sup> (optPBE-vdW)
	1/9				-1.34 <sup>[12]</sup> (BEEF-vdW)	
	1/9				-1.43 <sup>[49]</sup> (BEEF)	
	1/9				-1.68 <sup>[42]</sup> (MS2)	
	1/9				-2.21 <sup>[12]</sup> (SCAN)	
	1/9				-2.33 <sup>[12]</sup> (SCAN+rVV10)	
	1/9				-2.21 <sup>[42]</sup> (HSE06)	
	1/9				-1.44 <sup>[53]</sup> (PW91)	
	1/16	-1.89	-1.35	-1.66 (initial, T=303K) <sup>[50]</sup>		
	$\theta = 0.05$			-1.43 <sup>[59]</sup> <sup>a</sup>		
	$\theta < 0.10$			-1.80 ± 0.04 <sup>[60]</sup>		
	$\theta = 0.17$			-1.29 ± 0.03 <sup>[60]</sup>		
	cluster				-1.32 <sup>[52]</sup> (B3LYP)	



# Adsorption energy and geometry to evaluate the mBEEF and RPBE XC functionals



(a) Calculated adsorption energies ( $E_{ads}$ ) and (b) adsorption free energies ( $\Delta F_{ads} = E_{ads} + F_{vib}$ ) of  $C_2H_2$  and  $C_2H_4$  on the Pt(111) surface versus corresponding experimental values. Data points of each functional fitted to  $y=x+a$  are also shown by dashed lines and dotted lines for mBEEF and RPBE functionals, respectively. The gray line shows the ideal  $y=x$ .

# Conclusion

- mBEEF results in higher RMSE of vibrational modes:

- gas-phase:

C<sub>2</sub>H<sub>2</sub>: RMSE(mBEEF): 120 cm<sup>-1</sup>    RMSE(RPBE): 41 cm<sup>-1</sup>

C<sub>2</sub>H<sub>4</sub>: RMSE(mBEEF): 87 cm<sup>-1</sup>    RMSE(RPBE): 29 cm<sup>-1</sup>

- adsorbed:

RMSE(mBEEF): 118 cm<sup>-1</sup>                  RMSE(RPBE): 61 cm<sup>-1</sup>

- The local minima are so sensitive to the initial starting geometry

- b-par bridge site for C<sub>2</sub>H<sub>2</sub> adsorption cannot be captured via mBEEF

- RPBE results in lower RMSE in adsorption energy

- RMSE of adsorption energy:                          mBEEF: 0.48 eV    RPBE: 18 eV

- RMSE of adsorption free energy:                          mBEEF: 0.46 eV    RPBE: 24 eV

**Thank you...**

**Questions?**